

## USER MANUAL

# FrequenC

Version 2.0

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# FrequenC

## A Library of C Functions for Frequency Stability Analysis

FrequenC is a library of C functions for the analysis of frequency stability that is distributed along with the Stable32 software package as a 32-bit Microsoft Windows dynamic link library (Freque32.dll). It includes many of the specialized functions needed to analyze time and frequency data. Included are functions for conversion between time and frequency data, conversion between time and frequency domains, and the calculation of various Allan, Hadamard and total variances from phase or frequency data. The library also includes functions for drift calculation and removal, common statistical functions, and several special functions for identifying noise types and determining confidence intervals. These functions use an array data format that defines analysis limits and can include gaps. The following tables list the FrequenC Library functions:

Allan Variance Functions	
CalcPhaseSigma	Calculate Allan deviation for phase data
CalcFreqSigma	Calculate Allan deviation for frequency data
CalcPhaseModSigma	Calculate modified Allan deviation for phase data
CalcFreqModSigma	Calculate modified Allan deviation for frequency data
CalcPhaseOverlapSigma	Calculate Allan deviation for phase data using overlapping samples
CalcFreqOverlapSigma	Calculate Allan deviation for frequency data using overlapping samples
CalcFastModSigma	Quickly calculate modified Allan deviation for gapless phase data
CalcGreenhallModSigma	Calculate mod sigma for gapless phase data using Greenhall method

Hadamard Variance Functions	
CalcHadamardDev	Calculate the 3-sample Hadamard deviation for phase data
CalcPhaseOverlapHadamardDev	Calculate the Hadamard deviation for phase data using overlapping samples
CalcFreqOverlapHadamardDev	Calculate the Hadamard deviation for freq data using overlapping samples

## FrequenC Library Reference Manual

Total Variance Functions	
ModTotvarCalc	

Other Stability Functions	
TIErms	
CalcMTIE	
CalcFastMTIE	
Thêo1	

Drift Functions	
CalcQuadraticDrift	Calculate least-squares quadratic fit to phase data
CalcFirstDiff	
CalcSecondDiff	Calculate average of 2nd differences of phase data
CalcThreePointDrift	Calculate frequency drift using first, middle and last phase data points
CalcLinFreqDrift	Calculate least-squares linear fit for frequency data
CalcBisection Drift	Calculate freq drift using averages of first & last halves of freq data
CalcLogFreqDrift	Calculate least-squares log fit for frequency data
RemoveQuadraticDrift	Remove quadratic (frequency) drift from phase data
RemoveLinFreqDrift	Remove linear drift from frequency data
RemoveLogFreqDrift	Remove log drift from frequency data

Conversion Functions	
ConvFreqToPhase	Convert from frequency data to phase data
ConvPhaseToFreq	Convert from phase data to frequency data
CalcDomain	Calculate the time and frequency domain noise parameter $h(\alpha)$
ConvDomain	Convert between time and frequency domains
DateToMJD	Convert calendar date to Modified Julian Date
MJDToDate	Convert Modified Julian Date to calendar date

Common Statistical Functions	
FindMinMax	Find min and max of phase or frequency data
FindMedian	
CalcMean	Calculate average of phase or frequency data
CalcPhaseStdDev	Calculate the standard deviation for phase data
CalcFreqStdDev	Calculate the standard deviation for frequency data

Data Modification	
ScaleData	Scale phase or frequency data by $a+bx$
NormalizeData	Normalize phase or freq data to zero mean
AveragePhaseData	Do averaging of phase data
AverageFreqData	Do averaging of frequency data
FillGaps	Fill gaps in phase or frequency data
FindFreqOutliers	Find, and optionally remove, outliers in frequency data

Special Functions	
CalcDegFree	Calculate # degrees of freedom for overlapping frequency data
CalcInvChiSqr	Calculate value of chi squared for certain # of degrees of freedom
CalcChiSqrProb	Calculate the area under the chi squared distribution
CalcNormalProb	Calculate the value of the normal deviate
CountGaps	Count # gaps in phase or frequency data
FindPlotScale	Find scale factor for plotting phase or freq data
CalcBias	Calculate the value of the B1 bias function for zero deadtime & integer mu
CalcBias1	Calculate the value of the B1 bias function
CalcBias2	Calculate the value of the B2 bias function
CalcBias3	Calculate the value of the B3 bias function
CalcRatio	Calculate the value of the R(n) function

### • License

A license is hereby granted for the use of this software within the immediate user group that purchased it. The FrequenC Library source and object code may be installed on any number of computers within that group, and backup copies may be made, but only one copy of the Library may be used at any time. Programs compiled using the FrequenC Library may be distributed without any royalty payment, but the Library source or object code may not be distributed unless a copy of the Library is purchased for every copy that is distributed.

The FrequenC functions have been extensively tested, but it is never possible to declare software completely bug-free. No warranty is made, nor is any liability assumed, in connection with the use of this software.

### • Other Licenses

Portions of the FrequenC library utilize code adapted from other sources, and the user is required to obtain licenses from those vendors, as necessary, before utilizing it. A list of those source codes and their vendors is as follows:

The Hammer Library (Version 2.40 of 3/9/1990)  
O.E.S. Systems  
1906 Brushcliff Road  
Pittsburgh, PA 15221

IPC-TC-006 Science and Engineering Tools (Revision 8.0 June 1992)  
Quinn-Curtis, Inc.  
18 Hearthstone Drive  
Medfield, MA 02052

Numerical Recipes in C  
Cambridge University Press  
40 West 20th Street  
New York, NY 10011

Specific references to these source codes are made in the text headers of the applicable FrequenC library files.

### • Installation

The FrequenC Library is distributed in packed form. To install it, copy the INSTALL.EXE file to the desired directory on your hard disk, and run INSTALL to unpack the Library files. The INSTALL program may then be deleted.

- **Files**

The FrequenC package includes source files for all functions, and a header file that contains ANSI C prototypes for the functions. These source files may be compiled into a library using the compiler and memory model of your choice. Also included is test data, and a driver programs that demonstrate the use of each function.

- **Data Format**

The FrequenC functions use an one-dimensional array format for phase or frequency data where the first three elements hold the number of data points, and the start and end analysis limits. The data is assumed to represent equally-spaced points, with gaps denoted by the value zero. All zeros are considered gaps in frequency data, while only embedded zeros are considered gaps in phase data. The sizes of the data arrays are determined by the calling program.

- **Drift Analysis Functions**

A complete set of drift analysis functions are provided for the calculation of linear and logarithmic drift for frequency data, and quadratic and second-difference drift for phase data. The "Calc" functions calculate the drift parameters, and the "Remove" functions drift-correct the data. These functions are summarized in the following table:

Drift Type	Phase Data	Frequency Data
Linear	CalcThreePointDrift()	CalcLinFreqDrift() RemoveLinFreqDrift() CalcBisectionDrift()
Log		CalcLogFreqDrift() RemoveLogFreqDrift()
2nd-Difference	CalcSecondDiff()	
Quadratic	CalcQuadraticDrift() RemoveQuadraticDrift()	

The arguments of all these functions include the name of the data array (x or y). The analysis functions have arguments for pointers to the relevant drift parameters (\*p\_slope, \*p\_intercept, etc.), and a pointer to the fit variance (\*p\_variance). Drift parameter calculations are direct except for the logarithmic case where an iterative algorithm is used. The removal functions have parameters for the values of the drift parameters (slope, intercept, etc.) to be subtracted. Drift removal does not include calculation of these parameters.

- **Variance Functions**

A complete set of Allan, Hadamard and total variance functions are provided for the calculation of those statistics for phase or frequency data. These functions are summarized in the following table:

Variance Type	Phase Data	Frequency Data
Standard	CalcPhaseStdDev()	CalcFreqStdDev()
Normal Allan (2-sample)	CalcPhaseSigma()	CalcFreqSigma()
Overlapping Allan	CalcPhaseOverlapSigma()	CalcFreqOverlapSigma()
Modified Allan	CalcPhaseModSigma() CalcFastModSigma() (no gaps) CalcGreenhallModSigma() (no gaps)	CalcFreqModSigma()
Time (multiply Mod $\sigma_y(\tau)$ by $\tau/\sqrt{3}$ )	CalcPhaseModSigma() CalcFastModSigma() (no gaps)	CalcFreqModSigma()
Hadamard (3-sample)	CalcHadamardDev()	

The arguments of these functions include the name of the data array (x or y) and a pointer to the deviation (\*p\_dev) or sigma (\*p\_sig) value. The phase data functions also have an argument for the averaging time (tau). In addition, the overlapping and modified Allan variance functions include an argument for the averaging factor (m). All these functions except CalcFastModSigma() handle gaps in the data represented by zeros. Only embedded zeros are considered gaps in phase data. All zeros are considered gaps in frequency data. The CalcFastModSigma() and CalcGreenhallModSig() functions are available for gapless phase data only. They are faster than CalcPhaseModSigma(), and much faster than CalcFreqModSigma(), especially for a large data set at a large averaging factor. The modified Allan variance for a large data set at a large averaging factor should therefore be performed with gapless phase data if possible. The ConvFreqToPhase() and FillGaps() functions may be used to allow this to be done for frequency data having gaps.

- **Progress Indicator**

An example of a calculation function prototype that includes a progress indicator is as follows:

```
int WINAPI CalcPhaseModSigma(F_TYPE x[], F_TYPE *p_sig, F_TYPE tau,
    int m, BOOL *bAbort, BOOL bProgress,
    void (*ProgressFunction)(int nPercentDone, char *szMessage));
```

The last argument is a pointer to a void function having the signature:

```
void WriteProgressMessage(int nPercentDone, char *szMessage);
```

where the first parameter is the % of the calculation that is complete, and the second parameter is a string to be displayed by the progress indicator. This function is not included in the FrequenC library because it is specific to the particular application. Both the % done and message text are generated by the calculation function.

The calculation function is called as:

```
nModSig=NewCalcPhaseModSigma(fWorkData, &fModSig, fTau*nAF, nAF,
    &bAbort, !bAllTau, WriteProgressMessage);
```

where the last argument is the name of the progress function.

- **Abort Flag**

The variance calculation functions having a progress indicator also have an argument `BOOL *bAbort`, a pointer to an integer flag that indicates whether the calculation should be aborted. This variable must be defined and initialized to `FALSE (0)` before each calculation. If it is set to `TRUE (1)` during a calculation, the calculation will be aborted the next time the progress indicator is updated.

- **Source Code**

C source code for the FrequenC library is not included with the Stable32 software package, but is available for separate purchase. Please contact Hamilton Technical Services for further information.

- **List of Source Files**

The following is a list of all the source files that comprise the FrequenC Library. The source file names directly follow their corresponding function names. Source files are included for each individual function and combined into one master source file, `FREQUENC.C`. The FrequenC header file, `FREQUENC.H`, must be included in any source file that uses the FrequenC Library. Two test programs are included in both source and executable form. `TEST_FC` tests all the FrequenC functions. `CALC_FC` is an interactive calculator-mode program for some of the FrequenC functions. The source file listings in this document are for informational purposes only, and the individual source files should be used for compiling the FrequenC library.

- **Master Source File:**

`FREQUENC.C` All FrequenC Functions

- **Function Source Files**

<code>AFD.C</code>	<code>AverageFreqData()</code>
<code>APD.C</code>	<code>AveragePhaseData()</code>
<code>CB.C</code>	<code>CalcBias()</code>
<code>CB1.C</code>	<code>CalcBias1()</code>
<code>CB2.C</code>	<code>CalcBias2()</code>
<code>CB3.C</code>	<code>CalcBias3()</code>
<code>CBD.C</code>	<code>CalcBisectionDrift()</code>
<code>CCSP.C</code>	<code>CalcChiSqrProb()</code>
<code>CFD.C</code>	<code>CalcDegFree()</code>
<code>CD2.C</code>	<code>CalcDomain()</code>
<code>CFMS.C</code>	<code>CalcFreqModSigma()</code>
<code>CFMS2.C</code>	<code>CalcFastModSigma()</code>
<code>CFOS.C</code>	<code>CalcFreqOverlapSigma()</code>
<code>CFS.C</code>	<code>CalcFreqSigma()</code>
<code>CFSD.C</code>	<code>CalcFreqStd Dev()</code>
<code>CFTP.C</code>	<code>ConvFreqToPhase()</code>
<code>CG.C</code>	<code>CountGaps()</code>
<code>CGMS.C</code>	<code>CalcGreenhallModSigma()</code>
<code>CHD.C</code>	<code>CalcHadamardDev()</code>
<code>CICS.C</code>	<code>CalcInvChiSqr()</code>
<code>CLFD.C</code>	<code>CalcLinFreqDrift()</code>
<code>CLFD2.C</code>	<code>CalcLogFreqDrift()</code>
<code>CM.C</code>	<code>CalcMean()</code>
<code>CNP.C</code>	<code>CalcNormalProb()</code>

```

CPMS.CCCalcPhaseModSigma()
CPOS.CCCalcPhaseOverlapSigma()
CPS.C          CalcPhaseSigma()
CPSD.CCCalcPhaseStdDev()
CPTF.CCConvPhaseToFreq()
CQD.C          CalcQuadraticDrift()
CR.C           CalcRatio()
CSD.C          CalcSecondDiff()
CTPD.CCCalcThreePointDrift()
CD.C           ConvDomain()
DTM.C          DateToMJD()
FFO.C          FindFreqOutliers()
FG.C           FillGaps()
FMM.C          FindMinMax()
FPS.C          FindPlotScale()
MTD.C          MJDToDate()
ND.C           NormalizeData()
RLFD.CRemoveLinFreqDrift()
RLFD2.C        RemoveLogFreqDrift()
RQD.C          RemoveQuadraticDrift()
SD.C           ScaleData()

```

- **Header File**

The FREQUENC.H header file invokes several Standard C Library header files, contains several macro definitions, and gives prototype information for the FrequenC Library functions. It should be included with each of the FrequenC Library source files when they are compiled. The F\_TYPE definition determines the type of floating point variable that is used for the phase and frequency data arrays and other FrequenC variables. It can be defined as either float or double.

The PHASE and FREQ definitions are useful for determining the datatype parameter. The PSD\_Y, PSD\_X, PSD\_P, PSD\_L, SIG\_Y, MODSIG\_Y and SIG\_X definitions are useful for setting the domain conversion type parameter. The W\_PM, F\_PM, W\_FM, F\_FM and RW\_FM definitions are useful for setting the domain conversion alpha parameter.

- **Test Program Files**

```

TEST_FC.C      Source File for Test Program for all FrequenC Functions
TEST_FC.EXE    Executable FrequenC Test Program
TEST.DAT       Test Data for TEST_FC Test Program

```

```

TEST_CD.C      Source File for Test Usage of Domain Conversion Functions
TEST_CD.EXE    Executable FrequenC Domain Conversion Program

```

```

CALC_FC.C      Source File for Calculator Mode for some FrequenC Functions
CALC_FC.EXE    Executable FrequenC Calculator Program

```

- **Reference**

An excellent reference for many of the FrequenC Library functions is *NIST Technical Note 1337*, "Characterization of Clocks and Oscillators", Edited by D.B. Sullivan, D.W. Allan, D.A. Howe and F.L. Walls. Other references are given in the Stable32 User Manual and the FrequenC Library source files.

## • FrequenC.DLL Contents

Dump of file FrequenC.dll

File Type: DLL

Section contains the following Exports for FrequenC.dll

```

0 characteristics
3E7C7282 time date stamp Sat Mar 22 09:26:10 2003
0.00 version
1 ordinal base
93 number of functions
93 number of names

```

ordinal	hint	name
1	0	_AddPSD@8 (00001190)
2	1	_AddSigma@4 (000013A0)
3	2	_AverageFreqData@8 (00001000)
4	3	_AveragePhaseData@8 (000012B0)
5	4	_BasScale@28 (00001440)
6	5	_BreakDate@16 (00001400)
7	6	_CalcBias1@12 (00001800)
8	7	_CalcBias2@8 (00001B00)
9	8	_CalcBias3@12 (00001D20)
10	9	_CalcBias@8 (000016F0)
11	A	_CalcBisectionDrift@4 (000021D0)
12	B	_CalcChiSqrProb@8 (000022A0)
13	C	_CalcDegFree@12 (00003150)
14	D	_CalcDiffusionFreqDrift@20 (00003440)
15	E	_CalcDomain@36 (00002930)
16	F	_CalcFastMTIE@16 (00003A20)
17	10	_CalcFastModSigma@20 (00003FA0)
18	11	_CalcFirstDiff@8 (000037A0)
19	12	_CalcFreqHadamardDev@8 (000038F0)
20	13	_CalcFreqModSigma@12 (00003DC0)
21	14	_CalcFreqOffset@16 (000041A0)
22	15	_CalcFreqOverlapHadamardDev@12 (000043B0)
23	16	_CalcFreqOverlapSigma@12 (00004570)
24	17	_CalcFreqSigma@8 (000046F0)
25	18	_CalcFreqStdDev@8 (000047E0)
26	19	_CalcGreenhallModSigma@20 (00004C10)
27	1A	_CalcHadamardB1@8 (00004DE0)
28	1B	_CalcHadamardDev@16 (000051E0)
29	1C	_CalcInvChiSqr@8 (00005420)
30	1D	_CalcLinFreqDrift@16 (00005B20)
31	1E	_CalcLogFreqDrift@20 (00005D10)
32	1F	_CalcMTIE@24 (00010170)
33	20	_CalcMean@12 (00006030)
34	21	_CalcNormalProb@4 (00006110)
35	22	_CalcPhaseHadamardDev@16 (000062C0)
36	23	_CalcPhaseModSigma@32 (00006500)
37	24	_CalcPhaseOverlapHadamardDev@20 (00006840)
38	25	_CalcPhaseOverlapSigma@20 (00006B00)
39	26	_CalcPhaseSigma@16 (00006D50)
40	27	_CalcPhaseStdDev@16 (00006F30)
41	28	_CalcQuadraticDrift@28 (00007600)
42	29	_CalcRatio@12 (000079A0)

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43	2A	_CalcSecondDiff@8 (00007D40)
44	2B	_CalcStarB1@20 (00007C50)
45	2C	_CalcThreePointDrift@4 (00007EC0)
46	2D	_CheckFrequenC@0 (00003790)
47	2E	_ConvDomain@36 (00002510)
48	2F	_ConvFreqToPhase@20 (00004940)
49	30	_ConvPhaseToFreq@20 (000071C0)
50	31	_ConvPhaseToFreqUsingTimetags@28 (000073B0)
51	32	_CountGaps@8 (00004B90)
52	33	_DateConv@24 (00007F80)
53	34	_DateToJulian@4 (00008180)
54	35	_DateToMJD@12 (00008250)
55	36	_DayOfWeek@4 (00008090)
56	37	_EDF@12 (000082B0)
57	38	_FillFloatGaps@8 (00008310)
58	39	_FillGaps@8 (00008670)
59	3A	_FindFreqOutliers@12 (00008580)
60	3B	_FindMedian@12 (000088E0)
61	3C	_FindMinMax@16 (00009010)
62	3D	_FindPlotScale@24 (00009170)
63	3E	_GenNoise@24 (00009580)
64	3F	_HadTotvarBias@4 (0000B180)
65	40	_HadTotvarCalc@24 (0000B210)
66	41	_HadTotvarEDF@8 (0000B7F0)
67	42	_HadamardEDF@12 (0000A1A0)
68	43	_HistoCalc@24 (0000A070)
69	44	_JulianToDate@4 (0000B8F0)
70	45	_MJDToDate@16 (0000FF20)
71	46	_MJDtoDOY@4 (0000FFE0)
72	47	_MJDtoGPS@4 (00010140)
73	48	_MakeDate@12 (0000BCD0)
74	49	_MedDev@8 (0000BA30)
75	4A	_ModTotvarBias@4 (0000F9F0)
76	4B	_ModTotvarCalc@32 (0000FA80)
77	4C	_ModTotvarEDF@8 (00010060)
78	4D	_MultiTaperSpectrumCalc@52 (0000BDA4)
79	4E	_NoiseID@20 (000103D0)
80	4F	_NormalizeData@16 (00010320)
81	50	_RemoveDiffusionFreqDrift@28 (00010B20)
82	51	_RemoveFreqOffset@24 (00010BD0)
83	52	_RemoveLinFreqDrift@20 (00010CC0)
84	53	_RemoveLogFreqDrift@28 (00010D50)
85	54	_RemoveQuadraticDrift@28 (00010E00)
86	55	_RoundAxes@12 (00010770)
87	56	_ScaleData@24 (00011FE0)
88	57	_SpectrumCalc@44 (00010ED0)
89	58	_TIErms@12 (000125D0)
90	59	_TotalvarBias@20 (000120B0)
91	5A	_TotvarBias@8 (00012170)
92	5B	_TotvarCalc@24 (00012220)
93	5C	_TotvarEDF@8 (00012540)

### Summary

```

6000 .data
1000 .idata
3000 .rdata
3000 .reloc
1D000 .text

```



The FrequenC Library	
<b>NAME:</b> AverageFreqData	<b>FUNCTION:</b> Average frequency data by an integer factor
<b>SYNOPSIS:</b> int AverageFreqData(F_TYPE y[], int af)	
F_TYPE y[]	Frequency data array: y[0] = # data points y[1] = analysis start point y[2] = analysis end point
int af	Averaging factor
<b>RETURN:</b> int	The # of data points in averaged data, or -1 if error
<b>REMARKS:</b> All data points are processed regardless of analysis limits. Averaging factor must be >0 and ≤ # data points. Averaging Factor=1 does nothing. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* frequency data array */ int af;  /* averaging factor */ int num;   /* # points in averaged data */ . . af=2;  /* assign value to averaging factor */ num=AverageFreqData(y, af);                          /* average freq data */ if(num== -1)   /* check for error */ {     printf("\nError");                               /* error message */ } else {     printf("\n# Averaged Data Points = %d", num);    /* display num */ }           </pre>	
<b>SEE ALSO:</b> AveragePhaseData()	
<b>REFERENCE:</b> None	

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```

/*****
/*
/*                                     AverageFreqData()
/*
/*      Function to do averaging of frequency data
/*
/*      Parameters:      F_TYPE y[] = frequency data
/*                      y[0] = # data points
/*                      y[1] = analysis start
/*                      y[2] = analysis end
/*                      int    af  = averaging factor
/*                      = # points to combine into each average
/*
/*      Return:          int        = # data points in averaged data,
/*                      or -1 if error
/*
/*      Note:            All data points processed regardless of analysis
/*                      limits. Zeros are treated as gaps in freq data.
/*                      Error if af<1 or af> # original data points.
/*                      af=1 is OK, and results in no change in data.
/*
/*      Revision record:
/*          04/11/97      Cloned from AverageFrequencyData() of FrequenC Lib
/*                      Changed to use analysis limits
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/21/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1992-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL AverageFreqData(F_TYPE y[], int af)
{
    int i;
    int j;
    int k=3;
    int n=(int) (y[2]-y[1]+1);          /* # original data points */
    int num;
    double sum;

    if( (af<1) || (af>n) )
    {
        return(-1);                    /* error */
    }

    for(i=(int) (y[1]+2); i+af-1<=(int) (y[2]+2); i+=af)
    {
        sum=0;
        num=af;

```

```

for(j=0; j<af; j++)
{
    if(*(y+i+j))                                /* don't average in a gap */
    {
        sum+=*(y+i+j);
    }                                           /* end if */
    else
    {
        num--;
    }                                           /* end else */
}                                           /* end for */
if(num)                                       /* check if all gaps */
{
    *(y+k++)=sum/num;
}                                           /* end if */
else
{
    *(y+k++)=0;
}                                           /* end else */
}                                           /* end for */

*y=floor(n/af);
*(y+1)=1.0;
*(y+2)=*y;

return (int)*y;                               /* # data points in averaged data */
}                                           /* end AverageFreqData() */

```



The FrequenC Library	
<b>NAME:</b> AddPSD	<b>FUNCTION:</b> Add freq domain noise terms
<b>SYNOPSIS:</b> float AddPSD(float PSD[], int PSDtype)	
float PSD[]	Array of PSD terms
int PSDtype	PSD type macro (e.g. PSD_L)
<b>RETURN:</b> float	Sum of PSD noise terms
<b>REMARKS:</b> Used with CalcDomain() and ConvDomain(). See domain conversion type macros in frequenc.h	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ float PSD[5];   /* PSD array */ float sum;   /* sum of PSD terms */ . . sum=AddPSD(PSD, PSD_L);                             /* call function */ printf("\nPSD Sum = %e", sum);                      /* display result */ </pre>	
<b>SEE ALSO:</b> CalcDomain(), ConvDomain(), AddSigma()	
<b>REFERENCE:</b>	

```

/*****
/*
/*                      AddPSD()
/*
/*      Function to add freq domain noise terms
/*
/*      Revision record:
/*          05/03/97      Adapted from AddPSD() of STABLE_A.C
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/21/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1992-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

#include "frequenc.h"

float __declspec(dllexport) FAR PASCAL AddPSD(float fPSD[], int nPSDType)
{
    // Local variables
    int i;                      // Index
    float fNoise[5];           // So(f) values
    float fAll;                // Total So(f)

    if(nPSDType==PSD_L)
    {
        // Convert L(f) log values to So(f) numerical ones before adding
        // So{f}=2*10^[L(f)/10]
        for(i=0; i<5; i++)
        {
            if(fPSD[i])
            {
                fNoise[i]=(float) (2*(pow(10,fPSD[i]/10)));
            }
            else
            {
                fNoise[i]=0.0;
            }
        }

        // Sum noise terms
        fAll=fNoise[0]+fNoise[1]+fNoise[2]+fNoise[3]+fNoise[4];

        // Convert sum to L(f)
        if(fAll)
        {
            return (float) (10*log10(fAll/2));
        }
        else
        {
            return 0.0;
        }
    }
    else
    {
        return (float) (sqrt(fPSD[0]*fPSD[0]+fPSD[1]*fPSD[1]+fPSD[2]*fPSD[2]+
            fPSD[3]*fPSD[3]+fPSD[4]*fPSD[4]));
    }
}

```

The FrequenC Library	
<b>NAME:</b> AveragePhaseData	<b>FUNCTION:</b> Average phase data by an integer factor
<b>SYNOPSIS:</b> int AveragePhaseData(F_TYPE x[], int af)	
F_TYPE x[]	Phase data array: x[0] = # data points x[1] = analysis start point x[2] = analysis end point
int af	Averaging factor
<b>RETURN:</b> int	The # of data points in averaged data, or -1 if error
<b>REMARKS:</b> All data points are processed regardless of analysis limits. Averaging factor must be >0 and $\leq$ # data points. Averaging factor = 1 does nothing. Embedded zeros are treated as gaps in phase data. Averaging of phase data simply omits the intermediate points (i.e decimates the data).	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[512];                                       /* phase data array */ int af;  /* averaging factor */ int num;   /* # points in averaged data */ . . af=2;  /* assign value to averaging factor */ num=AveragePhaseData(x, af);                      /* average phase data */ (if num== -1)                                       /* check for error */ {     printf("\nError");                             /* error message */ } else {     printf("\n# Averaged Data Points = %d", num);  /* display num */ } </pre>	
<b>SEE ALSO:</b> AverageFreqData()	
<b>REFERENCE:</b> None	

## FrequenC Library Reference Manual

```

/*****
/*
/*                                     AveragePhaseData()
/*
/*      Function to average phase data by an integer factor
/*
/*      Parameters:      float x[] = phase data array
/*                      x[0] = # data points
/*                      x[1] = analysis start
/*                      x[2] = analysis end
/*                      int af    = averaging factor
/*
/*      Return:          int        = # points in averaged data,
/*                                or -1 if error
/*
/*      Note:            All data points are processed regardless of
/*                      analysis limits. Averaging phase data by
/*                      factor=af is done by simply using only every
/*                      (af)th data point. A gap is retained if it is
/*                      one of the averaged points. Error if af<1 or
/*                      af> # original data points. af=1 is OK, and
/*                      results in no change in the data.
/*
/*      Revision record:
/*          12/30/91    Created
/*          12/31/91    Renamed
/*          01/16/92    Edited per FrequenC documentation
/*          01/17/92    Edited title block
/*                      Changed return to int=# points processed
/*          01/18/92    Added error trap.
/*          02/03/96    Modified for use as Win 3.1 DLL
/*          04/21/03    Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL AveragePhaseData(F_TYPE x[], int af)
{
    int num=(int)x[0];      /* # original phase data points to be averaged */
    int i;                  /* index for averaged phase data */
    /* i goes from 1 to ((num-1)/af)+1 averaged phase data points */
    int j;                  /* index for original phase data */
    /* j starts at the analysis start offset */
    /* which is 1 for original phase data starting at 1st data point */
    /* j is incremented by the averaging factor af */

    if( (af<1) || (af>num) )
    {
        return(-1);        /* error */
    }

    j=1;
    for(i=1; i<=((num-1)/af)+1; i++)
    {
        *(x+i*2) = *(x+j*2);    /* 2 is the data array offset */
        j += af;
    }
}

```

```
    }                                     /* end for */

    x[0]=( (num-1)/af)+1;
    x[1]=1;
    x[2]=x[0];

    return( (int) x[0]);
}                                     /* end AveragePhaseData() */
```



The FrequenC Library	
<b>NAME:</b> AddSigma	<b>FUNCTION:</b> Add time domain noise terms
<b>SYNOPSIS:</b> float AddSigma(float sigma[])	
Float sigma[]	
<b>RETURN:</b> float	Sum of sigma noise terms
<b>REMARKS:</b> Used with CalcDomain() and ConvDomain().	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ float sigma[5];                                       /* sigma array */ float sum;   /* sum of sigma terms */ . . sum=AddSigma(sigma);                                /* call function */ printf("\nSigma Sum = %e", sum);                     /* display result */ </pre>	
<b>SEE ALSO:</b> CalcDomain(), ConvDomain(), AddPSD()	
<b>REFERENCE:</b>	

## FrequenC Library Reference Manual

```

/*****
/*
/*          AddSigma()
/*
/*      Function to add time domain noise terms
/*
/*      Revision record:
/*          05/03/97      Adapted from AddSigma() of STABLE_A.C
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/21/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1992-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

#include "frequenc.h"

float __declspec(dllexport) FAR PASCAL AddSigma(float fSigma[])
{
    return (float)(sqrt(fSigma[0]*fSigma[0]+fSigma[1]*fSigma[1]+fSigma[2]*fSigma[2]+
        fSigma[3]*fSigma[3]+fSigma[4]*fSigma[4]));
}
```

The FrequenC Library	
<b>NAME:</b> BreakDate	<b>FUNCTION:</b> Break down Gregorian date into month, day and year
<b>SYNOPSIS:</b> void BreakDate(long gdate, int *month, int *day, int *year)	
long gdate	Gregorian date (yyyymmdd)
int *month	Pointer to month (1-12)
int *day	Pointer to day (1-31)
int *year	Pointer to year (4-digit, e.g. 2003)
<b>RETURN:</b> void	
<b>REMARKS:</b>	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ long gdate;   /* Gregorian date */ int month;   /* month */ int day;   /* day */ int year;   /* year */ . . gdate=20030101;                                       /* set ldate */ BreakDate(gdate, &amp;month, &amp;day, &amp;year);             /* call function */ printf("\nMonth = %d, Day = %d, Year = %d", month, day, year); /* display results */ </pre>	
<b>SEE ALSO:</b> MakeDate()	
<b>REFERENCE:</b>	

## FrequenC Library Reference Manual

```

/*****
/*
/*          BreakDate()
/*
/*      Function to break down a Gregorian date into month, day and year
/*
/*      Parameters: long    gdate    Gregorian date (yyyymmdd)
/*                   int *   mo      month (1-12)
/*                   int *   da      day  (1-31)
/*                   int *   yr      year  (4-digit)
/*
/*      Return:      void          None
/*
/*      Revision record:
/*          07/17/97    Cloned from brkdate() of Hammer Library
/*                   Modified code so full 4-digit year is returned
/*          04/21/03    Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1997-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

#include "frequenc.h"                                /* FrequenC Library header file */

void __declspec(dllexport) FAR PASCAL BreakDate(LONG gdate, int *mo, int *da,
int *yr)
{
    *yr=(int) (gdate/10000L);
    *mo=(int) ((gdate/100L) % 100L);
    *da=(int) (gdate%100L);
}

```

The FrequenC Library	
<b>NAME:</b> BasScale	<b>FUNCTION:</b> Find neat plot scale
<b>SYNOPSIS:</b> int BasScale (double min, double max, int n, double* smin, double* step)	
double min	minimum data value
double max	maximum data value
int n	maximum # of divisions in plot scale
double *smin	pointer to scale minimum
double *step	pointer to step size
<b>RETURN:</b> int	1 if OK, or -1 if error
<b>REMARKS:</b> This function is recommended for a small relative data range, even though its scale choice is often sub-optimum, and the # of minor ticks is not always 5. Written by Antonio Gómez Bas based on subroutine SCALE by J.A. Nelder (1976) and W. Douglas Stirling (1981).	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* freq data array */ int n=10;   /* # plot divs */ double min, max;                                    /* data min &amp; max */ double smin, step;                                  /* scale min &amp; step size */ . . FindMinMax(y, &amp;min, &amp;max, FREQ_DATA);              /* get data min &amp; max */ BasScale(min, max, n, &amp;smin, &amp;step);                 /* get plot scale */ printf("\nMin = %e, Step = %e", smin, step);        /* display results */ </pre>	
<b>SEE ALSO:</b> FindPlotScale(), RoundAxes()	
<b>REFERENCE:</b> A. Bas, "Finding Neat Scales for Plotting", C Users Journal, March 2000	

## FrequenC Library Reference Manual

```

/*****
/*
/*          BasScale()
/*
/*      Function to find neat plot scale
/*      Ref: A. Bas, "Finding Neat Scales for Plotting", CUJ, March 2000
/*
/*      Parameters:      double XMin          = minimum data value
/*                      double XMax          = maximum data value
/*                      int N                = max # divs in plot scale
/*                      double *SMin         = pointer to scale minimum
/*                      double *Step        = pointer to step size
/*
/*      Return:          int                  = 1 if OK or 0 if error
/*
/*      Written by Antonio Gómez Bas, 1999 based on subroutine SCALE
/*      by W. Douglas Stirling
/*
/*      Revision record:
/*          03/09/02      Downloaded and adapted
/*                      Runs AOK and seems to produce nice tight scales
/*          03/19/03      Adapted for FrequenC DLL
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 2002-3 Hamilton Technical Services All Rights Reserved
/*
*****/

#include "frequenc.h"

int __declspec(dllexport) FAR PASCAL BasScale (double XMin, double XMax,
        int N, double* SMin, double* Step)
{
    int    iNegScl;        // Negative scale flag
    int    iNm1;           // Number of scale subintervals
    double lfIniStep;      // Initial step
    double lfSclStep;      // Scaled step
    double lfTmp;           // Temporary value
    double lfSclFct;       // Scaling back factor
    double lfSMax;         // Scale maximum value
    int     it;             // Iteration counter
    int     i;              // Neat step counter

    // Neat steps

    // Original version had these steps
    int Steps [] = {10, 12, 15, 16, 20, 25, 30, 40, 50, 60, 75, 80, 100, 120, 150};

    // Try reduced choices for use in case of narrow range
    // int Steps [] = {10, 20, 50, 100};

    int iNS = sizeof (Steps) / sizeof (Steps [0]);

    // Some checks
    if (XMin > XMax)
    {
        lfTmp = XMin;
        XMin = XMax;
        XMax = lfTmp;
    }
}

```

```

if (XMin == XMax) XMax = XMin == 0.0 ? 1.0 : XMin + fabs (XMin) / 10.0;

// Reduce to positive scale case if possible
if (XMax <= 0)
{
    iNegScl = 1;
    lfTmp   = XMin;
    XMin    = -XMax;
    XMax    = -lfTmp;
}
else
    iNegScl = 0;

if (N < 2) N = 2;
iNm1 = N - 1;

for (it = 0; it < 3; it++)
{
    // Compute initial and scaled steps
    lfIniStep = (XMax - XMin) / iNm1;
    lfSclStep = lfIniStep;

    for (; lfSclStep < 10.0; lfSclStep *= 10.0);
    for (; lfSclStep > 100.0; lfSclStep /= 10.0);

    // Find a suitable neat step
    for (i = 0; i < iNS && lfSclStep > Steps [i]; i++);
    lfSclFct = lfIniStep / lfSclStep;

    // Compute step and scale minimum value
    do
    {
        *Step = lfSclFct * Steps [i];
        *SMin = floor (XMin / *Step) * *Step;
        lfSMax = *SMin + iNm1 * *Step;
        if (XMax <= lfSMax) // Function maximum is in the
                           // range: the work is done.
        {
            if (iNegScl) *SMin = -lfSMax;
            *Step *= iNm1 / (N - 1);
            return 1;
        }
        i++;
    }
    while (i < iNS);

    // Double number of intervals
    iNm1 *= 2;
}

// Could not solve the problem
return 0;
}

```



The FrequenC Library	
<b>NAME:</b> CalcBias	<b>FUNCTION:</b> Calculate the B1 bias function for zero dead time and integer power law noise slope
<b>SYNOPSIS:</b> float CalcBias(int num, int mu)	
int num	The # of data points
int mu	Log-log slope, $\mu$ , of Allan variance, $\sigma_y^2(\tau)$ , for a power law noise process: <div style="text-align: right; margin-right: 20px;"> <u>Noise Type</u>      <u><math>\mu</math></u>  Flicker Walk FM      2  Random Walk FM      1  Flicker FM            0  White FM              -1  Flicker PM            -2  White PM              -2 </div>
<b>RETURN:</b> float	The value of the $B_1(N, r, \mu)$ bias function, the ratio of the standard variance to the Allan variance for zero dead time ( $r=1$ ) and integer $\mu$ power law $\sigma_y^2(\tau)$ noise process, or -1.0 if error.
<b>REMARKS:</b> The value of mu must be an integer between -2 and +2.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h" float b1; int num; int mu; . . num=(int) x[0]; mu=0; b1=CalcBias(num, mu); if(b1==-1.0) {     printf("\nError"); } else {     printf("\nB1 = %e", b1); } </pre> <div style="float: right; text-align: right;"> <pre> /* FrequenC header file */ /* value of B1 bias function */ /* # data points */ /* power law noise slope */  /* set num = # data points */ /* set mu for noise type */ /* calc B1 */ /* check for error */ /* error message */ /* display b1 */ </pre> </div>	
<b>SEE ALSO:</b> CalcBias1()	
<b>REFERENCE:</b> NIST Technical Note 1337	

## FrequenC Library Reference Manual

```

/*****
/*
/*          CalcBias()
/*
/*      Function to calculate bias function B1(N, r=1, æ), the ratio
/*      of the standard variance to the Allan variance for N samples,
/*      zero dead-time, and integer log sigma vs log tau slope æ.
/*
/*      Parameters:      int num      = # samples
/*                      int mu       = sigma-tau slope (-2 to +2)
/*
/*      Return:          float        = B1 bias function value,
/*                                or -1 if error
/*
/*      Revision Record:
/*          11/16/90      Created
/*          12/31/91      Renamed
/*          01/05/92      Changed error code to -1
/*                      Added error traps
/*          01/18/92      Edited title block
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1990-2003 Hamilton Technical Services All Rights Reserved */
*/
*****/

```

```
#include "frequenc.h"
```

```

float __declspec(dllexport) FAR PASCAL CalcBias(int num, int mu)
{
    float n=(float)num;
    float b;

    if(n<=1)
    {
        return(-1);
    }

    switch(mu)
    {
        case -2:
            {
                b=((n*n)-1)/((float)(1.5)*n*(n-1));
                break;
            }
        case -1:
            {
                b=1;
                break;
            }
        case 0:
            {
                b=(n*(float)log(n))/(2*(n-1)*(float)log(2));
                break;
            }
    }
}

```

```

case 1:                                     /* random walk FM */
{
    b=n/2;
    break;

}
case 2:                                     /* frequency drift or flicker walk FM */
{
    b=(n*(n+1))/6;
    break;
}
default:                                   /* unallowed mu */
{
    b=-1;                                  /* error code */
    break;
}
}                                           /* end switch */

return(b);

}                                           /* end CalcBias() */

```



The FrequenC Library															
<b>NAME:</b> CalcBias1	<b>FUNCTION:</b> Calculate the B1 bias function														
<b>SYNOPSIS:</b> float CalcBias1(int num, float r, float mu)															
int num	The # of data points														
float r	Dead time ratio; $r=T/\tau$														
float mu	Log-log slope, $\mu$ , of Allan variance, $\sigma_y^2(\tau)$ , for a power law noise process: <div style="text-align: right; margin-right: 20px;"> <table> <tr> <th>Noise Type</th><th><math>\mu</math></th></tr> <tr> <td>Flicker Walk FM</td><td>2</td></tr> <tr> <td>Random Walk FM</td><td>1</td></tr> <tr> <td>Flicker FM</td><td>0</td></tr> <tr> <td>White FM</td><td>-1</td></tr> <tr> <td>Flicker PM</td><td>-2</td></tr> <tr> <td>White PM</td><td>-2</td></tr> </table> </div>	Noise Type	$\mu$	Flicker Walk FM	2	Random Walk FM	1	Flicker FM	0	White FM	-1	Flicker PM	-2	White PM	-2
Noise Type	$\mu$														
Flicker Walk FM	2														
Random Walk FM	1														
Flicker FM	0														
White FM	-1														
Flicker PM	-2														
White PM	-2														
<b>RETURN:</b> float	The value of the $B_1(N, r, \mu)$ bias function, the ratio of the standard variance to the Allan variance for dead time ratio $r$ and power law $\sigma_y^2(\tau)$ noise exponent $\mu$ , or -1.0 if error.														
<b>REMARKS:</b> The value of mu must be between -2 and +2.															
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ float b1;   /* value of B1 bias function */ float r;   /* dead time ratio */ float mu;   /* power law noise exponent */ int num;   /* # data points */ . . num=(int) x[0];                                     /* set num = # data points */ r=1.1;   /* set r = dead time ratio */ mu=0.0;   /* set mu for noise type */ b1=CalcBias(num, r, mu);                           /* calc B1 */ if(b1==-1.0)                                       /* check for error */ {     printf("\nError");                             /* error message */ } else {     printf("\nB1 = %e", b1);                         /* display b1 */ } </pre>															
<b>SEE ALSO:</b> CalcBias()															
<b>REFERENCE:</b> NIST Technical Note 1337															

```

/*****
/*
/*                                     CalcBias1()
/*
/*      Function to calculate bias function B1(N, r, æ) = ratio of
/*      standard to Allan variance as a function of N = # samples, r =
/*      T/ç = dead time ratio and æ = power law noise exponent of åy(ç).
/*      r = 1 for no dead time. B1 = 1 for N = 2.
/*
/*
/*      References:      (1) NBS Technical Note 375, J.A. Barnes, "Tables
/*                        of Bias Functions B1 and B2, for Variances
/*                        Based on Finite Samples of Processes with
/*                        Power Law Spectral Densities", January, 1969.
/*                        (2) NIST Technical Note 1337, TN-296 to TN-335,
/*                        J.A. Barnes and D.W. Allan, "Variances Based
/*                        on Data with Dead Time Between the
/*                        Measurements".
/*                        (3) J.A. Barnes, "The Analysis of Time and
/*                        Frequency Data", Austron, Inc, December, 1991.
/*
/*      Note:            Faster direct solution CalcBias() function
/*                        available for r=1 zero dead time, int æ case.
/*
/*      Parameters:      int num = # samples (tested for 4 to 1024)
/*                        OK for 2 to INT_MAX, large # takes longer
/*                        float r = dead time ratio (tested for .001 to 8192)
/*                        Bounded to 1e-4 < r < 1e6 to avoid O/F
/*                        float mu= noise type (tested for -2 to +2)
/*                        Get -1 error code for mu < -2 or mu > 2
/*
/*      Return:          float    = B1 bias function value,
/*                        or -1 if error
/*
/*      Revision record:
/*      12/22/91   Drafted & debugged
/*      12/23/91   Added more bounds traps
/*      12/24/91   Added traps for special cases
/*      12/31/91   Renamed
/*      01/05/92   More error trapping
/*      01/16/92   Edited per FrequenC documentation
/*      01/18/92   Edited title block
/*      02/03/96   Modified for use as Win 3.1 DLL
/*      01/01/98   Changes for MS VC++ compatibility & warnings
/*      04/26/03   Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

float __declspec(dllexport) FAR PASCAL CalcBias1(int num, float r, float mu)
{
    double f;
    double p;
    double s;
    int i;

    /* term f */
    /* product term */
    /* summation term */
    /* summation index */

```

```

if(num<=1)                                /* NG if # samples < 2 */
{
    return(-1.0);                          /* error code */
}
r=(float)fabs(r);                          /* avoid negative ratio */

if((mu<-2) || (mu>2))                      /* avoid  $\mu < -2$  or  $\mu > 2$  */
{
    return(-1.0);                          /* error code */
}                                          /* end if */

if(num==2)                                /* check for special case */
{
    return(1.0);
}                                          /* end if */

if(mu==2)                                  /* check for special case */
{
    p=num;                                /* done in two steps to avoid int overflow */
    return(float)((p*(num+1))/6);
}                                          /* end if */

if((r==1) && (mu==1))                      /* check for special case */
{
    return(float)(num/2);
}                                          /* end if */

if((mu== -1) && (r>=1))                    /* check for special case */
{
    return(1.0);
}                                          /* end if */

if((mu== -2) && (r!=0) && (r!=1))          /* check for special case */
{
    return(1.0);
}                                          /* end if */

if((mu==0) || (mu== -2))                  /* check for  $\mu = 0$  or  $-2$  */
{
    mu+=(float)1e-6;                      /* to avoid singularity */
}                                          /* end if */

if(r<.0001)                               /* check for r near 0 */
{
    r=(float)1e-4;                        /* to avoid singularity */
}                                          /* end if */

if(r>1e6)                                 /* check for very large r */
{
    r=1e6;                                /* to avoid overflow */
}                                          /* end if */

p=num;                                    /* initialize p */
p*=(num-1);                               /* done in two steps to avoid int overflow */
s=0;                                      /* initialize sum to zero */

```

```
for(i=1; i<num; i++)                                /* do summation */
{
    f=2*pow(i*r, mu+2) - pow((i*r)+1, mu+2) - pow(fabs((i*r)-1), mu+2);
    s+=(f*(num-i))/p;
}                                                    /* end for */

f=2*pow(r, mu+2) - pow(r+1, mu+2) - pow(fabs(r-1), mu+2);

return(float)((1+s)/(1+(f/2)));

}                                                    /* end CalcBias1() */
```

The FrequenC Library	
<b>NAME:</b> CalcBias2	<b>FUNCTION:</b> Calculate the B2 bias function
<b>SYNOPSIS:</b> float CalcBias2(float r, float mu)	
float r	Dead time ratio; $r=T/\tau$
float mu	Log-log slope, $\mu$ , of Allan variance $\sigma_y^2(\tau)$ for a power law noise process: <div style="text-align: right; margin-right: 20px;"> <u>Noise Type</u>      <u><math>\mu</math></u>  Flicker Walk FM      2  Random Walk FM      1  Flicker FM            0  White FM              -1  Flicker PM            -2  White PM              -2 </div>
<b>RETURN:</b> float	The value of the $B_2(r, \mu)$ bias function, the ratio of the Allan variance with dead time to the Allan variance without dead time for dead time ratio $r$ and power law $\sigma_y^2(\tau)$ noise exponent $\mu$ , or -1.0 if error.
<b>REMARKS:</b> The value of mu must be between -2 and +2.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h" float b2; float r; float mu; . . r=1.1; mu=0.0; b2=CalcBias(r, mu); if(b2==-1.0) {     printf("\nError"); } else {     printf("\nB2 = %e", b2); } </pre> <div style="float: right; text-align: right;"> <pre> /* FrequenC header file */ /* value of B2 bias function */ /* dead time ratio */ /* power law noise exponent */  /* set r = dead time ratio */ /* set mu for noise type */ /* calc B2 */ /* check if error */ /* error message */ /* display b2 */ </pre> </div>	
<b>SEE ALSO:</b> CalcBias3()	
<b>REFERENCE:</b> NIST Technical Note 1337	

## FrequenC Library Reference Manual

```

/*****
/*
/*                               CalcBias2()                               */
/*
/*      Function to calculate the bias function B2(r, u) = ratio of
/*      Allan variance with dead time to Allan variance without dead time
/*      as a function of r and u, where r = T/tau = dead time ratio and
/*      u = power law noise exponent of sigma-tau.
/*      r = 1 for no dead time and B2(1, u) = 1.
/*
/*
/*      References:      (1) NBS Technical Note 375, J.A. Barnes, "Tables
/*                        of Bias Functions B1 and B2 ...", Jan. 1969.
/*                        (2) NIST Technical Note 1337, TN-296 to TN-335,
/*                        J.A Barnes and D.W. Allan, "Variances Based on
/*                        Data with Dead Time Between the Measurements".
/*                        (3) J.A. Barnes, "The Analysis of Time and
/*                        Frequency Data", Austron, Inc, December, 1991.
/*
/*      Parameters:      float r =   dead time ratio
/*                        Tested for.0001 to 4096)
/*                        Bounded to 1e-4 < r < 1e6 to avoid O/F
/*                        float mu=   noise type (mu = -2 to +2)
/*                        Get -1 error code for mu < -2 or mu > 2
/*
/*      Return:          float      = B2 bias function value,
/*                        or -1 if error
/*
/*      Revision record:
/*      09/21/02   Copied from CalcBias2() of FrequenC library
/*      09/22/02   Fixed error in F PM case
/*      03/08/03   Brought into Ver 2.0 of FrequenC lib
/*      04/26/03   Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003  Hamilton Technical Services  All Rights Reserved */
*/
*****/

```

```
#include "frequenc.h"
```

```

float __declspec(dllexport) FAR PASCAL CalcBias2(float r, float mu)
{
    double f;                               /* term f */
    double d;                               /* denominator term */

    r=(float)fabs(r);                        /* avoid negative ratio */

    if((mu<-2) || (mu>2))                    /* avoid æ<-2 or æ>2 */
    {
        return(-1.0);                       /* error code */
    }                                        /* end if */

    if(r==0)                                /* no need to calc for r=0 */
    {
        return(0.0);
    }                                        /* end if */

    if(r==1)                                /* no need to calc for r=1 */
    {
        return(1.0);
    }                                        /* end if */
}

```

```

if(mu==2)                                /* special case for æ=2 */
{
    return(r*r);
}                                           /* end if */

if((mu==1) && (r>=1))                    /* special case for æ=2 and r>=1 */
{
    return(((3*r)-1)/2);
}                                           /* end if */

if((mu==-1) && (r>=0))                    /* special case for æ=-1 and r>=0 */
{
    if(r<=1)
    {
        return(r);
    }                                           /* end if */
    else
    {
        return(1.0);
    }                                           /* end else */
}                                           /* end if */

if(mu==--2)                              /* special case for æ=-2 and r!=0 or 1 */
{
    return((float)(2.0/3.0));
}                                           /* end if */

if(mu==0)                                /* check for æ=0 */
{
    mu+=(float)1e-6;
}                                           /* to avoid singularity */
                                           /* end if */

if(r<.0001)                              /* check for r near 0 */
{
    r=(float)1e-4;
}                                           /* to avoid singularity */
                                           /* end if */

if(r>1e6)                                /* check for very large r */
{
    r=1e6;
}                                           /* to avoid overflow */
                                           /* end if */

f=2*pow(r, mu+2) - pow(r+1, mu+2) - pow(fabs(r-1), mu+2);
d=2*(1-pow(2, mu));

return(float)((1+(f/2))/d);

}                                           /* end CalcBias2() */

```



The FrequenC Library															
<b>NAME:</b> CalcBias3	<b>FUNCTION:</b> Calculate the B3 bias function														
<b>SYNOPSIS:</b> float CalcBias3(int m, float r, float mu)															
int m	The # of averages														
float r	Dead time ratio; $r=T/\tau$														
float mu	Log-log slope, $\mu$ , of Allan variance, $\sigma_y^2(\tau)$ for a power law noise process: <div style="text-align: right; margin-right: 20px;"> <table> <tr> <th>Noise Type</th><th><math>\mu</math></th></tr> <tr> <td>Flicker Walk FM</td><td>2</td></tr> <tr> <td>Random Walk FM</td><td>1</td></tr> <tr> <td>Flicker FM</td><td>0</td></tr> <tr> <td>White FM</td><td>-1</td></tr> <tr> <td>Flicker PM</td><td>-2</td></tr> <tr> <td>White PM</td><td>-2</td></tr> </table> </div>	Noise Type	$\mu$	Flicker Walk FM	2	Random Walk FM	1	Flicker FM	0	White FM	-1	Flicker PM	-2	White PM	-2
Noise Type	$\mu$														
Flicker Walk FM	2														
Random Walk FM	1														
Flicker FM	0														
White FM	-1														
Flicker PM	-2														
White PM	-2														
<b>RETURN:</b> float	The value of the $B_3(m, r, \mu)$ bias function, the ratio of the Allan variance with distributed dead times to the Allan variance with all dead time at end as a function of # averages m, dead time ratio r and power law $\sigma_y^2(\tau)$ noise exponent $\mu$ , or -1.0 if error.														
<b>REMARKS:</b> The value of mu must be between -2 and +2.															
<b>EXAMPLE:</b> <pre> #include "frequenc.h" float b3; float r; float mu; int m; . . m=2; r=1.1; mu=0.0; b3=CalcBias(m, r, mu); if(b3==-1.0) {     printf("\nError"); } else {     printf("\nB3 = %e", b3); } </pre> <div style="text-align: right; margin-right: 20px;"> <pre> /* FrequenC header file */ /* value of B3 bias function */ /* dead time ratio */ /* power law noise exponent */ /* # averages */  /* set m = # averages */ /* set r = dead time ratio */ /* set mu for noise type */ /* calc B3 */ /* check for error */  /* error message */  /* display b3 */ </pre> </div>															
<b>SEE ALSO:</b> CalcBias2()															
<b>REFERENCE:</b> NIST Technical Note 1337															

## FrequenC Library Reference Manual

```

/*****
/*
/*                               CalcBias3()                               */
/*
/*  Function to calculate bias function B3(2, M, r, u) = ratio of          */
/*  Allan variance with distributed dead times to Allan variance          */
/*  with all dead time at end as a function of M=# averages,            */
/*  r=T/tau=dead time ratio and u=power law noise exponent of sigma-tau. */
/*  r=1 for no dead time.  B1=1 for N=2.                                  */
/*  Use product of B2 and B3 for averaged data with dead time.          */
/*
/*  References:  (1) NBS Technical Note 375, J.A. Barnes, "Tables         */
/*               of Bias Functions B1 and B2 ...", Jan. 1969.             */
/*               (2) NIST Technical Note 1337, TN-296 to TN-335,         */
/*               J.A. Barnes and D.W. Allan, "Variances Based            */
/*               on Data with Dead Time Between the                      */
/*               Measurements".                                           */
/*               (3) J.A. Barnes, "The Analysis of Time and              */
/*               Frequency Data", Austron, Inc, Dec. 1991.               */
/*
/*  Parameters:  int m    = # averages (tested for 1 to 1024)           */
/*               OK for 1 to INT_MAX, large n takes longer              */
/*               float r = dead time ratio (tested for .01 to 8192)      */
/*               Bounded to 1e-4 < r < 1e6 to avoid O/F                 */
/*               float mu= noise type (tested for -2 to +2)              */
/*               Get -1 error code for mu < -2 or mu > 2                  */
/*
/*  Return:      float    = B3 bias function value,                     */
/*               or -1 if error                                          */
/*
/*  Revision record:                                                     */
/*      09/21/02   Copied from CalcBias2() of FrequenC library          */
/*      03/08/03   Brought into Ver 2.0 of FrequenC lib                */
/*      04/26/03   Adapted for Version 2.0 source code documentation   */
/*
/*  (c) Copyright 1991-2003  Hamilton Technical Services  All Rights Reserved */
/*
*****/

```

```
#include "frequenc.h"
```

```

float __declspec(dllexport) FAR PASCAL CalcBias3(int m, float r, float mu)
{
    double f;                               /* term f */
    double s;                               /* summation term */
    int i;                                  /* summation index */

    if(m==0)
    {
        return(-1.0);                      /* error code */
    }
    m=abs(m);                             /* avoid negative # points */
    r=(float)fabs(r);                      /* avoid negative ratio */

    if((mu<-2) || (mu>2))                  /* avoid æ<-2 or æ>2 */
    {
        return(-1.0);                      /* error code */
    }
    /* end if */
}

```

```

if((r==1)|| (m==1)|| (mu==2))      /* no need to calc if r=1 or m=1 or mu=2 */

{
    return(1.0);
}                                     /* end if */

if(mu== -2)                         /* no need to calc if mu=-2 */
{
    return(float) (m);
}                                     /* end if */

if(mu==0)                           /* check for æ=0 */
{
    mu+=(float)1e-6;                 /* to avoid singularity */
}                                     /* end if */

if(r<.0001)                         /* check for r near 0 */
{
    r=(float)1e-4;                   /* to avoid singularity */
}                                     /* end if */

if(r>1e6)                           /* check for very large r */
{
    r=1e6;                           /* to avoid overflow */
}                                     /* end if */

s=0;                                 /* initialize sum to zero */

for(i=1; i<m; i++)                  /* do summation */
{
    f=2*pow(i*r, mu+2) - pow((i*r)+1, mu+2) - pow(fabs((i*r)-1), mu+2);
    f*=2;
    f-=2*pow((m+i)*r, mu+2) - pow(((m+i)*r)+1, mu+2)
        - pow(fabs(((m+i)*r)-1), mu+2);
    f-=2*pow((m-i)*r, mu+2) - pow(((m-i)*r)+1, mu+2)
        - pow(fabs(((m-i)*r)-1), mu+2);
    f*=(m-i);
    s-=f;
}                                     /* end for */

s+=m*(2*pow(m*r, mu+2) - pow((m*r)+1, mu+2) - pow(fabs((m*r)-1), mu+2));
s+=2*m;
f=2*pow(r, mu+2) - pow(r+1, mu+2) - pow(fabs(r-1), mu+2);
f+=2;

return(float) (s/(f*pow(m, mu+2)));
}                                     /* end CalcBias3() */

```



The FrequenC Library	
<b>NAME:</b> CalcBisectionDrift	<b>FUNCTION:</b> Calc freq drift using the average freq over the first and last halves of the data points
<b>SYNOPSIS:</b> float CalcBisectionDrift(F_TYPE y[])	
F_TYPE y[]	Frequency data array y[0] = # data points y[1] = analysis start point y[2] = analysis end point
<b>RETURN:</b> float	Drift per unity data interval
<b>REMARKS:</b> Only data points between start and end analysis limits are modified. All zeros are treated as gaps in frequency data. This is the best estimator of drift for the combination of white and random walk FM noise (see reference. Tau=1 is assumed. Drift is per tau interval. This function calls FrequenC function CalcMean()).	
<b>EXAMPLE:</b> <pre>#include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* data array */ float drift;   /* drift */ . . drift=CalcBisectionDrift(y);                          /* call function */ printf("\nDrift = %e", drift);                      /* display result */</pre>	
<b>SEE ALSO:</b> CalcMean()	
<b>REFERENCE:</b> M. Weiss, D. Allan, and D. Howe, "Confidence on the Second Difference Estimation of Frequency Drift", 1992 IEEE Frequency Control Symposium, pp.300-305, June, 1992.	

```

/*****
/*
/*          CalcBisectionDrift()
/*
/*      Function to calculate frequency drift using the average frequency
/*      over the first and last halves of the data points.
/*
/*      Parameters:      y[]      frequency data array
/*
/*      Return:          float    frequency drift
/*
/*      Notes:   This is the best estimator of drift for the combination
/*               of white and random walk FM noise (see reference).
/*               Tau=1 is assumed.   Drift is per tau interval.
/*               This function calls FrequenC function CalcMean().
/*
/*      Reference:
/*      M. Weiss, D. Allan, and D. Howe, "Confidence on the Second Diff-
/*      erence Estimation of Frequency Drift", 1992 IEEE Frequency Control
/*      Symposium, pp.300-305, June, 1992.
/*
/*      Revision record:
/*      11/01/92      Created
/*      02/03/96      Modified for use as Win 3.1 DLL
/*      01/01/98      Changes for MS VC++ compatibility & warnings
/*      04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1992-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

#include "frequenc.h"                                /* FrequenC header file */

float __declspec(dllexport) FAR PASCAL CalcBisectionDrift(F_TYPE y[])
{
    F_TYPE start, end, mid;          /* original analysis limits & midpoint */
    F_TYPE a1, a2;                  /* frequency averages */
    float d;                        /* frequency drift */

    /* save original analysis limits */
    start=y[1];
    end=y[2];

    /* find midpoint of analysis data */
    mid = ((y[2]-y[1])+1)/2;          /* not necessarily an integer */

    /* calc avg freq over 1st half */
    y[1]=1;
    y[2]=floor(mid);                 /* rounded down to the next smaller integer */
    CalcMean(y, &a1, FREQ);          /* calc avg freq over 1st half */

    /* calc avg freq over 2nd half */
    y[1]=y[2]+1;
    y[2]=end;
    CalcMean(y, &a2, FREQ);

    /* calc drift */
    d=(float)((a2-a1)/(mid));

```

```
/* restore analysis limit */
y[1]=start;

return(d);
}                                     /* frequency drift */
                                     /* end CalcBisectionDrift() */
```



The FrequenC Library	
<b>NAME:</b> CalcChiSqrProb	<b>FUNCTION:</b> Calculate the chi-square probability function
<b>SYNOPSIS:</b> float CalcChiSqrProb(float x, float df)	
float x	The chi-square value
float df	The # of chi square degrees of freedom
<b>RETURN:</b> float	The value of the chi-square probability, the area under the chi-square curve for the chi-square value x and the # of degrees of freedom df, or -1.0 if error.
<b>REMARKS:</b> None	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ float p;  /* value of chi-square probability */ float x;  /* chi-square value */ float df;   /* # degrees of freedom */ . . x=3.94;  /* set r = dead time ratio */ df=10;  /* set mu for noise type */ p=CalcChiSqrProb(r, mu);                            /* calc X<sup>2</sup> prob */ if(p== -1.0)   /* check for error */ {     printf("\nError");                               /* error message */ } else {     printf("\np(X<sup>2</sup>,df) = %e", p);                    /* display p */ } </pre>	
<b>SEE ALSO:</b> CalcInvChiSqr()	
<b>REFERENCE:</b> Collected Algorithms from CACM, Vol. I, # 299	

## FrequenC Library Reference Manual

```

/*****
/*
/*          CalcChiSqrProb()
/*
/*      Function to calculate the chi-square probability, the area under
/*      the chi-square distribution.
/*
/*      Reference:      Collected Algorithms from CACM, Vol. I, #299,
/*                      I.D. Hill and M.C. Pike, 1965.
/*
/*      Parameters:      float x = chi-square value
/*                      float df = # of degrees of freedom
/*
/*      Return:          float      = chi-square probability value,
/*                      or -1 if error
/*
/*      Revision record:
/*          12/30/91      Created
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

float __declspec(dllexport) FAR PASCAL CalcChiSqrProb(float x, float df)
{
    int f;
    BOOL even;
    BOOL bigx=FALSE;
    float chiprob;
    double a, c, e, y, z, s;

    if(x > 1416)          /* avoid O/F of exp(-0.5*x) < DBL_MIN ÷ 2.225e-308 */
    {
        bigx=TRUE;
    }
    /* end if */

    f = (int) df;
    if (x < 0.0 || f < 1.0)
    {
        return (-1.0);
    }
    /* error code */
    /* end if */

    a = .5 * x;
    even = (f % 2);
    even = !even;
    if (even || f > 2 && ! bigx)
    {
        y = exp(-a);
    }
    /* end if */

    if (even)
    {
        s = y;
    }
    /* end if */
}

```

```

else
{
    s = 2.0 * CalcNormalProb((float)-sqrt(x));
}
/* end else */
if (f > 2)
{
    x = (float)(0.5 * (df - 1.0));
    if (even)
    {
        z = 1.0;
    }
    /* end if */
    else
    {
        z = .5;
    }
    /* end else */
    if (bigx)
    {
        e = (even) ? 0.0 : .572364942925;
        c = log(a);
        for ( ; z <= x; z += 1.0)
        {
            e = log(z) + e;
            s = exp(c * z - a - e) + s;
        }
        /* end for */
        chiprob = (float)s;
    }
    /* end if */
    else
    {
        e = (even) ? 1.0 : .564189583548 / sqrt(a);
        c = 0.0;
        for ( ; z <= x; z += 1.0)
        {
            e = e * a / z;
            c += e;
        }
        /* end for */
        /* end else */
        chiprob = (float)(c * y + s);
    }
    /* end if */
}
else
{
    chiprob = (float)s;
}
/* end else */

return (chiprob);
/* end CalcChiSqrProb() */
}

```



The FrequenC Library	
<b>NAME:</b> ConvDomain	<b>FUNCTION:</b> Perform time-frequency domain conversions
<b>SYNOPSIS:</b> int ConvDomain(float h, float *z, float tau, float f, float v, float fh, int type, int alpha, int n)	
float h	Noise parameter, $h(\alpha)$
float *z	Pointer to output parameter: 1= $S_y(f)$ , 1/Hz, 2= $S_x(f)$ , $\text{sec}^2/\text{Hz}$ , 3= $S_\phi(f)$ , $\text{rad}^2/\text{Hz}$ , 4= $\ell(f)$ , dBc/Hz, 5= $\sigma_y(\tau)$ , 6=Mod $\sigma_y(\tau)$ , 7= $\sigma_x(\tau)$ , sec
float tau	Averaging time $\tau$ , sec
float f	Fourier frequency f, Hz
float v	Carrier frequency, Hz
float fh	System high frequency cut off, Hz
int type	Input parameter type: 1= $S_y(f)$ , 2= $S_x(f)$ , 3= $S_\phi(f)$ , 4= $\ell(f)$ , 5= $\sigma_y(\tau)$ , 6=Mod $\sigma_y(\tau)$ , 7= $\sigma_x(\tau)$
int alpha	Power law noise type, $\alpha$
int n	# samples averaged; sampling time= $\tau_0=\tau/n$
<b>RETURN:</b> int	Status: +1=OK, -1=Error
<b>REMARKS:</b> This function converts the noise parameter $h(\alpha)$ to an output parameter determined by type. Depending on the conversion desired, the parameters t, f, v, fh, alpha and n are used. Use the function CalcDomain() for the inverse conversion from one of the time or frequency noise parameters to $h(\alpha)$ . A general domain conversion is performed by using both functions. Calls FrequenC Library function CalcRatio(). Original z unchanged if bad parameter (error).	
<b>EXAMPLE:</b> <pre> #include "frequenc.h" float h, tau, f, v, fh, type; float z; int alpha, n; int status;  /* set parameters */  ConvDomain(h, &amp;z, tau, f, fh, type, alpha, n); printf("\nv = %e", v); </pre> <div style="float: right; text-align: right;"> <pre> /* FrequenC header file */ /* input parameters */ /* output parameter */ /* input parameters */ /* return code */  /* call function */ /* display result */ </pre> </div>	
<b>SEE ALSO:</b> CalcDomain()	
<b>REFERENCE:</b> NIST Technical Note 1337	

## FrequenC Library Reference Manual

```

/*****
/*
/*          ConvDomain()
/*
/*          Function to do time-frequency domain conversions
/*
/*          Parameters:      float h      = Noise parameter h(à)
/*                          float *p_z  = Pointer to output parameter z:
/*                                = Sy(f), 1/Hz      if type=1
/*                                = Sx(f), sec2/Hz if type=2
/*                                = Si(f), rad2/Hz if type=3
/*                                = æ(f), dBc/Hz    if type=4
/*                                = åy(ç)          if type=5
/*                                = Mod åy(ç)       if type=6
/*                                = åx(ç), sec      if type=7
/*                          float tau    = Averaging time ç, sec
/*                          float f      = Fourier frequency f, Hz
/*                          float v      = Carrier frequency, Hz
/*                          float fh     = System high frequency cut off, Hz
/*                          int type     = Input parameter type:
/*                                1=Sy(f), 2=Sx(f), 3=Si(f), 4=æ(f)
/*                                5=åy(ç), 6=Mod åy(ç), 7=åx(ç)
/*                          int alpha    = Power law noise type, à
/*                                = Log=log slope of Sy(f)=h(à)fà
/*                                White PM à=+2, Flicker PM à=+1
/*                                White FM à= 0, Flicker FM à=-1
/*                                Random Walk FM à=-2
/*                          int n        = # samples averaged
/*                                sampling time = tau_0 = tau/n
/*
/*          Return:         int          = Status: +1=OK, -1=Error
/*
/*          Notes:          This function converts the noise parameter h(à)
/*                          to an output parameter determined by type.
/*                          Depending on the conversion desired, the
/*                          parameters t, f, v, fh, alpha and n are used.
/*                          Use the function CalcDomain() for the inverse
/*                          conversion from one of the time or frequency
/*                          noise parameters to h(à). A general domain
/*                          conversion is performed by using both functions.
/*                          Calls FrequenC Library function CalcRatio().
/*                          Original z unchanged if bad parameter (error).
/*
/*          Revision record:
/*          01/25/92      Adapted from conversion() of DOMAIN_F.C
/*          01/26/92      Changed type #s to agree with CalcDomain()
/*                          Fixed errors in Sp & L calculations
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1992-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"                                /* FrequenC Library header file */
```

```

int __declspec(dllexport) FAR PASCAL ConvDomain(float h, float *p_z,
float tau, float f, float v, float fh, int type, int alpha, int n)
{
    double pi;

```

```
/* ã */
```

```

double a;
double b;
double c;
double d;
double e;
double Sx;
double Sp;
double L;
double Sy;
double sy;
double sx;
double mod_sy;

/* Sx(f) */
/* Sí(f) */
/* œ(f) */
/* Sy(f) */
/* ây(ç) */
/* âx(ç) */
/* Mod ây(ç) */

/* check parameters */

if( (h==0) || (tau<=0) || (f<=0) || (v<=0) || (fh<=0) ||
    (type<1) || (type>7) || (alpha<-2) || (alpha>2) || (n<1) )
{
    return(-1);
}

/* initialize constants */

pi=4*atan(1);
a=4*pi*pi/6;
b=2*log(2);
c=0.5;
d=(1.038+(3*log(2*pi*f*tau)))/(4*pi*pi);
e=(3*f*tau)/(4*pi*pi);

/* perform basic frequency domain conversion */

Sy=h*pow(f, alpha);

/* perform basic time domain conversion */

switch(alpha)
{
    case 2: /* W í */
    {
        sy=sqrt(e*Sy/(f*f*tau*tau));
        break;
    }
    case 1: /* F í */
    {
        sy=sqrt(d*Sy/(f*tau*tau));
        break;
    }
    case 0: /* W f */
    {
        sy=sqrt(c*Sy/tau);
        break;
    }
    case -1: /* F f */
    {
        sy=sqrt(b*f*Sy);
        break;
    }
}

```

```

case -2:      /* RW f */
{
    sy=sqrt(a*f*f*Sy*tau);

    break;
}
default:
{
    return(-1);                                /* error */
}
}                                                  /* end switch */

/* complete specific conversion */

switch(type)
{
    case 1:    /* Sy(f) */
    {
        *p_z=Sy;
        break;
    }
    case 2:    /* Sx(f) */
    {
        Sx=Sy/(4*pi*pi*f*f);
        *p_z=Sx;
        break;
    }
    case 3:    /* S1(f) */
    {
        Sp=Sy*v*v/(f*f);
        *p_z=Sp;
        break;
    }
    case 4:    /* α(f) */
    {
        Sp=Sy*v*v/(f*f);
        L=10*log10(Sp/2);
        *p_z=L;
        break;
    }
    case 5:    /* sy(ζ) */
    {
        *p_z=sy;
        break;
    }
    case 6:    /* Mod sy(ζ) */
    {
        if( (tau/n)<1 )
        {
            return(-1);
        }
        mod_sy=sqrt(sy*sy*CalcRatio(alpha, n, 2*pi*f*tau/n));
        *p_z=mod_sy;
        break;
    }
}

```

```

case 7:    /* sx(ç) */
{
    if( (tau/n)<1 )
    {
        return(-1);
    }
    mod_sy=sqrt(sy*sy*CalcRatio(alpha, n, 2*pi*fh*tau/n));
    sx=tau*mod_sy/sqrt(3);
    *p_z=sx;

    break;
}
default:
{
    return(-1);                                /* error */
}
/* end switch */
return(1);
/* end ConvDomain() */
}

```



The FrequenC Library	
<b>NAME:</b> CalcDomain	<b>FUNCTION:</b> Calc time-frequency domain noise parameters
<b>SYNOPSIS:</b> int CalcDomain(float *h, float z, float tau, float tau, float v, float fh, int type, int alpha, int n)	
float *h	Pointer to noise parameter output, $h(\alpha)$
float z	Input parameter: 1= $S_y(f)$ , 1/Hz, 2= $S_x(f)$ , $\text{sec}^2/\text{Hz}$ , 3= $S_\phi(f)$ , $\text{rad}^2/\text{Hz}$ , 4= $\mathcal{L}(f)$ , dBc/Hz, 5= $\sigma_y(\tau)$ , 6=Mod $\sigma_y(\tau)$ , 7= $\sigma_x(\tau)$ , sec
float tau	Averaging time $\tau$ , sec
float v	Carrier frequency, Hz
float fh	System high frequency cut off, Hz
int type	Input parameter type: 1= $S_y(f)$ , 2= $S_x(f)$ , 3= $S_\phi(f)$ , 4= $\mathcal{L}(f)$ , 5= $\sigma_y(\tau)$ , 6=Mod $\sigma_y(\tau)$ , 7= $\sigma_x(\tau)$
int alpha	Power law noise type, $\alpha$
int n	# samples averaged; sampling time= $\tau_0=\tau/n$
<b>RETURN:</b> int	Status: +1=OK, -1=Error
<b>REMARKS:</b> This function calculates the power law noise parameter $h(\alpha)$ for an input parameter type. Depending on the conversion desired, the parameters t, f, v, fh, alpha and n are used. Use the function ConvDomain() for the inverse conversion from $h(\alpha)$ to one of the time or frequency noise parameters. A general domain conversion is performed by using both functions. Calls FrequenC Library function CalcRatio(). Original h unchanged if bad parameter (error).	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ float z, tau, f, v, fh, type;                        /* input parameters */ float h;  /* output parameter */ int alpha, n;                                       /* input parameters */ int status;   /* return code */  /* set parameters */  CalcDomain(&amp;h, z, tau, v, fh, type, alpha, n);        /* call function */ printf("\nh = %e", h);                             /* display result */ </pre>	
<b>SEE ALSO:</b> ConvDomain()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*          CalcDomain()
/*
/*      Function to calc time-frequency domain noise parameters
/*
/*      Parameters:      float *p_h = Pointer to noise parameter h(à)
/*                      float z   = input parameter:
/*                          = Sy(f), 1/Hz      if type=1
/*                          = Sx(f), sec2/Hz if type=2
/*                          = Si(f), rad2/Hz if type=3
/*                          = æ(f), dBc/Hz    if type=4
/*                          = åy(ç)          if type=5
/*                          = Mod åy(ç)      if type=6
/*                          = åx(ç), sec      if type=7
/*                      float tau  = Averaging time ç, sec
/*                      float f    = Fourier frequency f, Hz
/*                      float v    = Carrier frequency, Hz
/*                      float fh   = System high frequency cut off, Hz
/*                      int type   = Input parameter type:
/*                                  1=Sy(f), 2=Sx(f), 3=Si(f), 4=æ(f)
/*                                  5=åy(ç), 6=Mod åy(ç), 7=åx(ç)
/*                      int alpha  = Power law noise type, à
/*                                  = Log=log slope of Sy(f)=h(à)fà
/*                                  White PM à=+2, Flicker PM à=+1
/*                                  White FM à= 0, Flicker FM à=-1
/*                                  Random Walk FM à=-2
/*                      int n      = # samples averaged
/*                                  sampling time = tau_0 = tau/n
/*
/*      Return:          int        = Status: +1=OK, -1=Error
/*
/*      Notes:           This function calculates the power law noise
/*                        parameter h(à) for an input parameter type.
/*                        Depending on the conversion desired, the
/*                        parameters t, f, v, fh, alpha and n are used.
/*                        Use the function ConvDomain() for the inverse
/*                        conversion from h(à) to one of the time or
/*                        frequency noise parameters . A general domain
/*                        conversion is performed by using both functions.
/*                        Calls FrequenC Library function CalcRatio().
/*                        Original h unchanged if bad parameter (error).
/*
/*      Revision record:
/*          01/25/92      Adapted from table_calc() of DOMAIN_C.C
/*          01/26/92      Changed title block type #s
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1992-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

#include "frequenc.h"                                /* FrequenC Library header file */

int __declspec(dllexport) FAR PASCAL CalcDomain(float *p_h, float z,
float tau, float f, float v, float fh, int type, int alpha, int n)
{
    double pi;
    double a;

```

```

double b;
double c;
double d;
int index;                                     /* case index */

/* check parameters */

if( (z==0) || (tau<=0) || (f<=0) || (v<=0) || (fh<=0) ||
    (type<1) || (type>7) || (alpha<-2) || (alpha>2) || (n<1) )
{
    return(-1);
}

/* initialize constants */

pi=4*atan(1);
a=4*pi*pi;
b=2*log(2);
c=2*pi*f*tau;
d=1.038+(3*log(c));

index=((alpha+2)*7)+type;

/* process noise data entry */

switch(index)
{
    case 1: /* Sy(f) for RW f à=-2 */
        {
            *p_h=z*f*f;
            break;
        }
    case 2: /* Sx(f) for RW f à=-2 */
        {
            *p_h=a*z*f*f*f*f;
            break;
        }
    case 3: /* Sí(f) for RW f à=-2 */
        {
            *p_h=z*f*f*f*f/(v*v);
            break;
        }
    case 4: /* œ(f) for RW f à=-2 */
        {
            *p_h=2*pow(10, (z/10))/(v*v);
            *p_h*=f*f*f*f;
            break;
        }
    case 5: /* åy(ç) for RW f à=-2 */
        {
            *p_h=6*z*z/(a*tau);
            break;
        }
    case 6: /* Mod åy(ç) for RW f à=-2 */
        {
            *p_h=6*z*z;
            *p_h/=CalcRatio(2, n, c/n);
            *p_h/=a*tau;
            break;
        }
}

```

```

case 7:      /*  $\alpha_x(\zeta)$  for RW f à=-2 */
            {
                *p_h=3*6*z*z;
                *p_h/=CalcRatio(2, n, c/n);
                *p_h/=a*tau*tau*tau;
                break;
            }
case 8:      /*  $S_y(f)$  for F f à=-1 */
            {
                *p_h=z*f;
                break;
            }
case 9:      /*  $S_x(f)$  for F f à=-1 */
            {
                *p_h=a*f*f*f*z;
                break;
            }
case 10:     /*  $S_i(f)$  for F f à=-1 */
            {
                *p_h=f*f*f*z/(v*v);
                break;
            }
case 11:     /*  $\alpha(f)$  for F f à=-1 */
            {
                *p_h=2*pow(10, (z/10))/(v*v);
                *p_h*=f*f*f;
                break;
            }
case 12:     /*  $\alpha_y(\zeta)$  for F f à=-1 */
            {
                *p_h=z*z/(b);
                break;
            }
case 13:     /* Mod  $\alpha_y(\zeta)$  for F f à=-1 */
            {
                *p_h=z*z;
                *p_h/=b;
                *p_h/=CalcRatio(1, n, c/n);
                break;
            }
case 14:     /*  $\alpha_x(\zeta)$  for F f à=-1 */
            {
                *p_h=3*z*z/(b);
                *p_h/=CalcRatio(1, n, c/n);
                *p_h/=tau*tau;
                break;
            }
case 15:     /*  $S_y(f)$  for W f à=0 */
            {
                *p_h=z;
                break;
            }
case 16:     /*  $S_x(f)$  for W f à=0 */
            {
                *p_h=a*f*f*z;
                break;
            }

```

```

case 17: /*  $S_1(f)$  for  $W f \rightarrow 0$  */
        {
            *p_h=f*f*z/(v*v);
            break;
        }
case 18: /*  $\alpha(f)$  for  $W f \rightarrow 0$  */
        {
            *p_h=f*f*2*pow(10,(z/10))/(v*v);
            break;
        }
case 19: /*  $\Delta y(\zeta)$  for  $W f \rightarrow 0$  */
        {
            *p_h=2*z*z*tau;
            break;
        }
case 20: /* Mod  $\Delta y(\zeta)$  for  $W f \rightarrow 0$  */
        {
            *p_h=2*z*z*tau;
            *p_h/=CalcRatio(0, n, c/n);
            break;
        }
case 21: /*  $\Delta x(\zeta)$  for  $W f \rightarrow 0$  */
        {
            *p_h=3*2*z*z*tau;
            *p_h/=CalcRatio(0, n, c/n);
            *p_h/=tau*tau;
            break;
        }
case 22: /*  $S_y(f)$  for  $F i \rightarrow 1$  */
        {
            *p_h=z/f;
            break;
        }
case 23: /*  $S_x(f)$  for  $F i \rightarrow 1$  */
        {
            *p_h=a*f*z;
            break;
        }
case 24: /*  $S_1(f)$  for  $F i \rightarrow 1$  */
        {
            *p_h=f*z/(v*v);
            break;
        }
case 25: /*  $\alpha(f)$  for  $F i \rightarrow 1$  */
        {
            *p_h=f*2*pow(10,(z/10));
            *p_h/=v*v;
            break;
        }
case 26 : /*  $\Delta y(\zeta)$  for  $F i \rightarrow 1$  */
        {
            *p_h=a*z*z*tau*tau;
            *p_h/=(d);
            break;
        }
    }

```

```

case 27: /* Mod  $\alpha_y(\zeta)$  for  $F \in \mathbb{A}^1$  */
{
    *p_h=a*z*z;
    *p_h/=CalcRatio(-1, n, c/n);
    *p_h*=tau*tau;
    *p_h/=(d);
    break;
}
case 28: /*  $\alpha_x(\zeta)$  for  $F \in \mathbb{A}^1$  */
{
    *p_h=3*a*z*z*tau*tau;
    *p_h/=CalcRatio(-1, n, c/n);
    *p_h/=tau*tau;
    *p_h/=(d);
    break;
}
case 29: /*  $S_y(f)$  for  $W \in \mathbb{A}^2$  */
{
    *p_h=z/(f*f);
    break;
}
case 30: /*  $S_x(f)$  for  $W \in \mathbb{A}^2$  */
{
    *p_h=a*z;
    break;
}
case 31: /*  $S_1(f)$  for  $W \in \mathbb{A}^2$  */
{
    *p_h=z/(v*v);
    break;
}
case 32: /*  $\alpha(f)$  for  $W \in \mathbb{A}^2$  */
{
    *p_h=2*pow(10, (z/10));
    *p_h/=v*v;
    break;
}
case 33: /*  $\alpha_y(\zeta)$  for  $W \in \mathbb{A}^2$  */
{
    *p_h=a*z*z;
    *p_h*=tau*tau/(3*f_h);
    break;
}
case 34: /* Mod  $\alpha_y(\zeta)$  for  $W \in \mathbb{A}^2$  */
{
    *p_h=a*z*z;
    *p_h*=tau*tau;
    *p_h/=CalcRatio(-2, n, c/n);
    *p_h/=3*f_h;
    break;
}
case 35: /*  $\alpha_x(\zeta)$  for  $W \in \mathbb{A}^2$  */
{
    *p_h=3*a*z*z;
    *p_h*=tau*tau;
    *p_h/=CalcRatio(-2, n, c/n);
    *p_h/=3*tau*tau*f_h;
    break;
}

```

```
        default:    break;
    }
    return(1);
}
/* end switch */
/* end CalcDomain() */
```



The FrequenC Library															
<b>NAME:</b> CalcDegFree	<b>FUNCTION:</b> Calculate the # of degrees of freedom for a set of phase or frequency data														
<b>SYNOPSIS:</b> float CalcDegFree(int alpha, int num, int m)															
int alpha	<p>The log-log slope, <math>\alpha</math>, of <math>S_y(f)</math> for a power law noise process:</p> <table> <tr> <th>Noise Type</th><th><math>\alpha</math></th></tr> <tr> <td>Flicker Walk FM</td><td>-3</td></tr> <tr> <td>Random Walk FM</td><td>-2</td></tr> <tr> <td>Flicker FM</td><td>-1</td></tr> <tr> <td>White FM</td><td>0</td></tr> <tr> <td>Flicker PM</td><td>1</td></tr> <tr> <td>White PM</td><td>2</td></tr> </table>	Noise Type	$\alpha$	Flicker Walk FM	-3	Random Walk FM	-2	Flicker FM	-1	White FM	0	Flicker PM	1	White PM	2
Noise Type	$\alpha$														
Flicker Walk FM	-3														
Random Walk FM	-2														
Flicker FM	-1														
White FM	0														
Flicker PM	1														
White PM	2														
int num	The # of phase data points = # frequency data points + 1														
int m	Averaging factor														
<b>RETURN:</b> float	The # of chi-squared degrees of freedom for num fully-overlapping phase data points with an averaging factor of m, or -1.0 if error.														
<b>REMARKS:</b> None															
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[513];                                       /* phase data array */ float df;   /* # of degrees of freedom */ int num;   /* # phase data points */ int m;   /* averaging factor */ int alpha;   /* noise exponent alpha */ . . m=2;   /* set m = # averages */ num=(int)x[0];                                       /* set # data points */ alpha=0;   /* set noise type alpha */ df=CalcDegFree(alpha, num, m);                     /* calc df */ if(df==-1.0)                                       /* check for error */ {     printf("\nError");                             /* error message */ } else {     printf("\ndf = %e", df);                         /* display df */ } </pre>															
<b>SEE ALSO:</b> None															
<b>REFERENCE:</b> NIST Technical Note 1337															

## FrequenC Library Reference Manual

```

/*****
/*
/*          CalcDegFree()
/*
/*      Function to calculate the # of chi-square degrees of freedom
/*      for phase or frequency data.
/*
/*      Reference:      NIST Technical Note 1337, p.TN-85, Table 12-4
/*                      (as corrected).
/*
/*      Parameters:    int alpha = power-law exponent of Sy(f) noise type
/*                    int n      = # phase data points
/*                    int m      = # frequency data points + 1
/*                    int m      = fully-overlapping averaging factor
/*
/*      Return:        float      = # chi-square degrees of freedom,
/*                                or -1 if error
/*
/*      Revision record:
/*          12/30/91    Created
/*          12/31/91    Renamed
/*          01/04/92    Changed switch from (2-a) to a
/*                      Added default case for NG alpha
/*                      Changed n and m parameters to ints
/*                      Do calcs with double versions dn and dm
/*                      Added error traps
/*          01/18/92    Edited title block
/*          02/03/96    Modified for use as Win 3.1 DLL
/*          01/01/98    Changes for MS VC++ compatibility & warnings
/*          04/26/03    Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

float __declspec(dllexport) FAR PASCAL CalcDegFree(int alpha, int n, int m)
{
    double dn;                /* double version of n */
    double dm;                /* double version of m */
    double df;                /* # degrees of freedom */
    double df1,df2,df3;       /* terms of df calculation */

    if( (n==0) || (m==0) )
    {
        return(-1.0);        /* error code */
    }

    dn=(double) abs(n);        /* make sure n is positive */
    dm=(double) abs(m);        /* make sure m is positive */

    switch(alpha)              /* alpha is exponent of power-law noise process */
    {                           /* slope of Sy(f) on log-log plot */
        case 2:
        {

```

```

if (dn==dm)
{
    return(-1.0);                                /* error code */
}

df=((dn+1)*(dn-(2*dm)))/(2*(dn-dm)); /* white phase noise */
break;                                           /* alpha=2 */
}
case 1:
{
    if (dn==1)
    {
        return(-1.0);                                /* error code */
    }
    df1=log(((2*dm)+1)*(dn-1))/(4); /* flicker phase noise */
    df2=log((dn-1)/(2*dm));          /* alpha=1) */
    if (df1*df2<0)
    {
        return(-1.0);                                /* error code */
    }
    df=exp(sqrt(df1*df2));
    break;
}
case 0:
{
    df1=(4*dm*dm)/((4*dm*dm)+5); /* white frequency noise */
    df2=(3*(dn-1))/(2*dm);        /* alpha=0 */
    df3=(2*(dn-2))/(dn);
    df=(df2-df3)*df1;
    break;
}
case -1:
{
    if (dm==1.0)                                /* flicker frequency noise */
    {
                                                /* alpha=-1 */
        df=(2*(dn-2)*(dn-2))/((2.3*dn)-4.9);
        break;
    }
    /* end if */
    else
    {
        df=(5*dn*dn)/((4*dm)*(dn+(3*dm)));
        break;
    }
    /* end else */
}
case -2:
{
    if (dn==3)
    {
        return(-1.0);                                /* error code */
    }
    df1=(dn-1)*(dn-1); /* random-walk frequency noise */
    df2=(dn-2)/((dm)*(dn-3)*(dn-3)); /* alpha=-2 */
    df3=(3*dm)*(1-dn)+(4*dm*dm);
    df=df2*(df1+df3);
    break;
}

```

```
        default:                                /* NG alpha */
        {
            df=-1.0;                             /* error code */
        }                                         /* end switch */

return(float)df;                                /* chi-squared degrees of freedom */
}                                                /* end CalcDegFree() */
```

The FrequenC Library	
<b>NAME:</b> CalcDiffusionFreqDrift()	<b>FUNCTION:</b> Calculate diffusion frequency drift. Fit fractional frequency data to time-shifted diffusion model: $y(t) = a + b\sqrt{t+c}$
<b>SYNOPSIS:</b> <pre>int CalcDiffusionFreqDrift(F_TYPE y[], F_TYPE *a, F_TYPE *b,                            F_TYPE *c, F_TYPE *v)</pre>	
F_TYPE y[]	Frequency data array y[0] = # data points y[1] = analysis start point y[2] = analysis end point
F_TYPE *a	Pointer to offset coefficient
F_TYPE *b	Square root of time multiplier coefficient
F_TYPE *c	Time shift coefficient
F_TYPE *v	Pointer to fit variance
<b>RETURN:</b> int	# non-gap data points processed, or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are used. All zeros are treated as gaps in frequency data. A value of c is chosen, the diffusion fit is found, and c is varied iteratively until the rms error is below a limit criterion. Need at least 2 non-zero data points.	
<b>EXAMPLE:</b> <pre>#include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* frequency data array */ F_TYPE a;   /* fit parameter a */ F_TYPE b;   /* fit parameter b */ F_TYPE c;   /* fit parameter c */ F_TYPE v;   /* fit variance */ int num;   /* # data points processed */ . . num= CalcLogFreqDrift (y, &amp;a, &amp;b, &amp;c, &amp;v);          /* call function */ printf("\na = %e", b = %e, c = %e, a, b, c);      /* display results */</pre>	
<b>SEE ALSO:</b> CalcLogFreqDrift()	
<b>REFERENCE:</b> None	

```

/*****
/*
/*          CalcDiffusionFreqDrift()
/*
/*          Function to calculate diffusion frequency drift
/*          Fit fractional frequency data to time-shifted diffusion model:
/*           $y(t) = a + b\sqrt{t+c}$ 
/*          where:  $y(t)$  = fractional frequency
/*          t      = time
/*          a      = offset term
/*          b      = sqrt time multiplier term
/*          c      = time shift term
/*
/*          Parameters:      F_TYPE y[] = frequency data
/*                          y[0] = # data points
/*                          y[1] = analysis start
/*                          y[2] = analysis end
/*                          F_TYPE *p_a = pointer to offset term
/*                          F_TYPE *p_b = pointer to sqrt time multiplier term
/*                          F_TYPE *p_c = pointer to time shift term
/*                          F_TYPE *p_v = pointer to fit variance
/*
/*          Return:          int          = # non-zero analysis points,
/*                                     or -1 if error
/*
/*          Notes:           Zeros treated as gaps in frequency data.
/*                          A value of c is chosen, the diffusion fit parameters
/*                          are found, and c is varied iteratively until the
/*                          rms error is below a limit criterion.
/*                          Need at least 2 non-zero data points.
/*
/*          Revision record:
/*          06/09/97      Created from CalcLogFreqDrift() of FrequenC Lib and
/*                          CalcDiffusionFreqDrift() of Stable/Win
/*          06/10/97      Running - converges OK
/*          12/09/97      Added to FrequenC Library
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1997-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcDiffusionFreqDrift(F_TYPE y[],
    F_TYPE *p_a, F_TYPE *p_b, F_TYPE *p_c, F_TYPE *p_v)
{
    int i;                                /* freq data index */
    int num = (int)(*(y+2) - *(y+1) + 1); /* # frequency data points */

    #if(0) // Original code of Release 1.01 - Doesn't always converge
    double error_limit=0.00000001;        /* fractional error limit for variance */
    #endif

    #if(1) // Trial code 06/20/97
    // This seems better - converges for all known test cases & results OK
    double error_limit=0.000001;          /* fractional error limit for variance */
    #endif

```

```

double err=1.0; /* sum of squared error */

double prev_err=0; /* initialized so (err-prev_err)/err > error_limit */
double sum_x; /* sum of x=sqrt(t+c) */
double sum_y; /* sum of y=t */
double sum_xx; /* sum of x^2 */
double sum_xy; /* sum of xy */
double d=100.0; /* c iteration factor */

*p_c=0.0; /* initial value for c */

while(fabs(((err-prev_err)/err))>error_limit) /* iterate */
{
    prev_err=err; /* save previous error */
    sum_x = 0; /* sum of x=sqrt(t+c) */
    sum_y = 0; /* sum of y */
    sum_xx = 0; /* sum of x^2 */
    sum_xy = 0; /* sum of xy */
    num = (int) (* (y+2) - * (y+1) +1); /* # frequency data points */

    for( i=(int) (* (y+1)+2); i<=(int) (* (y+2)+2); i++) /* accumulate sums */
    {
        if(* (y+i)) /* gap in data? */
        {
            sum_x += sqrt(((double) (i-2))+ *p_c);
            sum_y += * (y+i);
            sum_xx += ((double) (i-2))+ *p_c;
            sum_xy += sqrt(((double) (i-2))+ *p_c) * * (y+i);
        } /* end if */
        else
        {
            num--;
        } /* end else */
    } /* end for */

    if(num<2) /* must have at least 2 data points */
    {
        return(-1);
    } /* end if */

    *p_b = sum_xy - (sum_x * sum_y / num); /* find parameters */
    *p_b /= sum_xx- (sum_x * sum_x / num);
    *p_a = (sum_y - (*p_b * sum_x )) / num;

    err=0; /* calc sum of squared error */

    for( i=(int) (* (y+1)+2); i<=(int) (* (y+2)+2); i++)
    {
        if(* (y+i))
        {
            // error = SQR [ fit - actual = a + b*sqrt(t+c) - y(t) ]
            err += SQR(*p_a + *p_b * sqrt((double) (i-2)+ *p_c) - * (y+i));
        }
    }

    if(err>prev_err) /* wrong way? */
    {
        d *= -0.1;
    }

    *p_c+= d; /* modify c for next iteration */
}

```

```

        if(*p_c<0.0)                                /* avoid sqrt domain error */
        {
            d *= -0.1;
            *p_c=0.0;
        }

    }

    *p_v = err;

    return(num);

}                                                    /* end NewCalcDiffusionFreqDrift() */

```

The FrequenC Library	
<b>NAME:</b> CalcFirstDiff	<b>FUNCTION:</b> Calculate the average of the 1st differences (frequency offset) for phase data
<b>SYNOPSIS:</b> int CalcFirstDiff(F_TYPE x[], F_TYPE *d)	
F_TYPE x[]	Phase data array x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE *d	Pointer to average of 1st diffs of phase data
<b>RETURN:</b> int	# non-gap data points processed or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. Embedded zeros are treated as gaps in phase data. There must be at least 2 adjacent non-gap phase data points.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[512];                                       /* phase data array */ F_TYPE d;   /* 1<sup>st</sup> diff */ int num;   /* # data points processed */ . . num=CalcFirstDiff(x, &amp;d);                           /* call function */ printf("\nFreq Offset = %e", d);                   /* display result */ </pre>	
<b>SEE ALSO:</b> CalcFreqOffset()	
<b>REFERENCE:</b> NIST Technical Note 1337	

## FrequenC Library Reference Manual

```

/*****
/*
/*          CalcFirstDiff()
/*
/*      Function to calculate average of 1st differences of phase data
/*      Can also be used to check phase data for zero frequency due to
/*      zero first differences (equal adjacent phase points)
/*
/*      Parameters:      F_TYPE x[]  = array of phase data
/*                        x[0] = # phase data points
/*                        x[1] = analysis start
/*                        x[2] = analysis end
/*                        F_TYPE *p_d = pointer to average of first
/*                        differences of phase data
/*                        = frequency offset of phase data
/*                        = 0 if zero frequency point exists
/*
/*      Return:          int          = # analysis points,
/*                                or -1 if error
/*
/*      Note:            Embedded gaps are treated as gaps in phase data.
/*                        There must be at least 1 analysis point,
/*                        which requires at least 2 adjacent non-gap
/*                        phase data points.
/*
/*      Revision record:
/*          03/23/98      Created from CSD.C
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1998-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcFirstDiff(F_TYPE x[], F_TYPE *p_d)
{
    float num;
    double d1;
    double sum;
    int i;

    num = 0;
    sum = 0;

    for(i=(int) (x[1]+2); i<(int) (x[2]+1); i++)
    {
        if( (x[i] && x[i+1]) || (i==3 && x[4]) || ((i==x[0]+1) && x[i]) )
            /* no phase points are gaps, or 1st point with non-zero 2nd point, */
            /* or last point with non-zero next-to-last point */

```

```

{
    if(d1 == x[i+1] - x[i])
    {
        sum += d1;
        num++;
    }
    else
    {
        *p_d = 0.0;
        return(-1);
    }
}
/* end if */
/* end for */
}
if(num>0)
{
    *p_d = sum / num;
    return(int)num;
}
else
{
    return(-1);
}
/* error */
}
/* end CalcFirstDiff() */

```



The FrequenC Library	
<b>NAME:</b> CalcFreqHadamardDev	<b>FUNCTION:</b> Calc Hadamard deviation from frequency data
<b>SYNOPSIS:</b> int CalcFreqHadamardDev(F_TYPE y[], F_TYPE *dev)	
F_TYPE y[]	Frequency data array y[0] = # data points y[1] = analysis start point y[2] = analysis end point
F_TYPE *dev	Pointer to Hadamard deviation
<b>RETURN:</b> int	# non-gap data points processed or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. All zeros are treated as gaps in frequency data. Must have at least 3 adjacent non-gap freq data points.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* freq data array */ F_TYPE dev;  /* Hadamard deviation */ int num;   /* # data points processed */ . . num=CalcFreqHadamardDev(y, &amp;dev);                    /* call function */ printf("\nHadamard Dev = %e", dev);                 /* display result */ </pre>	
<b>SEE ALSO:</b> CalcPhaseHadamardDev	
<b>REFERENCE:</b> S. Hutsell, Proc. 27th PTTI Meeting, Dec. 1995	

```

/*****
/*
/*          CalcFreqHadamardDev()
/*
/*          Function to calculate Hadamard variance from frequency data
/*
/*
/*          
$$H_{\hat{y}}(\zeta) = \frac{1}{6(M-2)} \sum_{i=1}^{M-2} [y(i+2) - 2y(i+1) - y(i)]^2$$

/*
/*
/*
/*          Parameters:      F_TYPE y[]      = frequency data
/*                          y[0] = # data points
/*                          y[1] = analysis start
/*                          y[2] = analysis end
/*                          float *p_dev = pointer to Hadamard deviation
/*
/*          Return:          int              = # analysis points,
/*                                          or -1 if error
/*
/*          Note:            Embedded zeros treated as gaps in freq data.
/*                          Must have at least 1 analysis point; this
/*                          requires at least 3 adjacent non-gap freq data
/*                          points.
/*
/*          Reference:       S. Hutsell, Proc. 27th PTTI Meeting, Dec. 1995.
/*
/*          Revision record:
/*          05/03/96      Adapted from hadamardev_f() of STABLE_A.C
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/*          (c) Copyright 1996-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcFreqHadamardDev(F_TYPE y[],
F_TYPE *p_dev)
{
    double sum;                /* summing variable to calc sigma */
    int i;                     /* index for summing */
    int num = 0;                /* # analysis points */

    for( i = (int)(*(y+1)+2), sum = 0; i < (int)(*(y+2)+1); i++)
        /* index goes from 1 to n-2 */
        /* for n data points from 1 to n; data starts at y[3] */
    {
        if( *(y+i) && *(y+i+1) && *(y+i+2) )
            /* skip if any freq data value is zero */
        {
            sum += SQR( *(y+i+2) - 2 * *(y+i+1) + *(y+i) );
            num++;
        }
    }
}

```

```
if(num>0)
{
    *p_dev = ( sqrt( sum / (6.0 * num )));
    return(num);
}
else
{
    return(-1);
}
}
```

/\* # analysis points \*/

/\* no analysis points \*/

/\* error \*/



The FrequenC Library	
<b>NAME:</b> CalcFastMTIE	<b>FUNCTION:</b> Quickly calculate maximum time interval error for phase data
<b>SYNOPSIS:</b> <pre>int CalcFastMTIE(F_TYPE fX[], struct sigmadata *results, BOOL *abort, void *ProgressFunc(int percent, char *msg))</pre>	
F_TYPE x[]	Phase data array x[0] = # data points x[1] = analysis start point x[2] = analysis end point
struct sigmadata *results	Pointer to sigmadata structure for results
BOOL *abort	Pointer to abort flag (FALSE = no abort)
void *ProgressFunc( int percent, char *msg)	Pointer to function to display progress, with int arg set to % calc complete, and char* arg set to text message to display. Can be NULL.
<b>RETURN:</b> int	# MTIE points, or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are used. Embedded zeros are treated as gaps in phase data. Sigmadata structure is defined in frequenc.h This function calculates a complete set of MTIE points.	
<b>EXAMPLE:</b> <pre>#include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[512];                                       /* phase data array */ struct sigmadata results;                           /* MTIE results */ int num;   /* # MTIE points */ . . num=CalcFastMTIE(x, &amp;results FALSE, NULL);          /* call function */ /* No aborting or progress display */ printf("\nMTIE = %e", results.sigma[0]); /* display 1<sup>st</sup> MTIE point */</pre>	
<b>SEE ALSO:</b> CalcMTIE()	
<b>REFERENCE:</b> S. Bregni and S. Maccabruni, "Fast Computation of Maximum Time Interval Error by Binary Decomposition", IEEE Transactions on Instrumentation and Measurement, Vol. 49, No. 6, Dec. 2000, pp. 1240-1244.	

```

/*****
/*
/*          CalcFastMTIE()
/*
/*
/*  Function to calc MTIE (maximum time interval error) for phase data
/*  Parameters:
/*      F_TYPE fX[]      = data array, where:
/*                          F_TYPE fX[0] = # data points
/*                          F_TYPE fX[1] = analysis start
/*                          F_TYPE fX[2] = analysis end
/*      plotdata *pResults = MTIE results sigmadata structure
/*
/*
/*  Return:
/*      k      = Outer index (# MTIE points), or -1 if error
/*
/*
/*  sigmadata structure elements for sigma data:
/*      int      points      number of sigma data points
/*      float    *tau        pointer to averaging time data array
/*      float    *num        pointer to number of data points array
/*      float    *sigma      pointer to sigma data array
/*      float    *ci         pointer to confidence interval
/*      float    *sig_min    pointer to lower sigma error bar array
/*      float    *sig_max    pointer to upper sigma error bar array
/*      float    *std_dev    pointer to standard deviation array
/*      int      *alpha      pointer to noise type exponent array
/*      int      *af         pointer to averaging factor
/*
/*
/*  Note: Signature of this function is necessarily different from
/*  CalcMTIE() because it includes the outer averaging factor loop.
/*  It is used differently in main program.
/*
/*
/*  Basic Algorithm:
/*      An n-point wide window is moved thru the phase data and the
/*      difference between the maximum and minimum phase (time) values
/*      is found at each window position.  MTIE is the overall maximum
/*      of this time interval error over the whole data set.
/*
/*
/*  Fast Algorithm:
/*      Calc MTIE in octave steps only.  Store max and min for each tau
/*      = AF*tau0 in two vectors.  For next AF, just search these
/*      vectors, not all data, for next maxs and mins.
/*
/*
/*  Notes:
/*      (1) This function does not handle gaps.
/*      (2) No abort option or progress message for this function
/*      (4) # time intervals is N-1, where N = # phase data points, so
/*          AF can go from 1 to N-1.
/*      (3) B&M algorithm uses AF sequence 1,3,7,15,...2^k -1
/*          where k is outer index that goes from 1 to <= log2(N)
/*
/*
/*  Reference 1:
/*      S. Bregni, "Clock Stability Characterization and Measurement
/*      in Telecommunications", IEEE Transactions on Instrumentation
/*      and Measurement, Vol. 46, No. 6, Dec. 1997, pp. 1284-1294,
/*      Eq. 14.
/*
/*  Reference 2:
/*      S. Bregni and S. Maccabruni, "Fast Computation of Maximum Time
/*      Interval Error by Binary Decomposition", IEEE Transactions on
/*      Instrumentation and Measurement, Vol. 49, No. 6, Dec. 2000, pp.
/*      1240-1244.

```

```

/*                                                                 */
/*      Revision record:                                          */
/*      01/26/01   Drafted from CalcMTIE()                      */
/*      01/27/01   Running                                       */
/*      01/28/01   Added progress message                       */
/*      Changed 2nd param to plotdata struct                    */
/*      Changed min & max arrays from F_TYPE to float          */
/*      Tried various speed enhancements                       */
/*      Moved here from stable_r.c to use compiler speed      */
/*      optimizations - they work the best                     */
/*      Copy in stable_r.c still has debug code if needed.     */
/*      01/30/01   Added results on-the-fly & progress display  */
/*      03/22/03   Adapted for FrequenC DLL                    */
/*      Added abort flag & progress function arguments        */
/*      Not yet fully-integrated into FrequenC DLL             */
/*      Function prototype now in frequenc.h                   */
/*      04/26/03   Adapted for Version 2.0 source code documentation */
/*                                                                 */
/* (c) Copyright 2001-3   Hamilton Technical Services   All Rights Reserved */
/*                                                                 */
/*****

```

```
#include "frequenc.h"
```

```
// Struct for sigma run data
```

```

struct sigmadata /* structure template for sigma data */
{
    int points; /* number of sigma data points */
    int rows; /* # rows of results = # tau values */
    float *tau; /* pointer to averaging time data array */
    float *num; /* pointer to number of data points array */
    float *sigma; /* pointer to sigma data array */
    float *ci; /* pointer to confidence interval from SIGMA.TAU file */
    float *sig_min; /* pointer to lower sigma error bar array */
    float *sig_max; /* pointer to upper sigma error bar array */
    float *std_dev; /* pointer to standard deviation array */
    float *df; /* pointer to degrees of freedom array */
    int *alpha; /* pointer to power-law noise type exponent array */
    int *af; /* pointer to averaging factor array */
};

```

```

int __declspec(dllexport) FAR PASCAL CalcFastMTIE(F_TYPE fX[],
struct sigmadata *pResults, BOOL *bAbort,
void *ProgressFunction(int nPercentDone, char *szMessage))

```

```

{
    // Local variables
    // Ints
    int i; /* Inner and general inner index */
    int j; /* Middle index */
    int last_j; /* Previous middle index */
    int k; /* Outer index */
    int p; /* Span */
    int nStart; /* Analysis start */
    int nEnd; /* Analysis end */
    int nNum; /* # analysis points */
    int nAF; /* Averaging factor */
    int nStop; /* Max value of outer index */
    int tic; /* Progress interval */
    // Floats
    float fMTIE; /* Current MTIE value */

```

```

float *fSmall;                // Min phase data value array
float *fBig;                  // Max phase data value array

// Initialize progress display
ProgressFunction(0, "Calculating MTIE");

// Set analysis limits
nStart=(int)fX[1];
nEnd=(int)fX[2];
nNum=nEnd-nStart+1;

// Allocate working memory for max and min vectors
// First pass they must be same size as analysis data array (w/o header)
// Together they hold all points in overlapping big/small pairs
// No point in reallocing as they get smaller

// Allocate maximum array
if((fBig=(float*)malloc((nNum)*sizeof(float)))==NULL)
{
    return -1; // Error
}

// Allocate minimum array
if((fSmall=(float*)malloc((nNum)*sizeof(float)))==NULL)
{
    free(fBig);
    return -1; // Error
}

// Initialize the max and min arrays by copying the phase data into them
for(i=0; i<nNum; i++)
{
    // Copy data
    fBig[i]=(float)fX[nStart+ARRAY_OFFSET+i-1];
    fSmall[i]=(float)fX[nStart+ARRAY_OFFSET+i-1];
}

// Calc MTIE
// Outer k loop over octave AFs up to max nAF = nNum-1
// nAF is 2^k -1 and max k is log2(nNum)

// Find maximum outer index = log2(nNum) as truncated integer
nStop=(int)(log(nNum)/log(2));

// Calc MITE points at octave averaging factors up to largest possible
for(k=1; k<=nStop; k++)
{
    // Find the current averaging factor nAF = 2^k -1
    nAF=(int)(pow(2, k))-1;

    // Find the current span p = 2^(k-1)
    p=(int)(pow(2, k-1));

    // Initialize previous middle index
    last_j=0;

```

```

// Update the min & max vectors for this AF
// Loop through all nNum-AF points
for(j=0; j<nNum-nAF; j++)
{
    /* Set 1% interval for progress report */

    tic=(int)ceil((nNum-nAF)/100);

    // The max and min values are already initialized
    // Find max & min values for each step in this window of span p
    // Note: This is apparently the section of code that takes the
    // most time as nAF and k get larger, and p gets much larger
    // But its hard to see how one can do any better than the
    // max() and min() macros.
    // This code was tried with index arithmetic outside loop
    // and just incrementing inside - little difference in speed
    // Pointer arithmetic was also tried - ditto
    // What does help is to ask the compiler to optimize for speed
    // That makes 5:1 improvement for any of the code versions
    for(i=1; i<=p; i++)
    {
        fBig[j]=max(fBig[j+i], fBig[j]);
        fSmall[j]=min(fSmall[j+i], fSmall[j]);
    }

    // Display progress
    // Note: This code provides updates only if index has changed
    // by at least tic amount (1%)
    if((j-last_j)>=tic)
    {
        ProgressFunction((int)(100.0*j/(nNum-nAF)),
            "Calculating MTIE");
        last_j=j;
    }
}

// Initialize the MTIE value
// Note that the results array is zero-based
fMTIE=(float)(fBig[0]-fSmall[0]);

// Loop thru the rest of the nNum-nAF points in each vector
for(i=1; i<nNum-nAF; i++)
{
    // MTIE is the overall maximum p-p excursion
    fMTIE=(float)(max((fBig[i]-fSmall[i]), fMTIE));
}

// Store results
pResults->sigma[k-1]=fMTIE;
pResults->points=k;
pResults->af[k-1]=nAF;
pResults->num[k-1]=(float)(nNum-nAF);
// Note: tau calc external to this function

```

```
// Check for abort
if(bAbort)
{
    // Bail out - program flow goes to code below, then to IDCANCEL
    // handler, and finally back to where this function was called
    break;
}

// Free working memory
free(fBig);
free(fSmall);

// Done
// Clear progress display
ProgressFunction(0, "");
return k;
}
```

The FrequenC Library	
<b>NAME:</b> CalcFreqModSigma	<b>FUNCTION:</b> Calculate modified Allan deviation for frequency data
<b>SYNOPSIS:</b> int CalcFreqModSigma(F_TYPE y[], F_TYPE *p_sig, int m)	
F_TYPE y[]	Frequency data array: y[0] = # data points y[1] = analysis start point y[2] = analysis end point
F_TYPE *p_sig	Pointer to sig, the modified Allan deviation for the frequency data
int m	Averaging factor, $m = \tau/\tau_0$
<b>RETURN:</b> int	The # of non-gap data points processed, or -1 if error.
<b>REMARKS:</b> All zeros are treated as gaps in frequency data. Only data points between start and end analysis limits are analyzed. There must be at least 2 non-gap analysis points. Maximum $m = (\text{int}) (\# \text{ freq data points} + 1) / 3$ . This calculation of the modified Allan variance from frequency data that may contain gaps is slow. Use ConvFreqToPhase() and CalcPhaseModSigma(), or preferably ConvFreqToPhase(), FillGaps() and CalcFastModSigma() if the # of data points is large.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* frequency data array */ F_TYPE sig;  /* modified Allan deviation */ int m;  /* averaging factor */ int num;   /* # data points processed */ . . m=2;  /* assign value to m */ num=CalcFreqModSigma(y, &amp;sig, m);                 /* calc mod sigma */ if(num==-1)  /* check for error */ {     printf("\nError");                             /* error message */ } else {     printf("\nMod Sigma = %e", sig);                /* display mod sigma */     printf("\n# Data Points Analyzed = %d", num);   /* display num */ } </pre>	
<b>SEE ALSO:</b> CalcFreqSigma(), CalcPhaseModSigma()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*          CalcFreqModSigma()
/*
/*          Function to calculate modified Allan deviation for freq dat
/*
/*          Parameters:      F_TYPE y[]      = frequency data
/*                          y[0] = # data points
/*                          y[1] = analysis start
/*                          y[2] = analysis end
/*                          F_TYPE *p_sig = pointer to mod Allan deviation
/*                          int m         = averaging factor = tau/tau_0
/*
/*          Return:         int              = # analysis points,
/*                                         or -1 if error
/*
/*          Notes:          Zeros treated as gaps in frequency data.
/*                          Frequency data is not averaged before calling
/*                          this function. The data consists of num-1 freq
/*                          samples at interval tau_0. m must be >0.
/*                          Denominator term (num-3m+1) must be >=1
/*                          This sets max m=(int)(num/3), where num=
/*                          (# frequency points +1) before averaging.
/*
/*          Revision record:
/*          12/16/91      Created
/*          12/31/91      Renamed
/*          01/16/92      Edited per FrequenC documentation
/*          01/17/92      Edited title
/*          01/18/92      Edited title block
/*          01/19/92      Added error traps
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcFreqModSigma(F_TYPE y[],
F_TYPE *p_sig, int m)
{
    double sum_i, sum_j, sum_k;      /* summing variables to calc mod sigma */
    float fm;                        /* float version of m */
    int i;                           /* index for inner summing loop */
    int j;                           /* index for outer summing loop */
    int k;                           /* index for inner averaging loop */
    int n_avg;                        /* # points in averaging loop */
    int n_sum=0;                     /* # points in outer summing loop */
    int num = (int)(*(y+2)-*(y+1)+2); /* # phase data points for analysis */
                                         /* = # freq points +1 */

    if( (m<1) || (num<3*m) )
    {
        return(-1);                  /* error */
    }

    fm=(float)m;
    sum_j=0;

```

```

for(j=1; j<=num-(3*m)+1; j++)                                /* outer loop */

    /* j goes from 1 to N-3m+1 where N=# phase points & m=avg factor */
    /* regardless of analysis limits */
    {
        sum_i=0;
        for(i=j+(int) (*(y+1))-1; i<=m+j-1+(int) (*(y+1))-1; i++) /* inner */
            /* i is the actual freq data index; it includes a term */
            /* *(y+1)-1 to account for the analysis starting point */
            /* the data array offset +2 is included in the code below */
            {
                sum_k=0;
                n_avg=0;                                       /* # freq differences averaged */
                for(k=i; k<=i+m-1; k++)                       /* find frequency averages */
                {
                    if(*(y+k+2+m) && *(y+k+2))               /* skip if either is zero */
                    {
                        sum_k += *(y+k+2+m) - *(y+k+2);
                        n_avg++;
                    }
                    /* end if */
                }
                /* end for */
                if(n_avg)                                     /* test to avoid div by 0 if all gaps */
                {
                    sum_i+=sum_k/n_avg;
                }
            }
            /* end for */
        }
        if(sum_i)
        {
            sum_j += SQR(sum_i);
            n_sum++;
        }
        /* if */
    }
    /* end for */
    if(n_sum>0)
    {
        *p_sig = sqrt((sum_j)/(2.0*fm*fm*n_sum));
        return(n_sum);                                       /* # analysis points */
    }
    else
    {
        return(-1);                                         /* error */
    }
}
/* end CalcFreqModSigma() */

```



The FrequenC Library	
<b>NAME:</b> CalcFastModSigma	<b>FUNCTION:</b> Quickly calculate modified Allan deviation for gapless phase data
<b>SYNOPSIS:</b> int CalcFastModSigma(F_TYPE x[], F_TYPE *p_sig, F_TYPE tau, int m)	
F_TYPE x[]	Phase data array: x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE *p_sig	Pointer to sig, the modified Allan deviation for the phase data
F_TYPE tau	The averaging time for the phase data
int m	Averaging factor, m = tau/tau_0
<b>RETURN:</b> int	The # of data points processed, or -1 if error
<b>REMARKS:</b> No gaps are allowed in the phase data. Only data points between start and end analysis limits are analyzed. There must be at least 3 analysis points. Tau must be >0. Maximum m = (int)(# phase data points/3, and m must be >0. This calculation of the modified Allan variance from gapless phase data is faster than any other method. Use CalcPhaseModSigma() if there are gaps in the phase data, or, preferably, FillGaps() and CalcFastModSigma() if the # of phase data points is large.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[512];                                       /* phase data array */ F_TYPE sig;  /* mod sigma */ F_TYPE tau;  /* averaging time */ int m;  /* averaging factor */ int num;   /* # data points processed */ . . tau=1.0; m=2;                                       /* assign values to tau and m */ num=CalcFastModSigma(x, &amp;sig, tau, m);              /* calc mod sigma */ if(num==-1)   /* check for error */ {     printf("\nError");                             /* error message */ } else {     printf("\nMod Sigma = %e", sig);                /* display mod sigma */     printf("\n# Data Points Analyzed = %d", num);    /* display num */ } </pre>	
<b>SEE ALSO:</b> CalcPhaseModSigma()	

```

/*****
/*
/*          CalcFastModSigma()
/*
/*      Function to calculate modified Allan variance for phase data
/*      Uses faster algorithm that avoids recalculation of inner sums
/*
/*      Reference:      D.W. Allan, "Time and Frequency Metrology:
/*                      Current Status and Future Considerations",
/*                      Proc. 5th EFTF, pp. 1-9, March, 1991
/*
/*      Parameters:      F_TYPE x[]      = phase data
/*                      x[0] = # data phase points
/*                      x[1] = analysis start
/*                      x[2] = analysis end
/*                      F_TYPE *p_sig = pointer to mod Allan deviation
/*                      F_TYPE tau     = analysis averaging time = m*tau_0
/*                      int m          = averaging factor = tau/tau_0
/*
/*      Return:          int              = # analysis points,
/*                                      or -1 if error
/*
/*      Notes:           No gaps allowed in data; check for embedded zeros
/*                      before using this function. If gaps, use (slower)
/*                      CalcPhaseModSigma(), or use FillGaps() first.
/*                      Phase data is not averaged before calling this
/*                      function. The data consists of num phase samples
/*                      at interval tau_0. Denominator term (num-3m+1)
/*                      must be >0. This sets max m=(int)(num/3),
/*                      where num=# phase points before averaging.
/*
/*      Revision record:
/*          12/16/91      Created
/*          12/31/91      Renamed
/*          01/16/92      Edited per FrequenC documentation
/*          01/17/92      Edited title
/*          01/18/92      Edited title block
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __cdeclspec(dllexport) FAR PASCAL CalcFastModSigma(F_TYPE x[],
F_TYPE *p_sig, F_TYPE tau, int m)
{
    double sum_i, sum_j;          /* summing variables to calc modified sigma */
    float fm;                     /* float version of m */
    int i;                        /* index for inner summing loop */
    int j;                        /* index for outer summing loop */
    int s = (int)*(x+1);          /* analysis start */
    int e = (int)*(x+2);          /* analysis end */
    int n_sum=0;                  /* # points in outer summing loop */
    int num = e-s+1;              /* # phase data points for analysis */

```

```

fm=(float)m;

sum_j=0;
sum_i=0;

if( (num<3*m) || (m<1) || (tau<=0) )
{
    return(-1);                                /* error */
}

/* 1st time find the average of all m phase points by summing them */
for(i=s; i<m+s; i++)                          /* i is the actual phase data index */
    /* it includes the term s to account for the analysis starting point */
    /* the data array offset +2 is included in the code below */
    {
        sum_i += *(x+i+2+(2*m)) - (2*(*(x+i+2+m))) + *(x+i+2);
    }

sum_j += SQR(sum_i);
n_sum++;

/* for rest of points need only drop 1st sum and add next sum */
for(j=2; j<=num-(3*m)+1; j++)                  /* j goes from 2 to num-3m+1 */
    /* where num=# phase points & m=avg factor */
    /* regardless of analysis limits */
    {
        i=j+s-2;                                /* index of old sum_i being dropped */
        sum_i -= *(x+i+2+(2*m)) - (2*(*(x+i+2+m))) + *(x+i+2);

        i=m+j-1+s-1;                            /* index of next sum_i being added */
        sum_i += *(x+i+2+(2*m)) - (2*(*(x+i+2+m))) + *(x+i+2);

        sum_j += SQR(sum_i);
        n_sum++;
    }
    /* end if */

if(n_sum>0)                                    /* avoid div by 0 */
{
    *p_sig = sqrt((sum_j)/(2.0*tau*tau*fm*fm*n_sum));
    return(n_sum);                            /* # analysis points */
}
else
{
    return(-1);                                /* error */
}
    /* end CalcFastModSigma() */
}

```



The FrequenC Library	
<b>NAME:</b> CalcFreqOffset	<b>FUNCTION:</b> Calc freq for phase data as slope of least-squares linear fit to phase data: $x(t)=a+bt$
<b>SYNOPSIS:</b> int CalcFreqOffset(F_TYPE x[], F_TYPE *a, F_TYPE *b, F_TYPE *v)	
F_TYPE x[]	Phase data array x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE *a	parameter one, and description of what it is
F_TYPE *b	Pointer to slope = freq offset
F_TYPE *v	Pointer to fit variance
<b>RETURN:</b> int	# non-gap data points processed, or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. Embedded zeros are treated as gaps in phase data. # non-gap data points must be at least 2 and at least 3 to calc finite fit variance.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[512];                                       /* phase data array */ F_TYPE a;   /* phase offset */ F_TYPE b;   /* phase slope */ F_TYPE c;   /* fit variance */ int num;   /* # data points processed */ . . num=CalcFreqOffset(x, &amp;a, &amp;b, &amp;c);                  /* call function */ printf("\nFreq Offset = %d", b);                   /* display result */ </pre>	
<b>SEE ALSO:</b> RemoveFreqOffset()	
<b>REFERENCE:</b> NIST Technical Note 1337	

## FrequenC Library Reference Manual

```

/*****
/*
/*          CalcFreqOffset()
/*
/*          Function to calculate freq for phase data:  $x(t)=a+bt$ 
/*
/*          Parameters:      F_TYPE x[]   = phase data
/*                          x[0] = # data points
/*                          x[1] = analysis start
/*                          x[2] = analysis end
/*                          F_TYPE p_a   = pointer to y-intercept
/*                          F_TYPE p_b   = pointer to slope = freq offset
/*                          F_TYPE p_v   = pointer to fit variance
/*
/*          Return:          int           = # analysis points,
/*                                      or -1 if error
/*
/*          Notes:           Embedded zeros treated as gaps in phase data
/*                          # non-gap data points must be at least 2
/*                          and at least 3 to calc finite fit variance
/*
/*          Revision record:
/*          02/22/97      Adapted from CalcLinFreqDrift() of Frequent
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1997-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __cdeclspec(dllexport) FAR PASCAL CalcFreqOffset(F_TYPE x[], F_TYPE *p_a,
F_TYPE *p_b, F_TYPE *p_v)
{
    int i;
    int num = (int) (*(x+2) - *(x+1) + 1);
    double sum_x = 0;
    double sum_y = 0;
    double sum_xx = 0;
    double sum_yy = 0;
    double sum_xy = 0;

    for( i = (int) *(x+1) + 2; i <= (int) *(x+2) + 2; i++)
    {
        if( (*(x+i)) || (i==3) || (i==*(x+2)+2) )          /* check for gap */
        {
            sum_x  += i-2;
            sum_y  += *(x+i);
            sum_xx += SQR ( (float) (i-2) );                /* must cast to float */
            sum_yy += SQR ( *(x+i) );
            sum_xy += (i-2) * *(x+i);
        }
        else
        {
            num--;
        }
    }
}

```

```

if(num<2)
{
    return(-1);                                /* error */
}

*p_b = (sum_xy - ((sum_x) * (sum_y) / num));
*p_b = *p_b / (sum_xx - ((sum_x) * (sum_x) / num));
*p_a = ((sum_y) / num) - (*p_b * sum_x / num);
*p_v = 0;                                       /* fit variance 0 if only 2 points */

if(num>=3)    /* need at least 3 analysis points to calc fit variance */
{
    *p_v = sum_yy - (sum_y * sum_y / num);
    *p_v -= *p_b * *p_b * (sum_xx - (sum_x * sum_x / num));
    *p_v /= (num-2);
}

return(num);
}

```



The FrequenC Library	
<b>NAME:</b> CalcFreqOverlap HadamardDev	<b>FUNCTION:</b> Description of what function does
<b>SYNOPSIS:</b> int FunctionName( F_TYPE z[], F_TYPE one, F_TYPE two)	
F_TYPE z[]	Phase or frequency data array z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE one	parameter one, and description of what it is
F_TYPE two	parameter two, and description of what it is
<b>RETURN:</b> int	# non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are modified. Embedded zeros are treated as gaps in phase data. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include &lt;frequenc.h&gt;                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ F_TYPE one;   /* parameter one */ F_TYPE two;   /* parameter two */ int num;   /* # data points processed */ . . one=1.0;   /* set 1st parameter value */ two=2.0;   /* set 2nd parameter value */ num=FunctionName(z, one, two);                     /* call function */ printf("\n# Data Points Scaled = %d", num);        /* display num */ </pre>	
<b>SEE ALSO:</b> RelatedFunctionName()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*          CalcFreqOverlapHadamardDev()
/*
/*          Function to calc Hadamard deviation using overlapping samples
/*          of frequency data
/*
/*          Parameters:      F_TYPE y[]      = frequency data array
/*                          y[0] = # data points
/*                          y[1]  = analysis start
/*                          y[2]  = analysis end
/*                          F_TYPE *p_sig = pointer to Hadamard deviation
/*                          int m        = averaging factor
/*
/*          Return:         int              = # analysis points,
/*                                         or -1 if error
/*
/*          Note:           Zeros treated as gaps in frequency data.
/*                          Must have at least 1 analysis point; this
/*                          requires at least two adjacent non-gap frequency
/*                          data points. m must be >0 and must have at least
/*                          3 non-gap adjacent frequency data points.
/*
/*          Revision record:
/*          03/06/99      Created from CFOS.C of Frequenc32 Library
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1999-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcFreqOverlapHadamardDev(F_TYPE y[],
    F_TYPE *p_sig, int m)
{
    double sum_j, sum_i;          /* summing variables to calc sigma */
    float fm=(float) m;           /* float version of m */
    int i;                        /* inner index for averaging */
    int j;                        /* outer index for summing 1st differences */
    int num=0;                    /* # analysis points */
    int n;                        /* # frequency data points */

    n=(int) (*(y+2)- *(y+1)+2);    /* total # phase data points */
                                   /* N=M+1 where M is # freq points */

    if(m<1)
    {
        return(-1);               /* error */
    }

    sum_j=0;
    for( j=1; j<=n-(3*m); j++)    /* outer loop */
                                   /* j goes over basic range from 1 to N-3m */
    {
        sum_i=0;

```

```

for(i=(int)(j+*(y+1)-1)); i<=(int)(j+*(y+1))-1+m-1; i++)
    /* inner loop */
    /* i index includes analysis start limit of *(y+1) */
    /* data array offset of 2 is included in code below */
{
    if(*(y+i+2*m+2) && *(y+1+m+2) && *(y+i+2))
    {
        sum_i += *(y+i+2*m+2) - *(y+i+m+2) - *(y+i+m+2) + *(y+i+2);
    }
    /* end if */
}
/* end for */
if(sum_i)
{
    sum_j += SQR(sum_i);
    num++;
}
/* end if */
}
/* end for */
if(num>0)
{
    *p_sig=sqrt(sum_j/(6.0*fm*fm*num));
    return(num);
}
/* # analysis points */
}
else
{
    return(-1);
}
/* error */
}
/* end CalcFreqOverlapHadamardDev() */

```



The FrequenC Library	
<b>NAME:</b> CalcFreqOverlapSigma	<b>FUNCTION:</b> Calculate overlapping Allan deviation for frequency data
<b>SYNOPSIS:</b> int CalcFreqOverlapSigma(F_TYPE y[], F_TYPE *p_sig, int m)	
F_TYPE y[]	Frequency data array: y[0] = # data points y[1] = analysis start point y[2] = analysis end point
F_TYPE *p_sig	Pointer to sig, the overlapping Allan deviation for the frequency data
int m	Averaging factor, $m = \tau/\tau_0$
<b>RETURN:</b> int	The # of non-gap data points processed, or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are modified. There must be at least 2 non-gap analysis points. Maximum $m = (\text{int})(\# \text{ freq data points} - 1)/2$ , and $m$ must be $>0$ . All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include &lt;stdio.h&gt; #include "frequenc.h" F_TYPE y[512]; F_TYPE sig; int m; int num;  . . m=2; num=CalcFreqSigma(y, &amp;sig, m); if(num==-1) {     printf("\nError"); } else {     printf("\nSigma = %e", sig);     printf("\n# Data Points Analyzed = %d", num); } </pre> <div style="text-align: right;"> /* for printf() */  /* FrequenC header file */  /* frequency data array */  /* overlapping Allan deviation */  /* averaging factor */  /* # data points processed */   /* assign value to m */  /* calc overlapping sigma */  /* check for error */  /* error message */  /* display overlapping sigma */  /* display num */ </div>	
<b>SEE ALSO:</b> CalcFreqSigma(), CalcPhaseOverlapSigma()	
<b>REFERENCE:</b> NIST Technical Note 1337	

## FrequenC Library Reference Manual

```

/*****
/*
/*          CalcFreqOverlapSigma()
/*
/*          Function to calculate Allan deviation using overlapping samples
/*          of frequency data
/*
/*          Parameters:      F_TYPE y[]      = frequency data array
/*                          y[0] = # data points
/*                          y[1]  = analysis start
/*                          y[2]  = analysis end
/*                          F_TYPE *p_sig = pointer to Allan deviation
/*                          int m        = averaging factor
/*
/*          Return:         int              = # analysis points,
/*                                         or -1 if error
/*
/*          Note:           Zeros treated as gaps in frequency data.
/*                          Must have at least 1 analysis point; this
/*                          requires at least two adjacent non-gap frequency
/*                          data points. m must be >0 and the # non-gap
/*                          frequency data points M must be > 2m-1.
/*
/*          Revision record:
/*          12/16/91      Created
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*                          Added error traps
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          01/29/99      Test for zero 1st difference removed to avoid
/*                          problem with low-precision data where two
/*                          adjacent frequency data point are identical.
/*          03/08/03      Brought into Ver 2.0 of FrequenC lib
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcFreqOverlapSigma(F_TYPE y[],
    F_TYPE *p_sig, int m)
{
    double sum_j, sum_i;          /* summing variables to calc sigma */
    float fm=(float) m;           /* float version of m */
    int i;                        /* inner index for averaging */
    int j;                        /* outer index for summing 1st differences */
    int num=0;                    /* # analysis points */
    int n;                        /* # frequency data points */

    n=(int) (*(y+2)-*(y+1)+2);    /* total # phase data points */
                                /* N=M+1 where M is # freq points */

    if( (m<1) || (n<2*m) )
    {
        return(-1);              /* error */
    }

    sum_j=0;

```

```

for( j=1; j<=n-(2*m); j++)                                /* outer loop */
    /* j goes over basic range from 1 to N-2m */
{
    sum_i=0;
    for(i=(int) (j+*(y+1)-1)); i<=(int) (j+*(y+1))-1+m-1; i++)
        /* inner loop */
        /* i index includes analysis start limit of *(y+1) */
        /* data array offset of 2 is included in code below */
        {
            if(*(y+i+m+2) && *(y+i+2))
            {
                sum_i += *(y+i+m+2) - *(y+i+2);
            }
            /* end if */
        }
        /* end for */

    sum_j += SQR(sum_i);
    num++;
}
/* end for */

if(num>0)
{
    *p_sig=sqrt(sum_j/(2.0*fm*fm*num));
    return(num);
}
/* # analysis points */

else
{
    return(-1);
}
/* error */

}
/* end CalcFreqOverlapSigma() */

```



The FrequenC Library	
<b>NAME:</b> CalcFreqSigma	<b>FUNCTION:</b> Calculate Allan deviation for frequency data
<b>SYNOPSIS:</b> int CalcFreqSigma(F_TYPE y[], F_TYPE *p_sig)	
F_TYPE y[]	Frequency data array: y[0] = # data points y[1] = analysis start point y[2] = analysis end point
F_TYPE *p_sig	Pointer to sig, the Allan deviation for the frequency data
<b>RETURN:</b> int	The # of non-gap data points processed, or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. There must be at least 2 non-gap analysis points. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* frequency data array */ F_TYPE sig;  /* Allan deviation */ int num;   /* # data points processed */ . . num=CalcFreqSigma(y, &amp;sig);                          /* calc sigma */ if(num==-1)   /* check for error */ {     printf("\nError");                               /* error message */ } else {     printf("\nSigma = %e", sig);                      /* display sigma */     printf("\n# Data Points Analyzed = %d", num);    /* display num */ } </pre>	
<b>SEE ALSO:</b> CalcPhaseSigma()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*          CalcFreqSigma()
/*
/*          Function to calculate Allan variance from frequency data
/*
/*          Parameters:      F_TYPE y[]      = frequency data
/*                          y[0] = # data points
/*                          y[1] = analysis start
/*                          y[2] = analysis end
/*                          F_TYPE *p_sig = pointer to Allan deviation
/*
/*          Returns:         int              = # analysis points,
/*                                          or -1 if error
/*
/*          Note:            Zero value treated as gap in frequency data.
/*                          Must have at least 1 analysis point; this
/*                          requires at least 2 adjacent non-gap frequency
/*                          data points.
/*
/*          Revision record:
/*          12/16/91      Created
/*          12/26/91      Changed to int returning # analysis points
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*                          Added error trap
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcFreqSigma(F_TYPE y[],
F_TYPE *p_sig)
{
    double sum;                /* summing variable to calc sigma */
    int i;                     /* index for summing */
    int num = 0;               /* # analysis points */

    for( i = (int)(*(y+1)+2), sum = 0; i < (int)(*(y+2)+2); i++)
        /* index goes from 1 to n-1 */
        /* for n data points from 1 to n; data starts at y[3] */
        {
            if( *(y+i) && *(y+i+1) ) /* skip if either value is zero */
            {
                sum += SQR( *(y+i+1) - *(y+i) );
                num++;
            }
        }
        /* end if */
        /* end for */
    if(num>0)
    {
        *p_sig = ( sqrt( sum / (2.0 * num) ));
        return(num); /* # analysis points */
    }
}

```

```
else
{
    return(-1);
}
/* error */
/* end CalcFreqSigma() */
```



The FrequenC Library	
<b>NAME:</b> CalcFreqStdDev	<b>FUNCTION:</b> Calculate standard deviation for frequency data
<b>SYNOPSIS:</b> int CalcFreqStdDev(F_TYPE y[], F_TYPE *p_dev)	
F_TYPE y[]	Frequency data array: y[0] = # data points y[1] = analysis start point y[2] = analysis end point
F_TYPE *p_dev	Pointer to dev, the standard deviation for the frequency data
<b>RETURN:</b> int	The # of non-gap data points processed, or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. There must be at least 2 non-gap analysis points. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* frequency data array */ F_TYPE dev;  /* standard deviation */ int num;   /* # data points processed */ . . num=CalcFreqSigma(y, &amp;dev);                          /* calc sigma */ if(num== -1)   /* check for error */ {     printf("\nError");                               /* error message */ } else {     printf("\nStd Dev = %e", dev);                   /* display sigma */     printf("\n# Data Points Analyzed = %d", num);    /* display num */ }           </pre>	
<b>SEE ALSO:</b> CalcPhaseStdDev()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*          CalcFreqStdDev()
/*
/*      Function to calculate standard deviation from frequency data
/*
/*      Parameters:      F_TYPE y[]      = frequency data
/*                      y[0] = # data points
/*                      y[1] = analysis start
/*                      y[2] = analysis end
/*                      F_TYPE *p_dev = pointer to standard deviation
/*
/*      Return:          int              = # analysis points,
/*                                      or -1 if error
/*
/*      Note:            All zeros treated as gaps in frequency data.
/*                      Must have at least 2 non-gap freq data points.
/*
/*      Revision record:
/*          12/16/91      Created
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          01/19/92      Added error trap
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved */
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcFreqStdDev(F_TYPE y[],
F_TYPE *p_dev)
{
    double sum=0;                                /* summing variable */
    double avg;                                  /* mean value of freq data */
    int i;                                       /* index for summing */
    int num = (int) (* (y+2) - * (y+1) + 1);    /* # analysis points */

    for(i=(int) (* (y+1) + 2); i<=(int) (* (y+2)) + 2; i++)    /* calc average */
    {
        if(* (y+i))
        {
            sum += * (y+i);
        }
        else
        {
            num--;
        }
    }
    if((num-1)>0)                                /* check for <2 non-gap data points */
    {
        avg = sum/num;
    }
    else
    {
        return(-1);                            /* error */
    }
}

```

```

sum=0;
for(i=(int) (* (y+1)+2); i<=(int) (* (y+2)+2); i++)      /* calc variance */
{
    if(* (y+i))                                           /* skip if value is zero */
    {
        sum += SQR(* (y+i) - avg);
    }
}                                                         /* end if */
*p_dev = (sqrt(sum/(num- 1)));                           /* end for */
return(num);
                                                         /* # analysis points */
}                                                         /* end CalcFreqStdDev() */

```



The FrequenC Library	
<b>NAME:</b> ConvFreqToPhase	<b>FUNCTION:</b> Convert frequency data to phase data
<b>SYNOPSIS:</b> int ConvFreqToPhase(F_TYPE y[], F_TYPE x[], F_TYPE tau, BOOL do_norm)	
F_TYPE y[]	Frequency data array: y[0] = # data points y[1] = analysis start point y[2] = analysis end point
F_TYPE x[]	Phase data array x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE tau	Averaging time of frequency data
BOOL do_norm	Normalization flag: 0 = no, 1 = yes
<b>RETURN:</b> int	The # of non-gap data points processed, or -1 if error
<b>REMARKS:</b> Only data between start and end analysis limits are converted. All zeros are treated as gaps in frequency data. The averaging time (tau) of the phase data will be the same as that of the frequency data. The original frequency data is unchanged. The do_norm flag determines whether or not the frequency data is normalized to zero mean before conversion to phase data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* frequency data array */ F_TYPE x[513];                                       /* phase data array */ F_TYPE tau;  /* averaging time */ int num;   /* # data points processed */ BOOL do_norm;                                       /* normalization flag */  . . do_norm=TRUE;                                       /* set flag to do normalization */ num=ConvFreqToPhase(y, x, tau, do_norm); /* convert freq to phase */ if(num==-1)   /* check for error */ {     printf("\nError");                               /* error message */ } else {     printf("\n# Data Points Converted = %d", num); /* display num */ } </pre>	
<b>SEE ALSO:</b> ConvPhaseToFreq()	

**REFERENCE:** None

## FrequenC Library Reference Manual

```

/*****
/*
/*          ConvFreqToPhase()
/*
/*          Function to convert frequency data to phase (time) data
/*
/*          Parameters:      F_TYPE y[]    = frequency data
/*                          y[0] = # data points
/*                          y[1] = analysis start
/*                          y[2] = analysis end
/*                          F_TYPE x[]    = phase data
/*                          F_TYPE tau   = time interval between freq samples
/*                          BOOL do_norm = normalization flag:
/*                                  0=don't normalize, 1=normalize
/*
/*          Return:         int           = # frequency data gaps,
/*                                  or -1 if error
/*
/*          Notes:          Calls FrequenC functions mean() and normalize().
/*                          Freq data normalized before conversion if do_norm
/*                          is TRUE. This option allows original freq data
/*                          to remain unnormalized. tau must be >0.
/*                          Zeros treated as gaps in frequency data.
/*                          Phase data in gap extrapolated from last previous
/*                          non-zero frequency value.
/*                          Function processes n = y[2] - y[1] +1 freq points
/*                          and produces n+1 phase points.
/*
/*          Revision record:
/*          08/28/02      Created from ConvFreqToPhase() of FrequenC library
/*          Changed code to preserve gap insted of linear
/*          integrated phase during gap
/*          08/30/02      Use average freq for gap interpolation
/*          03/08/03      Brought into Ver 2.0 of FrequenC lib
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL ConvFreqToPhase(F_TYPE y[],
F_TYPE x[], F_TYPE tau, BOOL do_norm)
{
    int g;                                /* # freq gaps */
    int i;                                /* y index */
    int j;                                /* x index */
    int num;                              /* # freq points */
    F_TYPE y_last;                        /* last non-zero freq value */
    F_TYPE y_avg;                         /* average freq value */
    F_TYPE xbar, *p_xbar;                 /* avg of x[] and pointer to it */

    if(tau<=0)
    {
        return(-1);                      /* error */
    }

    num = (int)(y[2]-y[1]+1);             /* set num = # freq points */
    x[0] = num;                           /* # phase points */

```

```

x[1] = 1;                                /* # of 1st phase point */
x[2] = num;                              /* # of last phase point */
p_xbar = &xbar;                          /* assign address to pointer */

/* put freq data to be converted into x[] array */
j=3;                                     /* initialize index for x[] */
for(i = (int)(y[1]+2); i <= (int)(y[2]+2); i++)
{
    x[j] = y[i];                         /* copy freq data */
    j++;                                 /* increment index */
}

// Find average frequency value
CalcMean(x, &y_avg, 1);                  /* calc avg freq */

if(do_norm)                             /* normalize frequency data to be converted */
{
    if((CalcMean( x, p_xbar, 1))== -1)    /* calc average frequency */
    {
        return(-1);                     /* pass along error */
    }
    if((NormalizeData( x, xbar, 1))==0)    /* normalize frequency data */
    {
        return(-1);                     /* pass along error */
    }
}                                         /* end if */

/* shift normalized frequency data up 1 position in x[] array */
for(i = num+2; i >= 3; i--)
{
    x[i+1] = x[i];
}

                                         /* add 1 to # of data points */
x[0]++;
x[2]++;
num++;

/* convert frequency data to phase data */
x[3] = 0;                               /* set 1st phase value to zero */
y_last = 0;                             /* ditto for y_last */
g=0;                                    /* initialize # gaps */
for(i = 4; i < num+3; i++)
{
    /* phase data goes from y[3] to y[num+2] */
    if( x[i] )                           /* freq point not a gap */
    {
        y_last = x[i];                   /* save current freq */
        x[i] = x[i-1] + ( x[i] * tau );
        /* x[i] is freq on RH side, converted to phase on LH side */
    }
    else                                  /* freq point is a gap */
    {
        // Avg freq gives better result for large gaps
        x[i] = x[i-1] + ( y_avg * tau );

        // Make phase value zero to preserve gap
        x[i-1]=0.0;

        g++;
    }
}                                         /* end else */

```

```
    }                                     /* end for */  
    return( g );  
}                                       /* end ConvFreqToPhase() */
```

The FrequenC Library	
<b>NAME:</b> CountGaps	<b>FUNCTION:</b> Count the number of gaps in phase or frequency phase data
<b>SYNOPSIS:</b> int CountGaps(F_TYPE z[], BOOL datatype)	
F_TYPE z[]	Phase or frequency data array: z[0] = # data points z[1] = analysis start point z[2] = analysis end point
BOOL datatype	Type of data: 0=phase, 1=frequency
<b>RETURN:</b> int	The # of gaps counted
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. All zeros are counted as gaps in frequency data. Only imbedded gaps are counted as gaps in phase data. The datatype flag determines whether the data is treated as phase or frequency data. The data is unchanged by the CountGaps() function. No error codes are returned from this function.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ BOOL datatype;                                       /* data type flag */ int num;   /* # gaps */ . . datatype=FREQ;                                       /* set flag for frequency data */ /* frequenc.h contains #define PHASE 0 and #define FREQ 1 */ num=CountGaps(z, datatype);                          /* count gaps in data */ printf("\n# Gaps = %d", num);                       /* display num */ </pre>	
<b>SEE ALSO:</b> FillGaps()	
<b>REFERENCE:</b> None	

## FrequenC Library Reference Manual

```

/*****
/*
/*          CountGaps()
/*
/*      Function counts the number of gaps in a phase or frequency
/*      data file.
/*
/*      Parameters:      F_TYPE z[]    = phase or frequency data array
/*                        z[0] = # data points
/*                        z[1] = analysis start
/*                        z[2] = analysis end
/*                        BOOL datatype = data type: 0=phase, 1=frequency
/*
/*      Return:          int            = # gaps in data
/*
/*      Note:            Gaps in data are indicated by zero values.
/*                        Leading and trailing zeros are not counted as
/*                        gaps in phase data.
/*
/*      Revision record:
/*          12/30/91      Created & edited
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CountGaps(F_TYPE z[], BOOL datatype)
{
    int i;                                /* array index */
    int count=0;                          /* # gaps */

    for(i=(int) (*z+1)+3-datatype; i<=(int) (*z+2)+1+datatype; i++)
        /* start at 1st and last data points for freq data, */
        /* 2nd and next to last for phase data */
        {
            if(!*(z+i))                  /* is data point a gap (zero)? */
            {
                count++;
            }
        }
        /* end if */
        /* end for */

    return(count);
}
/* end CountGaps() */

```

The FrequenC Library	
<b>NAME:</b> CalcGreenhallModSigma()	<b>FUNCTION:</b> Calc mod Allan variance for phase data using faster Greenhall algorithm
<b>SYNOPSIS:</b> int CalcGreenhallModSigma(F_TYPE x[], F_TYPE *sig, F_TYPE tau, int m)	
F_TYPE x[]	Phase data array x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE *sig	Pointer to mod Allan deviation, mod $\sigma_y(\tau)$
F_TYPE tau	Analysis averaging time = $\tau = m \cdot \tau_0$ , where $\tau_0$ is measurement interval of phase data
int m	Averaging factor, $m = \tau / \tau_0$
<b>RETURN:</b> int	# analysis points, or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. No gaps are allowed in phase data. Must have at least 3 phase data points. m must be >0, and cannot exceed (int)(n/3). tau must be >0.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[512];                                       /* phase data array */ F_TYPE sig;  /* mod sigma */ F_TYPE tau=1.0;                                     /* meas interval */ int m=100;  /* avg factor */ int num;   /* # analysis points */ . . num=CalcGreenhallModSigma(x, &amp;sig, tau, m);          /* call function */ printf("\nModSigma = %e", sig);                    /* display result */ </pre>	
<b>SEE ALSO:</b> CalcPhaseModSigma()	
<b>REFERENCE:</b> C.A. Greenhall, "A Shortcut for Computing the Modified Allan Variance", AFCS '92.	



The FrequenC Library	
<b>NAME:</b> CalcHadamardB1	<b>FUNCTION:</b> Description of what function does
<b>SYNOPSIS:</b> int FunctionName( F_TYPE z[], F_TYPE one, F_TYPE two)	
F_TYPE z[]	Phase or frequency data array z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE one	parameter one, and description of what it is
F_TYPE two	parameter two, and description of what it is
<b>RETURN:</b> int	# non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are modified. Embedded zeros are treated as gaps in phase data. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include &lt;frequenc.h&gt;                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ F_TYPE one;   /* parameter one */ F_TYPE two;   /* parameter two */ int num;   /* # data points processed */ . . one=1.0;   /* set 1st parameter value */ two=2.0;   /* set 2nd parameter value */ num=FunctionName(z, one, two);                     /* call function */ printf("\n# Data Points Scaled = %d", num);        /* display num */ </pre>	
<b>SEE ALSO:</b> RelatedFunctionName()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*                               CalcHadamardB1()
/*
/*  Function to calc the Hadamard B1 Bias Function BH1(N, 1, mu),
/*  the ratio of the standard to Hadamard variances as a function of
/*  N = # samples and integer mu = slope of log sigma vs log tau plot
/*  for r = 1 (no dead time). This function applies for integer mu =
/*  -1 thru 3 and N > 1. BH1 = 1 for N = 2 for any mu. This function
/*  can be used to ID power law noises from alpha = 0 to -4.
/*
/*
/*  Noise types handled:      Alpha    Mu    FM
/*                          -4         3    RR
/*                          -3         2    FW
/*                          -2         1    RW
/*                          -1         0    F
/*                          0         -1    W
/*
/*
/*  References:      (1) NBS Technical Note 375, J.A. Barnes, "Tables
/*                    of Bias Functions B1 and B2, for Variances
/*                    Based on Finite Samples of Processes with
/*                    Power Law Spectral Densities", January, 1969.
/*                    (2) NIST Technical Note 1318, J.A. Barnes and D.W.
/*                    Allan, "Variances Based on Data with Dead Time
/*                    Between the Measurements", 1990.
/*                    (3) NIST Technical Note 1337, TN-296 to TN-335,
/*                    J.A. Barnes and D.W. Allan, "Variances Based
/*                    on Data with Dead Time Between the
/*                    Measurements", 1990.
/*                    (4) J.A. Barnes, "The Analysis of Time and
/*                    Frequency Data", Austron, Inc, December, 1991.
/*                    (5) C.A Greenhall, "A Hadamard B1 Bias Function"
/*                    (private communication), 04/23/99.
/*
/*
/*  Parameters:      int num = # samples
/*                    Get -1 error code for n <2
/*                    int mu  = noise type
/*                    Get -1 error code for mu < -1 or mu > 3
/*
/*
/*  Return:          float    = B1 bias function value,
/*                    or -1 if error
/*
/*
/*  Revision record:
/*      04/24/99    Drafted & debugged
/*      04/26/03    Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1999-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

float __declspec(dllexport) FAR PASCAL CalcHadamardB1(int num, int mu)
{
    double n=(double)num;          // Double version of num
    double m=(double)mu;           // Double version of mu
    double b;                       // BH1 bias function
    double b1, b2, b3;              // Working variables

```

```

if(n<2)                                // Num must be at least 2
{
    return(-1.0);                      // Error code
}

switch(mu)                             // Switch according to mu
                                        // Different formulae are required for
                                        // mu = 0 & 2 to avoid singularities
{
    case -1:                           // White FM (alpha=0)
    case 1:                             // Random Walk FM (alpha=-2)
    case 3:                             // Random Run FM (alpha=-4)
    {
        b1=2*pow(1-(1/n), m+2);
        b2=2*pow(1+(1/n), m+2);
        b3=pow(n, m);
        b=b3*(4-b2-b1);
        b1=4/(n*n);
        b2=pow(2, m+3);
        b+=-8+b2+b1;
        b1=pow(3, m);
        b2=pow(2, m);
        b3=-15+24*b2-9*b1;
        b*=n/((n-1)*b3);
        break;
    }

    case 0:                             // Flicker FM (alpha=-1)
    {
        b1=1-(1/n);
        b2=1+(1/n);
        b=log(b1);
        b*=-2*b1*b1;
        b3=log(b2);
        b3*=-2*b2*b2;
        b+=b3;
        b-=4*log(n)/(n*n);
        b+=8*log(2);
        b1=24*log(2)-9*log(3);
        b*=n/((n-1)*b1);
        break;
    }

    case 2:                             // Flicker Walk FM (alpha=-3)
    {
        b1=1-(1/n);
        b2=1+(1/n);
        b=log(b1);
        b*=b1*b1*b1*b1;
        b3=log(b2);
        b3*=b2*b2*b2*b2;
        b+=b3;
        b*=-2*n*n;
        b-=4*log(n)/(n*n);
        b-=24*log(n);
        b+=32*log(2);
        b1=96*log(2)-81*log(3);
        b*=n/((n-1)*b1);
        break;
    }
}

```

```
default:                // Unallowed mu
{
    b=-1.0;              // Error code
    break;
}

return((float)b);        // Return valid value of BH1 bias function
}
```

The FrequenC Library	
<b>NAME:</b> CalcHadamardDev()	<b>FUNCTION:</b> Calculate Hadamard variance from phase data
<b>SYNOPSIS:</b> int CalcHadamardDev(F_TYPE x[], F_TYPE *dev, F_TYPE tau)	
F_TYPE x[]	Phase data array x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE *dev	Pointer to Hadamard deviation
F_TYPE tau	Averaging time
<b>RETURN:</b> int	# analysis points, or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. Embedded zeros treated as gaps in phase data. Must have at least 4 adjacent non-gap phase data points. Tau must be >0.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h" F_TYPE x[512]; F_TYPE dev; F_TYPE tau=1.0; int num; . . num=CalcHadamardDev(x, &amp;dev, tau); printf("\nHadamard Dev = %e", dev); </pre> <div style="float: right; text-align: right;"> <pre> /* FrequenC header file */ /* phase data array */ /* Hadamard dev */ /* avg time */ /* # analysis points */  /* call function */ /* display result */ </pre> </div>	
<b>SEE ALSO:</b> CalcFreqHadamardDev()	
<b>REFERENCE:</b> T. Walter, "A Multi-Variance Analysis in the Time Domain", Proc. 24th PTTI Meeting, Dec. 1992.	

```

/*****
/*
/*          CalcHadamardDev()
/*
/*          Function to calculate Hadamard variance from phase data
/*
/*          Parameters:      F_TYPE x[]      = phase data
/*                          x[0] = # data points
/*                          x[1] = analysis start
/*                          x[2] = analysis end
/*                          F_TYPE *p_dev = pointer to Hadamard deviation
/*                          F_TYPE tau    = time between phase measurements
/*
/*          Return:          int              = # analysis points,
/*                                          or -1 if error
/*
/*          Note:            Embedded zeros treated as gaps in phase data.
/*                          Must have at least 1 analysis point; this
/*                          requires at least 4 adjacent non-gap phase data
/*                          points.  Tau must be >0.
/*
/*          Reference:       T. Walter, "A Multi-Variance Analysis in the Time
/*                          Domain", Proc. 24th PTTI Meeting, Dec. 1992.
/*
/*          Revision record:
/*              11/10/92      Created from CPS.C
/*              02/03/96      Modified for use as Win 3.1 DLL
/*              01/01/98      Changes for MS VC++ compatibility & warnings
/*              04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1992-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcHadamardDev(F_TYPE x[],
F_TYPE *p_dev, F_TYPE tau)
{
    double sum;                /* summing variable to calc sigma */
    int i;                     /* index for summing */
    int num = 0;               /* # analysis points */

    if(tau<=0)
    {
        return(-1);           /* error */
    }

    for( i = (int)(*(x+1)+2), sum = 0; i < (int)(*(x+2)); i++)
        /* index goes from 1 to n-3 */
        /* for n data points from 1 to n; data starts at x[3] */
    {
        if( ( i==(x+1)+2 && *(x+i+1) && *(x+i+2) && *(x+i+3) )
            || ( *(x+i) && *(x+i+1) && *(x+i+2) && *(x+i+3) )
            || ( i==(x+2) && *(x+i) && *(x+i+1) && *(x+i+2) ) )
            /* skip if any imbedded phase data value is zero */
        {
            sum += SQR( *(x+i+3) - 3 * *(x+i+2) + 3 * *(x+i+1) - *(x+i) );
            num++;
        }
    }
    /* end if */
}

```

```

}                                                                 /* end for */

if(num>0)
{
    *p_dev = ( sqrt( sum / (6.0 * num * tau * tau )));
    return(num);          /* # analysis points */
}
else
{
    return(-1);           /* error */
}
}                         /* end CalcPhaseSigma() */

```



The FrequenC Library	
<b>NAME:</b> CalcInvChiSqr	<b>FUNCTION:</b> Calculate the chi square value that corresponds to a certain probability and number of degrees of freedom
<b>SYNOPSIS:</b> float CalcInvChiSqr(float p, float df)	
float p	Chi square probability, $p(X^2, df)$
float df	# of degrees of freedom, df
<b>RETURN:</b> float	The chi square value, $X^2$ , or -1 if error
<b>REMARKS:</b> This function uses an iterative process that is slow for very small values of p. It returns an error code (-1) for $p \leq 0.00001$ . The # degrees of freedom does not have to be an integer. This function defines $p(X^2, df)$ as the area under the upper tail of the chi square distribution from $X^2$ to $\infty$ . Depending on your usage, you may need to use (1-p) instead of p as defined here. CalcInvChiSqr() calls CalcChiSqrProb(), which uses CalcNormalProb().	
<b>EXAMPLE:</b> <pre> #include "frequenc.h" float p; float df; float x; . . p=0.95; df=10.0; x=CalcInvChiSqr(p, df); if(x==-1) {     printf("\nError"); } else {     printf("\nX<sup>2</sup> = %5.2f", x); } </pre>	
<pre> /* FrequenC header file */ /* chi square probability */ /* # degrees of freedom */ /* chi square value */  /* assign p value */ /* assign df value */ /* calc X<sup>2</sup>(p, df) */  /* error message */  /* display X<sup>2</sup> */ </pre>	
<b>SEE ALSO:</b> CalcChiSqrProb()	
<b>REFERENCE:</b> None	

```

/*****
/*
/*                                     CalcInvChiSqr()
/*
/*      Code to replace CalcInvChiSqr() of FrequenC32 library
/*
/*      1st function calculates closed-form approximation to inverse chi
/*      square for large # degrees of freedom (OK for df>10)
/*
/*      References: (1) C. Greenhall/JPL via e-mail 12/06/96
/*                  (2) Abramowitz & Stegun, Handbook of Mathematical
/*                  Functions, Sections 26.2.22 & 26.4.17
/*
/*      2nd function uses a WJR iterative process to calculate the
/*      value of chi squared associated with a given probability for
/*      a certain # of degrees of freedom.  Calls CalcChiSqrProb().
/*
/*      Parameters:      float p = chi squared probability value
/*                      float df = # of degrees of freedom (not necessarily
/*                      an integer)
/*
/*      Return:          float      = chi square value,
/*                      or -1 if error
/*
/*      Revision record:
/*          02/03/97      Adapted from CalcInvChiSqr() of FrequenC Library
/*          02/04/97      Added closed-form function for large df.  Faster,
/*                      and avoids possible convergence problems.
/*          02/05/97      Fixed problem with wrong tail for new large df calc
/*          05/16/00      Use NR routines to calc chi sqr probability
/*                      Fixes discontinuity in chi sqr vs. df
/*          04/13/02      Watch out when df<1 - can hang up
/*          03/08/03      Brought into Ver 2.0 of FrequenC lib
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1997-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

// Prototypes for Numerical Recipes functions used here - not exported
float gammln(float xx);
float gammf(float a, float x);
float gammq(float a, float x);
void gcf(float* gammcf, float a, float x, float* gln);
void gser(float* gamser, float a, float x, float* gln);

float __declspec(dllexport) FAR PASCAL CalcInvChiSqr(float p, float df)
{
    // Local variables
    double x;                // Chi-squared value
    double prob;             // Degrees of freedom
    double sign;             // Iteration control sign
    double div;              // Iteration control divisor

    // Closed-form variables
    double a0=2.30753;       // Coefficients from A&S 26.2.22
    double a1=0.27601;       // "
    double b1=0.99229;       // "

```

```

double b2=0.04481;          // "
double b;
double n;

double p1;
double s;
double t;
double y;

if(p<=0.00001)              /* check for small, zero or negative p */
{                             /* no/slow convergence for small p */
    return(-1.0);            /* error code */
}

// Use closed-form approximation for df > 100
if(df>100)
{
    // Use opposite tail of distribution
    p=1-p;

    // Calc approximation to inverse chi sqr for large df
    p1=min(p, 1-p);
    t=sqrt(-2.0*log(p1));      // A&S 26.2.22
    n=t-((a0+(a1*t))/(1+(t*(b1+(t*b2))))); // "
    b=2.0/(9.0*df);           // A&S 26.4.17

    if((p-0.5)<0) s=-1.0;      // Greenhall revision
    else if((p-0.5)>0) s=1.0;  // 1 function for
    else s=0.0;               // both tails

    y=1-b+(s*n*sqrt(b));       // A&S 26.4.17
    x=df*pow(y, 3.0);          // "

    return (float)x;
}

// Iterative solution for df<=100
x = df+(0.5-p)*df*0.5;         /* start value for chi squared */
prob=gammp(df/2, (float)(x/2));
prob=1-prob;

div = 0.1;

while(fabs((prob-p)/p)>0.0001)  /* accuracy criterion */
{
    if(prob-p>0)               /* save sign of error */
    {
        sign=1.0;
    }
    else
    {
        sign=-1.0;
    }
    x += df*(prob-p)/div;       /* iteration increment */
    if(x>0)                     /* make sure argument is + */
    {
        prob=gammp(df/2, (float)(x/2));
        prob=1-prob;
    }
}

```

```

        else                                /* otherwise restore it & reduce increment */
        {
            x -= df*(prob-p)/div;
            div*=2;
        }
        if(((prob-p)/sign)<0)                /* did sign of error reverse? */
        {
            div*=2;                          /* reduce increment if it did */
        }
    }
    return (float)x;
}

/*****
/*
/* Numerical Recipes Routines to Calculate Chi Square Probability
/*
/* Call with p=gammp(df/2, x/2);
/* where p=chi sqr prob, df=deg of freedom, x=chi sqr val
/*
/*
*****/

// Defines
#define ITMAX 100
#define EPS 3.0e-7

/*****
/*
/* gammln()
/*
*****/
float gammln(float xx)
{
    double x,tmp,ser;
    static double cof[6]={76.18009173,-86.50532033,24.01409822,
        -1.231739516,0.120858003e-2,-0.536382e-5};
    int j;

    x=xx-1.0;
    tmp=x+5.5;
    tmp -= (x+0.5)*log(tmp);
    ser=1.0;
    for(j=0;j<=5;j++)
    {
        x += 1.0;
        ser += cof[j]/x;
    }
    return (float) (-tmp+log(2.50662827465*ser));
}

/*****
/*
/* gammp()
/*
*****/
float gammp(float a, float x)
{
    float gamser,gammcf,gln;

```

```

    if(x < 0.0 || a <= 0.0)
    {
        // TRACE_STR("Invalid arguments in routine GAMMP");
    }
    if(x < (a+1.0))
    {
        gser(&gamser,a,x,&gln);
        return gamser;
    }
    else
    {
        gcf(&gammcf,a,x,&gln);
        return (float)(1.0-gammcf);
    }
}
/*****
/*
/*
/*          gammq()
/*
/*
/*****/
float gammq(float a, float x)
{
    float gamser,gammcf,gln;

    if(x < 0.0 || a <= 0.0)
    {
        // TRACE_STR("Invalid arguments in routine GAMMQ");
    }
    if(x < (a+1.0))
    {
        gser(&gamser,a,x,&gln);
        return (float)(1.0-gamser);
    }
    else
    {
        gcf(&gammcf,a,x,&gln);
        return gammcf;
    }
}
/*****
/*
/*
/*          gammcf()
/*
/*
/*****/
void gcf(float* gammcf, float a, float x, float* gln)
{
    int n;
    float gold=0.0,g,fac=1.0,b1=1.0;
    float b0=0.0,anf,ana,an,a1,a0=1.0;

    *gln=gammln(a);
    a1=x;
    for(n=1;n<=ITMAX;n++)
    {
        an=(float) n;
        ana=an-a;
        a0=(a1+a0*ana)*fac;
        b0=(b1+b0*ana)*fac;
        anf=an*fac;
        a1=x*a0+anf*a1;
    }
}

```

```

        b1=x*b0+anf*b1;
        if(a1)
        {
            fac=(float)1.0/a1;
            g=b1*fac;
            if(fabs((g-gold)/g) < EPS)
            {
                *gammcf=(float)exp(-x+a*log(x)-(*gln))*g;
                return;
            }
            gold=g;
        }
    }
}

/*****
/*
/*                                gser()                                */
/*
/*
/*****/
void gser(float* gamser, float a, float x, float* gln)
{
    int n;
    float sum,del,ap;

    *gln=gammln(a);
    if(x <= 0.0)
    {
        if(x < 0.0)
        {
            // TRACE_STR("x less than 0 in routine GSER");
        }
        *gamser=0.0;
        return;
    }
    else
    {
        ap=a;
        del=sum=(float)1.0/a;
        for(n=1;n<=ITMAX;n++)
        {
            ap += 1.0;
            del *= x/ap;
            sum += del;
            if(fabs(del) < fabs(sum)*EPS)
            {
                *gamser=sum*(float)exp(-x+a*log(x)-(*gln));
                return;
            }
        }
        return;
    }
}

```

The FrequenC Library	
<b>NAME:</b> CalcLinFreqDrift	<b>FUNCTION:</b> Calculate the linear drift for frequency data
<b>SYNOPSIS:</b> int CalcLinFreqDrift(F_TYPE y[],F_TYPE *p_a,F_TYPE *p_b,F_TYPE *p_v)	
F_TYPE y[]	Frequency data array: y[0] = # data points y[1] = analysis start point y[2] = analysis end point
F_TYPE *p_a	Pointer to intercept, a, of $y(t)=a+bt$ linear fit to the frequency drift
F_TYPE *p_b	Pointer to slope, b, of $y(t)=a+bt$ linear fit to the frequency data
F_TYPE *p_v	Pointer to variance, v, of linear fit to the frequency data
<b>RETURN:</b> int	The # of non-gap data points processed, or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. There must be at least 2 non-gap analysis points. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* frequency data array */ F_TYPE a;   /* intercept */ F_TYPE b;   /* slope */ F_TYPE v;   /* variance */ int num;   /* # data points processed */ . . num=CalcLinFreqDrift(y, &amp;a, &amp;b, &amp;v);                /* calc linear drift */ if(num== -1)  /* check for error */ {     printf("\nError");                               /* error message */ } else {     printf("\nIntercept = %e", a);                   /* display slope */     printf("\nSlope = %e", b);                       /* display intercept */     printf("\nVariance = %e, v);                     /* display variance */     printf("\n# Data Points Analyzed = %d", num);    /* display num */ } </pre>	
<b>SEE ALSO:</b> CalcLogFreqDrift()	
<b>REFERENCE:</b> None	

```

/*****
/*
/*          CalcLinFreqDrift()
/*
/*          Function to calculate linear frequency drift  $y(t)=a+bt$ 
/*
/*          Parameters:      F_TYPE y[]  = frequency data
/*                          y[0] = # data points
/*                          y[1] = analysis start
/*                          y[2] = analysis end
/*                          F_TYPE p_a  = pointer to y-intercept
/*                          F_TYPE p_b  = pointer to slope
/*                          F_TYPE p_v  = pointer to fit variance
/*
/*          Return:          int          = # analysis points,
/*                                      or -1 if error
/*
/*          Notes:           Zeros treated as gaps in frequency data
/*                          # non-gap data points must be at least 2
/*                          and at least 3 to calc finite fit variance
/*
/*          Revision record:
/*          12/16/91      Created
/*          12/26/91      Changed to int returning # non-gap data points
/*          12/31/91      Renamed
/*          01/16/92      Edited per FrequenC documentation
/*          01/18/92      Edited title block
/*          01/19/92      Added error traps
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved */
*/
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcLinFreqDrift(F_TYPE y[],
F_TYPE *p_a, F_TYPE *p_b, F_TYPE *p_v)
{
    int i;
    int num = (int) (*(y+2) - *(y+1) + 1);
    double sum_x = 0;
    double sum_y = 0;
    double sum_xx = 0;
    double sum_yy = 0;
    double sum_xy = 0;

    for( i = (int) (*(y+1)+2); i <= (int) (*(y+2)+2); i++)
    {
        if(*(y + i))
        {
            sum_x  += i-2;
            sum_y  += *(y + i);
            sum_xx += SQR ( (float) (i-2) );           /* must cast to float */
            sum_yy += SQR ( *(y + i) );
            sum_xy += (i-2) * *(y + i);
        }
    }
}
/* end if */

```

```

        else
        {
            num--;
        }
    }
    /* end else */
    /* end for */

    if(num<2)
    {
        return(-1);
    }
    /* error */

    *p_b = (sum_xy - ((sum_x) * (sum_y) / num));
    *p_b = *p_b / (sum_xx - ((sum_x) * (sum_x) / num));
    *p_a = ((sum_y) / num) - (*p_b * sum_x / num);
    *p_v = 0;
    /* fit variance 0 if only 2 points */

    if(num>=3)    /* need at least 3 analysis points to calc fit variance */
    {
        *p_v = sum_yy - (sum_y * sum_y / num);
        *p_v -= *p_b * *p_b * (sum_xx - (sum_x * sum_x / num));
        *p_v /= (num - 2);
    }

    return(num);
}
/* end CalcLinFreqDrift() */

```



The FrequenC Library	
<b>NAME:</b> CalcLogFreqDrift	<b>FUNCTION:</b> Calculate the log drift for frequency data
<b>SYNOPSIS:</b> <pre>int CalcLogFreqDrift(F_TYPE y[], F_TYPE *p_a, F_TYPE *p_b,                     F_TYPE *p_c, F_TYPE *p_v)</pre>	
F_TYPE y[]	Frequency data array: y[0] = # data points y[1] = analysis start point y[2] = analysis end point
F_TYPE *p_a	Pointer to multiplicative term, a, of $y(t) = a \cdot \ln(bt+1) + c$ log fit to frequency data
F_TYPE *p_b	Pointer to time term, b, of log fit
F_TYPE *p_c	Pointer to constant term, c, of log fit
F_TYPE *p_v	Pointer to fit variance, v, of log fit
<b>RETURN:</b> int	The # of non-gap data points processed, or -1 if error
<b>REMARKS:</b> All zeros are treayed as gaps in frequency data. Only data points between start and end analysis limits are analyzed. There must be at least 2 non-gap analysis points.	
<b>EXAMPLE:</b> <pre>#include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* frequency data array */ F_TYPE a, b, c, v;                                  /* fit parameters */ int num;   /* # data points processed */ . . num=CalcLogFreqDrift(y, &amp;a, &amp;b, &amp;c, &amp;v);              /* calc log drift */ if(num== -1)  /* check for error */ {     printf("\nError");                               /* error message */ } else {     printf("\na = %e", a);                            /* display a */     printf("\nb = %e", b);                            /* display b */     printf("\nc = %e", c);                            /* display c */     printf("\nv = %e", v);                            /* display v */     printf("\n# Data Points Analyzed = %d", num);     /* display num */ } </pre>	
<b>SEE ALSO:</b> CalcLinFreqDrift()	
<b>REFERENCE:</b> MIL-O-55310B, General Specification for Crystal Oscillators	

--

## FrequenC Library Reference Manual

```

/*****
/*
/*          CalcLogFreqDrift()
/*
/*          Function to calculate log frequency drift
/*          Fit fractional frequency data to log drift model:
/*           $y(t) = a \ln(bt+1) + c$ 
/*          where: y(t) = fractional frequency
/*          t      = time
/*          a      = multiplicative term
/*          b      = log time term
/*          c      = constant term
/*
/*          Reference:      MIL-O-55310B, General Specification for Crystal
/*                          Oscillators
/*
/*          Parameters:      F_TYPE y[] = frequency data
/*                          y[0] = # data points
/*                          y[1] = analysis start
/*                          y[2] = analysis end
/*                          F_TYPE *p_a = pointer to multiplicative term
/*                          F_TYPE *p_b = pointer to time constant term
/*                          F_TYPE *p_c = pointer to constant term
/*                          F_TYPE *p_v = pointer to fit variance
/*
/*          Return:          int          = # non-zero analysis points,
/*                                     or -1 if error
/*
/*          Notes:           Zeros treated as gaps in frequency data.
/*                          A value of b is chosen, the linear fit parameters
/*                          are found, and b is varied iteratively until the
/*                          rms error is below a limit criterion.
/*                          Need at least 2 non-zero data points.
/*
/*          Revision record:
/*          12/16/91      Created
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          01/19/92      Changed error trap
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcLogFreqDrift(F_TYPE y[],
F_TYPE *p_a, F_TYPE *p_b, F_TYPE *p_c, F_TYPE *p_v)
{
    int i;                                /* freq data index */
    int num = (int) (* (y+2) - * (y+1) + 1); /* # frequency data points */
    double error_limit = 0.00001;          /* fractional error limit for variance */
    double x;                             /*  $x = \ln(bt+1)$  */
    double err = 1.0;                      /* sum of squared error */
    double prev_err = 0; /* initialized so (err-prev_err)/err > error_limit */
    double sum_x;                          /* sum of  $x = \ln(bt+1)$  */
    double sum_y;                          /* sum of y */

```

```

double sum_xx;                                /* sum of x^2 */
double sum_xy;                                /* sum of xy */
double d=0.1;                                  /* b iteration factor */

*p_b=1.0;                                      /* initial value for b */

while(fabs(((err-prev_err)/err))>error_limit)    /* iterate */
{
    prev_err=err;                              /* save previous error */
    sum_x = 0;                                  /* sum of x=ln(bt+1) */
    sum_y = 0;                                  /* sum of y */
    sum_xx = 0;                                  /* sum of x^2 */
    sum_xy = 0;                                  /* sum of xy */
    num = (int) (* (y+2) - * (y+1) + 1);        /* # frequency data points */

    for( i=(int) (* (y+1) + 2); i<=(int) (* (y+2) + 2); i++)
                                                /* accumulate sums for fit */
    {
        if(* (y+i))                            /* gap in data? */
        {
            x=log(*p_b * (i-2))+1;
            sum_x += x;
            sum_y += * (y+i);
            sum_xx += x*x;
            sum_xy += x * * (y+i);
        }                                        /* end if */
        else
        {
            num--;
        }                                        /* end else */
    }                                           /* end for */

    if(num<2)                                  /* must have at least 2 data points */
    {
        return(-1);
    }                                           /* end if */

    *p_a = sum_xy - (sum_x * sum_y / num);      /* find parameters */
    *p_a /= sum_xx - (sum_x * sum_x / num);
    *p_c = (sum_y - (*p_a * sum_x)) / num;

    err=0;                                      /* calc sum of squared error */
    for( i=(int) (* (y+1) + 2); i<=(int) (* (y+2) + 2); i++)
    {
        if(* (y+i))
        {
            err += SQR(*p_a * log(*p_b * (i-2))+1) + *p_c - * (y+i));
        }
    }

    if(err>prev_err)                            /* wrong way? */
    {
        d *=-0.5;
    }
    *p_b += *p_b * d;                          /* modify b for next iteration */
}

*p_v = err;

return(num);

}                                              /* end CalcLogFreqDrift() */

```



The FrequenC Library	
<b>NAME:</b> CalcMean	<b>FUNCTION:</b> Calculate average value of phase or frequency data
<b>SYNOPSIS:</b> int CalcMean(F_TYPE z[], F_TYPE *p_avg, BOOL datatype)	
F_TYPE z[]	Phase or frequency data array: z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE *p_avg	Pointer to average
BOOL datatype	Type of data: 0=phase, 1=frequency
<b>RETURN:</b> int	The # of analysis points, or -1 if error
<b>REMARKS:</b> Only data between start and end analysis limits are analyzed. All zeros are treated as gaps in frequency data. Only embedded gaps are treated as gaps in phase data. The datatype flag determines whether the data is treated as phase or frequency data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ F_TYPE avg;  /* average value */ BOOL datatype;                                       /* data type flag */ int num;   /* # gaps */ . . datatype=FREQ;                                       /* set flag for frequency data */ /* frequenc.h contains #define PHASE 0 and #define FREQ 1 */ num=CalcMean(z, &amp;avg, datatype);                    /* calc avg */ if(num==-1)   /* check for error */ {     printf("\nError);                               /* error message */ } else {     printf("\nAverage = %e", avg);                  /* display average */     printf("\n# Analysis Points = %d", num);        /* display num */ }           </pre>	
<b>SEE ALSO:</b> NormalizeData()	
<b>REFERENCE:</b> None	

## FrequenC Library Reference Manual

```

/*****
/*
/*          CalcMean()
/*
/*      Function to calculate average value of phase or frequency data
/*
/*      Parameters:      F_TYPE z[]      = phase or frequency data
/*                        z[0] = # data points
/*                        z[1] = analysis start
/*                        z[2] = analysis end
/*
/*                        F_TYPE *p_avg = pointer to average value of data
/*                        BOOL datatype = data type: 0=phase, 1=frequency
/*
/*      Return:          int              = # non-gap data points,
/*                                      or -1 if error
/*
/*      Notes:           All zeros treated as gaps in frequency data.
/*                       Embedded zeros treated as gaps in phase data.
/*
/*      Revision record:
/*          12/16/91      Created
/*          12/24/91      Changed to make datatype a parameter rather than
/*                        a global variable. Made function an int return-
/*                        ing # non-gap data points. y[] changed to z[].
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          01/19/92      Added error trap
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcMean(F_TYPE z[], F_TYPE *p_avg,
        BOOL datatype)
{
    double sum = 0;
    float num = 0;
    int i;

    for( i=(int) (*(z+1)+2); i<=(int) (*(z+2)+2); i++)
        /* loop thru all analysis points */
        {
            /* skip gaps */
            if(*(z + i) || (!datatype && i==3) || (!datatype && i==z[0]+2))
            {
                sum += *(z+i);
                num++;
            }
            /* end if */
        }
        /* end for */
    if(num>0)
    {
        *p_avg = sum/num;
        return(int) num;
        /* return # non-gap data points */
    }
}

```

```
else
{
    return(-1);
}
/* error */
/* end CalcMean() */
```



The FrequenC Library	
<b>NAME:</b> CalcNormalProb	<b>FUNCTION:</b> Calculate the normal probability function
<b>SYNOPSIS:</b> float CalcNormalProb(float x)	
float x	The normal variable value
<b>RETURN:</b> float	The value of the normal probability, the area under the normal or Gaussian distribution to the left of the normal variable x.
<b>REMARKS:</b> No error codes are returned by this function	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ float p;  /* value of normal probability */ float x;  /* normal variable value */ . . x=1.5;  /* assign value to x */ p=CalcNormalProb(x);                               /* calc normal probability */ printf("\np = %5.3f", p);                          /* display p */ </pre>	
<b>SEE ALSO:</b> None	
<b>REFERENCE:</b> Collected Algorithms from CACM, Vol. I, #209	

## FrequenC Library Reference Manual

```

/*****
/*
/*          CalcNormalProb()
/*
/*      Function to calculate the cumulative normal distribution,
/*      the area under the normal or Gaussian distrubution to the
/*      left of the normal variable x.
/*
/*      Reference:      Collected Algorithms from CACM, Vol. I, #209,
/*                      D. Ibbetson and E. Brothers, 1963.
/*
/*      Parameter:      float x = normal variable
/*
/*      Return:         float    = p(x) = normal probability value
/*
/*      Revision record:
/*          12/30/91    Created
/*          12/31/91    Renamed
/*          01/18/92    Edited title block
/*          02/03/96    Modified for use as Win 3.1 DLL
/*          01/01/98    Changes for MS VC++ compatibility & warnings
/*          04/26/03    Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved */
*/
*****/

```

```
#include "frequenc.h"
```

```
float __declspec(dllexport) FAR PASCAL CalcNormalProb(float x)
```

```

{
    double w, y, z;

    if (x == 0.0)
    {
        z = 0.0;
    }
    else
    {
        y = fabs(x) / 2.0;
        if (y >= 3.0)
        {
            z = 1.0;
        }
        else
        {
            if (y < 1.0)
            {
                w = y * y;
                z = (((((((0.000124818987 * w
                - .001075204047) * w + .005198775019) * w
                - .019198292004) * w + .059054035642) * w
                - .151968751364) * w + .319152932694) * w
                - .531923007300) * w + .797884560593) * y * 2.0;
            }
            else
            {
                y = y - 2.0;
                z = ((((((((((((-.000045255659 * y

```

```

+.000152529290) * y - .000019538132) * y
-.000676904986) * y + .001390604284) * y
-.000794620820) * y - .002034254874) * y
+.006549791214) * y - .010557625006) * y
+.011630447319) * y - .009279453341) * y
+.005353579108) * y - .002141268741) * y
+.000535310849) * y + .999936657524;

    }
  }
}

if (x > 0.0)
{
    return (float)((z + 1.0) / 2.0);
}
else
{
    return (float)((1 - z) / 2.0);
}

/* end else */
/* end CalcNormProb() */
}

```



The FrequenC Library	
<b>NAME:</b> CalcPhaseHadamardDev	<b>FUNCTION:</b> Calculate Hadamard deviation from phase data
<b>SYNOPSIS:</b> int CalcPhaseHadamardDev(F_TYPE x[], F_TYPE *dev , F_TYPE tau)	
F_TYPE x[]	Phase data array x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE *dev	Pointer to Hadamard deviation
F_TYPE tau	Averaging time
<b>RETURN:</b> int	# non-gap data points processed or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. Embedded zeros are treated as gaps in phase data. Must have at least 4 adjacent non-gap phase data points. Tau must be > 0.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[512];                                       /* phase data array */ F_TYPE dev;  /* Hadamard deviation */ F_TYPE tau=1.0;                                     /* averaging time */ int num;   /* # data points processed */ . . num=CalcPhaseHadamardDev(x, &amp;dev, tau);             /* call function */ printf("\nHadamard Dev = %e", dev);                /* display result */ </pre>	
<b>SEE ALSO:</b> CalcFreqHadamardDev	
<b>REFERENCE:</b> T. Walter, "A Multi-Variance Analysis in the Time Domain", Proc. 24th PTTI Meeting, Dec. 1992.	

## FrequenC Library Reference Manual

```

/*****
/*
/*          CalcPhaseHadamardDev()
/*
/*      Function to calculate Hadamard variance from phase data
/*
/*      Parameters:      F_TYPE x[]      = phase data
/*                      x[0] = # data points
/*                      x[1] = analysis start
/*                      x[2] = analysis end
/*                      F_TYPE *p_dev = pointer to Hadamard deviation
/*                      F_TYPE tau    = time between phase measurements
/*
/*      Return:          int              = # analysis points,
/*                                      or -1 if error
/*
/*      Note:            Embedded zeros treated as gaps in phase data.
/*                      Must have at least 1 analysis point; this
/*                      requires at least 4 adjacent non-gap phase data
/*                      points.  Tau must be >0.
/*
/*      Reference:       T. Walter, "A Multi-Variance Analysis in the Time
/*                      Domain", Proc. 24th PTTI Meeting, Dec. 1992.
/*
/*      Revision record:
/*          04/26/96      Created from STAB_F45.C
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1996-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcPhaseHadamardDev(F_TYPE x[],
    F_TYPE *p_dev, F_TYPE tau)
{
    double sum;                /* summing variable to calc sigma */
    int i;                     /* index for summing */
    int num = 0;                /* # analysis points */

    if(tau<=0)
    {
        return(-1);            /* error */
    }

    for( i = (int)(*(x+1)+2), sum = 0; i < (int)(*(x+2)); i++)
        /* index goes from 1 to n-3 */
        /* for n data points from 1 to n; data starts at x[3] */
    {

```

```

if(      ( i==*(x+1)+2 && *(x+i+1) && *(x+i+2) && *(x+i+3) )
||      ( *(x+i)          && *(x+i+1) && *(x+i+2) && *(x+i+3) )
||      ( i==*(x+2)      && *(x+i)   && *(x+i+1) && *(x+i+2) ) )
        /* skip if any imbedded phase data value is zero */
{
    sum += SQR( *(x+i+3) - 3 * *(x+i+2) + 3 * *(x+i+1) - *(x+i) );
    num++;
}
/* end if */
/* end for */

if(num>0)
{
    *p_dev = ( sqrt( sum / (6.0 * num * tau * tau) ));
    return(num);
/* # analysis points */
/* end if */
}
else
/* no analysis points */
{
    return(-1);
/* error */
}
/* end else */
}

```



The FrequenC Library	
<b>NAME:</b> CalcPhaseModSigma	<b>FUNCTION:</b> Calculate the modified Allan deviation for phase data
<b>SYNOPSIS:</b> int CalcPhaseModSigma(F_TYPE x[], F_TYPE *p_sig, F_TYPE tau, int m)	
F_TYPE x[]	Phase data array: x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE *p_sig	Pointer to sig, the modified Allan deviation for the phase data
F_TYPE tau	The averaging time for the phase data
int m	The averaging factor
<b>RETURN:</b> int	the # of non-gap data points processed, or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. There must be at least 3 non-gap analysis points. Embedded zeros are treated as gaps in phase data. Maximum m = (int) num/3, and m must be >0. Tau must be >0.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[512];                                       /* phase data array */ F_TYPE sig;  /* modified sigma */ F_TYPE tau;  /* avergaing time */ int m;  /* averaging factor */ int num;   /* # data points processed */ . . tau=1.0;   /* set tau value */ m=2;  /* set m value */ num=CalcPhaseModSigma(x, &amp;sig, tau, m);          /* calc mod sigma */ if(num==-1)                                       /* check for error */ {     printf("\nError");                             /* error message */ } else {     printf("\nMod Sigma = %e", sig);              /* display sigma */     printf("\n# Data Points Analyzed = %d", num); /* display num */ }           </pre>	
<b>SEE ALSO:</b> CalcFastModSigma(), CalcFreqModSigma()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*          CalcPhaseModSigma()
/*
/*      Function to calculate the modified Allan variance for phase data,
/*      possibly with gaps.  A faster function, CalcFastModSigma(), can
/*      be used if there are no gaps.
/*
/*      Parameters:      F_TYPE x[]      = phase data
/*                      x[0] = # data phase points
/*                      x[1] = analysis start
/*                      x[2] = analysis end
/*                      F_TYPE *p_sig    = pointer to mod Allan deviation
/*                      F_TYPE tau       = analysis averaging time = m*tau_0
/*                      int m            = averaging factor = tau/tau_0
/*                      BOOL *bAbort     = pointer to abort flag
/*                      BOOL bProgress   = progress indicator flag
/*                      void *ProgressFunction()
/*                      = pointer to progress indicator
/*                      function with args int nPercentDone
/*                      and char *szMessage
/*
/*      Return:          int              = # analysis points,
/*                                      or -1 if error
/*
/*      Notes:           Embedded zero phase value treated as gap in data
/*                       Phase data is not averaged before calling this
/*                       function.  The data consists of num phase samples
/*                       at interval tau_0.  Denominator term (num-3m+1)
/*                       must be >0.  This sets max m=(int) (num/3),
/*                       where num=# phase points before averaging.
/*                       m must be >0 and tau must be >0.
/*                       Use faster CalcFastModSigma() if no gaps in data.
/*
/*                       The progress function pointer can be NULL, but is
/*                       intended as a way to display the % done and a
/*                       message about the calculation.
/*
/*                       The abort flag provides a way to abort the calc.
/*                       It must exist but does not have to be used.
/*
/*      Revision record:
/*          12/16/90      Created
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          01/19/92      Added error traps
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          06/15/02      Copied here for revision.  Added gap flag.
/*                       Fixed error for small AF and large sets of low
/*                       resolution noise where sum_i can be zero w/o gap
/*          01/28/03      Added progress indicator & argument
/*          03/08/03      Brought into Ver 2.0 of FrequenC lib
/*                       Added progress message function pointer to arg list
/*          03/09/03      Added bAbort pointer to arg list
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/*      (c) Copyright 1990-2003 Hamilton Technical Services  All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"

int __declspec(dllexport) FAR PASCAL CalcPhaseModSigma(F_TYPE x[],
    F_TYPE *p_sig, F_TYPE tau, int m, BOOL *bAbort, BOOL bProgress,
    void *ProgressFunction(int nPercentDone, char *szMessage))
{
    // Local variables
    double sum_i, sum_j;          /* summing variables to calc mod sigma */
    float fm;                     /* float version of m */
    int i;                        /* index for inner summing loop */
    int j;                        /* index for outer summing loop */
    int n_sum=0;                  /* # points in outer summing loop */
    int num = (int) (* (x+2) - * (x+1) + 1); /* # phase data points for analysis */
    int gap;                      /* gap flag */
    int nTic;                     /* Increment for progress indicator */
    int nLast_j=0;               /* Previous value of index */

    // Check args
    if( (m<1) || (num<3*m) || (tau<=0) )
    {
        return(-1);              /* error */
    }                             /* end if */

    // Initialize increment for progress report
    nTic=(int) ceil(num/100);

    // Start
    if(bProgress)
    {
        // Initialize progress display
        ProgressFunction(0,
            "Calculating Mod/Time Sigma (with gaps)");
    }                             /* end if */

    // Initialize outer loop
    fm=(float)m;
    sum_j=0;

    // Calc mod sigma
    for(j=1; j<=num-(3*m)+1; j++) /* outer loop */
        /* j goes from 1 to N-3m+1 where N=# phase points & m=avg factor */
        /* regardless of analysis limits */
    {
        sum_i=0;
        gap=1;
        for(i=j+(int) (* (x+1)) - 1; i<=m+j-1+(* (x+1)) - 1; i++) /* inner loop */
            /* i is the actual phase data index; it includes a term */
            /* * (x+1) - 1 to account for the analysis starting point */
            /* the data array offset +2 is included in the code below */
        {
            if( ( i==j+(* (x+1)) - 1 && * (x+i+2+m) && * (x+i+2+(2*m)) )
                || ( * (x+i+2) && * (x+i+2+m) && * (x+i+2+(2*m)) )
                || ( i==m+j-1+(* (x+1)) - 1 && * (x+i+2+m) && * (x+i) ) )
                /* skip if any imbedded phase data value is zero */
            {
                sum_i += * (x+i+2+(2*m)) - (2*(* (x+i+2+m))) + * (x+i+2);
                gap=0;             /* not a gap */
            }                     /* end if */
        }                         /* end for */
    }                             /* end for */
}
```

```

if(!gap)
{
    sum_j += SQR(sum_i);
    n_sum++;
}

/* end if */

// Display progress
// Update when index has changed by at least tic amount
if(((j-nLast_j)>=nTic) && (bProgress))
{
    ProgressFunction((int) (0.5+100.0*j/(num-3*m)),
        "Calculating Mod/Time Sigma (with gaps)");
    nLast_j=j;
}

/* end if */

// Check for abort
if(*bAbort)
{
    break;
}

/* end for */

// Done

// Clear progress display
ProgressFunction(0, "");

// Return results
if(n_sum>0)
{
    *p_sig = sqrt((sum_j)/(2.0*tau*tau*fm*fm*n_sum));
    return(n_sum);
}
else
{
    return(-1);
}

/* end CalcPhaseModSigma() */
}

```

The FrequenC Library	
<b>NAME:</b> CalcPhaseOverlap HadamardDev	<b>FUNCTION:</b> Description of what function does
<b>SYNOPSIS:</b> int FunctionName( F_TYPE z[], F_TYPE one, F_TYPE two)	
F_TYPE z[]	Phase or frequency data array z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE one	parameter one, and description of what it is
F_TYPE two	parameter two, and description of what it is
<b>RETURN:</b> int	# non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are modified. Embedded zeros are treated as gaps in phase data. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include &lt;frequenc.h&gt;                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ F_TYPE one;   /* parameter one */ F_TYPE two;   /* parameter two */ int num;   /* # data points processed */ . . one=1.0;   /* set 1st parameter value */ two=2.0;   /* set 2nd parameter value */ num=FunctionName(z, one, two);                     /* call function */ printf("\n# Data Points Scaled = %d", num);        /* display num */ </pre>	
<b>SEE ALSO:</b> RelatedFunctionName()	
<b>REFERENCE:</b> NIST Technical Note 1337	

## FrequenC Library Reference Manual

```

/*****
/*
/*          CalcPhaseOverlapHadamardDev()
/*
/*      Function to calc overlapping Hadamard variance from phase data
/*
/*      Parameters:      F_TYPE x[]      = phase data
/*                          x[0] = # data points
/*                          x[1] = analysis start
/*                          x[2] = analysis end
/*
/*                          F_TYPE *p_dev = pointer to Hadamard deviation
/*                          F_TYPE tau    = time between phase measurements
/*                          int    m      = averaging factor
/*
/*      Return:          int              = # analysis points,
/*                                      or -1 if error
/*
/*      Note:            Embedded zeros treated as gaps in phase data.
/*                        Must have at least 1 analysis point; this
/*                        requires at least 4 adjacent non-gap phase data
/*                        points.  Tau must be >0.
/*
/*      Reference:       T. Walter, "A Multi-Variance Analysis in the Time
/*                        Domain", Proc. 24th PTTI Meeting, Dec. 1992.
/*                        Modified by WJR to use fully-overlapping samples.
/*
/*      Revision record:
/*          03/05/99      Created from CPHD.C of FrequenC32 Library
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1999-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcPhaseOverlapHadamardDev(F_TYPE x[],
    F_TYPE *p_dev, F_TYPE tau, int m)
{
    double sum;                /* summing variable to calc sigma */
    int i;                    /* index for summing */
    int num=0;                /* # analysis points */
    float fm=(float)m;        /* float version of m */

    if(tau<=0)
    {
        return(-1);          /* error */
    }

    for(i=(int) (*(x+1)+2), sum=0; i<=(int) (*(x+2)+2-3*m); i++)
        /* index goes from 1 to n-3m */
        /* for n data points from 1 to n; data starts at x[3] */
    {

```

```

if(      ( i==*(x+1)+2 && *(x+i+m) && *(x+i+2*m) && *(x+i+3*m) )
||      ( *(x+i)      && *(x+i+m) && *(x+i+2*m) && *(x+i+3*m) )
||      ( i==*(x+2)   && *(x+i)   && *(x+i+m) && *(x+i+2*m) ) )
        /* skip if any imbedded phase data value is zero */
{
    sum+=SQRT( (*(x+i+(3*m)))-3*( *(x+i+(2*m)))+3*( *(x+i+m))-*(x+i) );
    num++;
}
/* end if */
/* end for */

if(num>0)
{
    *p_dev=sqrt(sum/(6.0*num*tau*tau*fm*fm));
    return(num);
}
/* # analysis points */
/* end if */
else
/* no analysis points */
{
    return(-1);
}
/* error */
/* end else */
}

```



The FrequenC Library	
<b>NAME:</b> CalcPhaseOverlapSigma	<b>FUNCTION:</b> Calculate the Allan deviation for overlapping samples of phase data
<b>SYNOPSIS:</b> int CalcPhaseOverlapSigma(F_TYPE x[],F_TYPE *p_sig,F_TYPE tau,int m)	
F_TYPE x[]	Phase data array: x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE *p_sig	Pointer to sig, the Allan deviation for overlapping samples of phase data
F_TYPE tau	The averaging time for the phase data
int m	The averaging factor
<b>RETURN:</b> int	the # of non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. There must be at least 3 non-gap analysis points. Embedded zeros are treated as gaps in phase data. Avg Factor m must be >0 and < # data points/2. Tau must be >0.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[512];                                       /* phase data array */ F_TYPE sig;  /* sigma */ F_TYPE tau;  /* averaging time */ int m;  /* averaging factor */ int num;   /* # data points processed */ . . tau=1.0;   /* set tau value */ m=2;  /* set m value */ num=CalcPhaseOverlapSigma(x, &amp;sig, tau, m);       /* calc sigma */ if(num== -1)                                       /* check for error */ {     printf("\nError");                             /* error message */ } else {     printf("\nSigma = %e", sig);                   /* display sigma */     printf("\n# Data Points Analyzed = %d", num); /* display num */ } </pre>	
<b>SEE ALSO:</b> CalcPhaseSigma(), CalcFreqOverlapSigma()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*          CalcPhaseOverlapSigma()
/*
/*      Function to calculate Allan variance using overlapping samples
/*      of phase data
/*
/*      Parameters:      F_TYPE x[]      = phase data array
/*                        x[0] = # phase data points
/*                        x[1] = analysis start
/*                        x[2] = analysis end
/*
/*                        F_TYPE *p_sig = pointer to Allan deviation
/*                        F_TYPE tau    = averaging time of phase data
/*                        int m         = averaging factor
/*
/*      Return:          int              = # analysis points,
/*                                      or -1 if error
/*
/*      Notes:           Embedded zeros treated as gaps in phase data.
/*                       Must have at least 1 analysis point; this
/*                       requires at least 3 adjacent non-gap phase data
/*                       points. Averaging time for sigma calculation is
/*                       m times the tau parameter of the phase data.
/*                       m must be >0 , tau must be >0, and the # non-gap
/*                       phase data points N must be > 2m.
/*
/*      Revision record:
/*          12/16/90      Created
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          01/19/92      Added error traps
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1990-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) CalcPhaseOverlapSigma(F_TYPE x[], F_TYPE *p_sig,
F_TYPE tau, int m)
{
    double sum=0;                /* summing variable to calc sigma */
    float fm=m;                  /* float version of m */
    int i;                       /* index for summation */
    int num=0;                   /* # analysis points */
    int n;                       /* # frequency data points */

    n=(x+2)-(x+1)+1;             /* total # phase data points */

    if( (m<1) || (n<2*m) || (tau<=0) )
    {
        return(-1);              /* error */
    }
}

```

```

for( i=*(x+1)+2; i<=n-2*m+2; i++)                                /* summing loop */
/* i basically goes from 1 to N-2m where N is # phase data points and */
/* m is averaging factor. Term *(x+1) is the analysis start limit (1 */
/* if all data used) & the 2 accounts for the data array offset      */
{
    if( ( i==*(x+1)+2 && *(x+i+m) && *(x+i+(2*m)) )
        || ( *(x+i) && *(x+i+m) && *(x+i+(2*m)) )
        || ( i==n-2*m+2 && *(x+i+m) && *(x+i) ) )
        /* skip if any imbedded phase data value is zero */
    {
        sum += SQR ( *(x+i+(2*m)) - (2 * (*(x+i+m))) + *(x+i) );
        num++;
    }
    /* end if */
}
if(num>0)
{
    *p_sig=sqrt( sum / (2.0*tau*tau*fm*fm*num));
    return(num);
    /* # analysis points */
}
else
{
    return(-1);
    /* error */
}
/* end CalcPhaseOverlapSigma() */

```



The FrequenC Library	
<b>NAME:</b> CalcPhaseSigma	<b>FUNCTION:</b> Calculate Allan deviation for phase data
<b>SYNOPSIS:</b> int CalcPhaseSigma(F_TYPE x[], F_TYPE *p_sig, F_TYPE tau)	
F_TYPE x[]	Phase data array: x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE *p_sig	Pointer to sig, the Allan deviation for the phase data
F_TYPE tau	The averaging time for the phase data
<b>RETURN:</b> int	the # of non-gap data points processed, or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. There must be at least 3 non-gap analysis points. Embedded zeros are treated as gaps in phase data. Tau must be >0.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[512];                                       /* phase data array */ F_TYPE sig;  /* Allan deviation */ F_TYPE tau;  /* averaging time */ int num;   /* # data points processed */ . . tau=1.0;   /* set tau value */ num=CalcPhaseSigma(x, &amp;sig, tau);                  /* calc sigma */ if(num==-1)  /* check for error */ {     printf("\nError");                             /* error message */ } else {     printf("\nSigma = %e", sig);                    /* display sigma */     printf("\n# Data Points Analyzed = %d", num);   /* display num */ } </pre>	
<b>SEE ALSO:</b> CalcFreqSigma()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*          CalcPhaseSigma()
/*
/*      Function to calculate Allan variance from phase data
/*
/*      Parameters:      F_TYPE x[]      = phase data
/*                      x[0] = # data points
/*                      x[1] = analysis start
/*                      x[2] = analysis end
/*                      F_TYPE *p_sig = pointer to Allan deviation
/*                      F_TYPE tau    = time between phase measurements
/*
/*      Return:          int              = # analysis points,
/*                                      or -1 if error
/*
/*      Note:            Embedded zeros treated as gaps in phase data.
/*                      Must have at least 1 analysis point; this
/*                      requires at least 3 adjacent non-gap phase data
/*                      points.  Tau must be >0.
/*
/*      Revision record:
/*          12/16/91      Created
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*                      Added error traps
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __cdeclspec(dllexport) FAR PASCAL CalcPhaseSigma(F_TYPE x[],
    F_TYPE *p_sig, F_TYPE tau)

{
    double sum;                /* summing variable to calc sigma */
    int i;                    /* index for summing */
    int num = 0;                /* # analysis points */

    if(tau<=0)
    {
        return(-1);            /* error */
    }

    for( i = (int) (*(x+1)+2), sum = 0; i < (int) (*(x+2)+1); i++)
        /* index goes from 1 to n-2 */
        /* for n data points from 1 to n; data starts at x[3] */
    {

```

```

if(      ( i==*(x+1)+2 && *(x+i+1) && *(x+i+2) )
||      ( *(x+i)          && *(x+i+1) && *(x+i+2) )
||      ( i==*(x+2)+1 && *(x+i)   && *(x+i+1) ) )
        /* skip if any imbedded phase data value is zero */
{
    sum += SQR( *(x+i+2) - 2 * *(x+i+1) + *(x+i) );
    num++;
}
/* end if */
}
/* end for */
if(num>0)
{
    *p_sig = ( sqrt( sum / (2.0 * num * tau * tau) ));
    return(num);
/* # analysis points */
}
else
{
    return(-1);
/* error */
}
/* end CalcPhaseSigma() */
}

```



The FrequenC Library	
<b>NAME:</b> CalcPhaseStdDev	<b>FUNCTION:</b> Calculate standard deviation for phase data
<b>SYNOPSIS:</b> int CalcPhaseStdDev(F_TYPE x[], F_TYPE *p_dev, F_TYPE tau)	
F_TYPE x[]	Phase data array: x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE *p_dev	Pointer to dev, the standard deviation for the phase data
<b>RETURN:</b> int	The # of non-gap data points processed, or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. There must be at least 3 non-gap analysis points. Embedded zeros are treated as gaps in phase data. Tau must be >0.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[513];                                       /* phase data array */ F_TYPE dev;  /* standard deviation */ F_TYPE tau;  /* averaging time of phase data */ int num;   /* # data points processed */ . . tau=1.0;   /* assign value to tau */ num=CalcPhaseSigma(x, &amp;dev, tau);                  /* calc std dev */ if(num==-1)   /* check for error */ {     printf("\nError");                             /* error message */ } else {     printf("\nStd Dev = %e", dev);                  /* display std dev */     printf("\n# Data Points Analyzed = %d", num);   /* display num */ }           </pre>	
<b>SEE ALSO:</b> CalcFreqStdDev()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*          CalcPhaseStdDev()
/*
/*      Function to calculate standard deviation from phase data
/*
/*      Parameters:      F_TYPE x[]      = phase data
/*                      x[0] = # data points
/*                      x[1] = analysis start
/*                      x[2] = analysis end
/*                      F_TYPE *p_dev = pointer to standard deviation
/*                      F_TYPE tau    = time interval between data points
/*
/*      Return:          int              = # analysis points,
/*                                      or -1 if error
/*
/*      Note:            Embedded zeros treated as gaps in phase data.
/*                      Must have at least 3 non-gap phase data points,
/*                      and tau must be >0.
/*
/*      Revision record:
/*          12/16/90      Created
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          06/05/95      Corrected num per standard_dev() function of
/*                      STABLE. S/B # frequency (not phase) data points.
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          05/15/00      Added New to function name & put into Stable_r.c
/*                      to fix long-standing error
/*          03/08/03      Brought into Ver 2.0 of FrequenC lib
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1990-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcPhaseStdDev(F_TYPE x[], F_TYPE *p_dev,
F_TYPE tau)
{
    double sum=0;                                /* summing variable */
    double avg;                                  /* mean value of freq data */
    int i;                                       /* index for summing */
    int num = (int) (* (x+2) - * (x+1));        /* # freq analysis points */

    if (tau <= 0)
    {
        return(-1);                                /* error */
    }

    for (i = (int) (* (x+1) + 2); i <= (int) (* (x+2) + 1); i++) /* calc average freq */
    {

```

```

if(    ( *(x+i)          && *(x+i+1) )
    || ( i == *(x+1)+2 && *(x+i+1) )
    || ( i == *(x+2)+1 && *(x+i)   ) )
    /* if don't have an embedded zero data point */
    {
        sum += *(x+i+1) - *(x+i);          /* freq is 1st diff of phase */
    }

else
    {
        num--;
    }
}

if((num-2)>0)                                /* check for <3 non-gap data points */
{
    avg = sum/num;
}
else
{
    return(-1);                             /* error */
}

sum=0;
for(i=(int) (*(x+1)+2); i<=(int) (*(x+2)+1); i++)    /* calc variance */
{
    if(    ( *(x+i)          && *(x+i+1) )                /* skip if */
        || ( i == *(x+1)+2 && *(x+i+1) )                /* non-imbedded zero */
        || ( i == *(x+2)+1 && *(x+i)   ) )
    {
        sum += SQR( ( *(x+i+1) - *(x+i) ) - avg );
    }
    /* end if */
}
/* end for */

*p_dev = sqrt(sum/((num-1)*tau*tau));

return(num);                                /* # non-zero data points */
/* end CalcPhaseStdDev() */
}

```



The FrequenC Library	
<b>NAME:</b> ConvPhaseToFreq	<b>FUNCTION:</b> Convert phase data to frequency data
<b>SYNOPSIS:</b> int ConvPhaseToFreq(F_TYPE x[], F_TYPE y[], F_TYPE tau)	
F_TYPE x[]	Phase data array: x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE y[]	Frequency data array: y[0] = # data points y[1] = analysis start point y[2] = analysis end point
F_TYPE tau	Averaging time of phase data
<b>RETURN:</b> int	The # of non-gap data points processed, or -1 if error
<b>REMARKS:</b> Only phase data between start and end analysis limits are converted. Embedded zeros are treated as gaps in phase data. Tau must be >0. The averaging time (tau) of the frequency data will be the same as that of the phase data. The original phase data is unchanged.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[513];                                       /* phase data array */ F_TYPE y[512];                                       /* frequency data array */ F_TYPE tau;  /* averaging time */ int num;   /* # data points processed */ . . tau=1.0;   /* assign value to tau */ num=ConvPhaseToFreq(x, y, tau);                     /* convert phase to freq */ if(num==-1)   /* check for error */ {     printf("\nError");                               /* error message */ } else {     printf("\n# Data Points Converted = %d", num); /* display num */ } </pre>	
<b>SEE ALSO:</b> ConvFreqToPhase()	
<b>REFERENCE:</b> None	

```

/*****
/*
/*          ConvPhaseToFreq()
/*
/*      Enhanced function to convert phase (time) data to frequency data
/*
/*      Parameters:      F_TYPE x[]  = phase data
/*                      x[0] = # phase data points
/*                      x[1] = analysis start
/*                      x[2] = analysis end
/*                      F_TYPE y[]  = frequency data
/*                      F_TYPE tau  = time interval between phase samples
/*                      BOOL z      = flag to avoid zero freq
/*
/*      Return:          int          = # frequency data gaps,
/*                                or -1 if error
/*
/*      Notes:           Embedded zeros treated as gaps in phase data.
/*                       Frequency data in gaps interpolated from nearest
/*                       non-gap phase values.  Function processes n =
/*                       x[2] - x[1] +1 phase points and produces n-1
/*                       frequency points.  tau must be >0.
/*
/*      Revision record:
/*          12/27/91      Created
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          01/19/92      Added error trap
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          05/22/01      Added flag for avoiding gaps if zero freq
/*          03/08/03      Brought into Ver 2.0 of FrequenC lib
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL ConvPhaseToFreq(F_TYPE x[], F_TYPE y[],
F_TYPE tau, BOOL z)
{
    int g;                                /* # phase gaps */
    int i;                                /* x index */
    int j;                                /* y index */
    int num;                              /* # phase points */

    if(tau<=0)
    {
        return(-1);                      /* error */
    }

    num=(int) (x[2]-x[1]+1);              /* set num = # phase points */
    y[0]=num-1;                          /* # freq points */
    y[1]=1;                              /* # of 1st freq point */
    y[2]=num-1;                          /* # of last freq point */

    /* put phase data to be converted into y[] array */
    j=3;                                  /* initialize index for y[] */

```

```

for(i=(int) (x[1]+2); i<=(int) (x[2]+2); i++ )

{
    y[j]=x[i];                                /* copy phase data */
    j++;                                       /* increment index */
}

/* convert phase data to freq data */
g=0;                                         /* initialize # gaps */
for(i=3; i<=num+2; i++)
{
    if( (y[i] && y[i+1]) || (i==3 && y[i+1]) || (y[i] && i==num+2) )
        /* neither phase point a gap, or 1st point with non-zero 2nd point, */
        /* or last point with non-zero next-to-last point */
        {
            y[i]=(y[i+1]-y[i])/tau;

            /* avoid zero freq = gap */
            if(!y[i] && z)
            {
                y[i]=1e-99;
            }
        }
        /* end if */
    else
        /* imbedded gap */
        {
            y[i]=0;
            g++;
        }
        /* end else */
}
/* end for */

return(g);

/* end ConvPhaseToFreq() */
}

```



The FrequenC Library	
<b>NAME:</b> CalcQuadraticDrift	<b>FUNCTION:</b> Calculate the least-squares quadratic fit for phase data
<b>SYNOPSIS:</b> <pre>int CalcQuadraticDrift(F_TYPE x[], F_TYPE tau, F_TYPE *p_a,                       F_TYPE *p_b, F_TYPE *p_c, F_TYPE *p_v)</pre>	
F_TYPE x[]	Phase data array: x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE tau	Averaging time for phase data
F_TYPE *p_a	Pointer to constant term, a, of quadratic fit $x(t)=a+bt+ct^2$ , $y(t)=b+2ct$ , freq drift=2c
F_TYPE *p_b	Pointer to linear term, b, of quadratic fit
F_TYPE *p_c	Pointer to quadratic term, c, of fit
F_TYPE *p_v	Pointer to fit variance, v
<b>RETURN:</b> int	The # of non-gap data points processed, or -1 if error
<b>REMARKS:</b> Embedded zeros are treated as gaps in phase data. Gaps are filled during analysis and restored thereafter. Only data points between start and end analysis limits are analyzed. There must be at least 3 non-gap analysis points. Tau must be >0.	
<b>EXAMPLE:</b> <pre>#include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[513];                                       /* phase data array */ F_TYPE a, b, c, v;                                  /* fit parameters */ F_TYPE tau;  /* averaging time */ int num;   /* # data points processed */  . . num=CalcQuadraticDrift(y, &amp;a, &amp;b, &amp;c, &amp;v);           /* calc quad fit */ if(num==-1) {     printf("\nError");                               /* error message */ } else {     printf("\na = %e, b = %e, c = %e", a,b,c);        /* disp fit params */     printf("\nv = %e", v);                            /* display fit variance */     printf("\n# Data Points Analyzed = %d", num);     /* display num */ } </pre>	
<b>SEE ALSO:</b> CalcLinFreqDrift()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*          CalcQuadraticDrift()
/*
/*
/*      Function to calculate least-squares quadratic fit to phase data
/*       $x(t) = a + bt + ct^2$ 
/*
/*
/*      Reference:      J.A. Barnes, "The Measurement of Linear Frequency
/*                      Drift in Oscillators", Proc. 15th Annual PTTI
/*                      Meeting, 1983, pp. 551-582.
/*
/*
/*      Parameters:      F_TYPE x[]  = phase data array
/*                      x[0] = # phase data points
/*                      x[1] = analysis start
/*                      x[2] = analysis end
/*                      F_TYPE tau   = time interval for phase data
/*                      F_TYPE *p_a  = pointer to phase intercept
/*                      F_TYPE *p_b  = pointer to frequency intercept
/*                      F_TYPE *p_c  = pointer to frequency slope
/*                      F_TYPE *p_v  = pointer to fit variance
/*
/*
/*      Return:          int          = # analysis points
/*                              or -1 if error
/*
/*
/*      Notes:           x(t) , t & a in sec, b in sec/sec, c in sec/sec2.
/*                      Frequency drift (slope) = 2c; intercept = b.
/*                      t is time interval of equally-spaced phase data.
/*                      t goes from 1 to n with no missing points.
/*                      Calls FrequenC functions CountGaps() and
/*                      FillGaps() as needed. To preserve gaps, save
/*                      data before calling this function.
/*
/*
/*      Revision record:
/*          12/29/91    Created
/*          12/31/91    Renamed
/*          01/18/92    Edited title block
/*          01/19/92    Added error traps
/*          01/22/92    Added error trap for tau<=0
/*          11/04/92    Changed gap handling -- was NG
/*          02/03/96    Modified for use as Win 3.1 DLL
/*          04/26/03    Adapted for Version 2.0 source code documentation
/*
/*      (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

#include "frequenc.h"                                /* FrequenC header file */

int F_declspec(dllexport) CalcQuadraticDrift(F_TYPE x[], F_TYPE tau,
      F_TYPE *p_a, F_TYPE *p_b, F_TYPE *p_c, F_TYPE *p_v)
{
    double aa,bb,cc,dd,ee,ff,gg;                    /* fit terms */
    double sx,sxx,snx,snnx;                          /* summations */
    int n=x[2]-x[1]+1;                                /* # points */
    int i;                                              /* data index */
    int j=1;                                           /* summation index */

```

```

/* check arguments */
if(tau<=0)                                /* tau negative or zero? */
{
    return(-1);                            /* error */
}

if(n<3)                                    /* need at least 3 points to calc parameters */
{
    return(-1);                            /* error */
}

/* fill gaps if necessary */
if( CountGaps(x, PHASE) )                  /* any gaps? */
{
    FillGaps(x, PHASE);                    /* fill gaps in phase data */
}

/* initialize sums */
sx = sxx = snx = snnx = 0;

/* calculate sums for quadratic fit */
for(i=x[1]; i<=x[2]; i++)
{
    sx  += x[i+2];
    sxx += SQR(x[i+2]);
    snx += x[i+2]*j;
    snnx+= x[i+2]*j*j;
    j++;
}                                           /* end for */

/* calculate terms for quadratic fit */
aa = 3*((3*n*(n+1))+2);
bb = -18*((2*n)+1);
cc = 30;
dd = (12*((2*n)+1)*((8*n)+11))/((n+1)*(n+2));
ee = -180/(n+2);
ff = 180/((n+1)*(n+2));
gg = n*(n-1)*(n-2);

/* calculate coefficients for quadratic fit */
*p_a = ((aa*sx)+(tau*bb*snx)+(tau*tau*cc*snnx))/(gg          );
*p_b = ((bb*sx)+(tau*dd*snx)+(tau*tau*ee*snnx))/(gg*tau      );
*p_c = ((cc*sx)+(tau*ee*snx)+(tau*tau*ff*snnx))/(gg*tau*tau);
*p_v=0;                                /* fit variance 0 if only 3 analysis points */

if(n>=4)                                /* need at least 4 analysis points to calc fit variance */
{
    *p_v = (sxx-(*p_a*sx)-(tau**p_b*snx)-(tau*tau**p_c*snnx))/(n-3);
}

return(n);

}                                           /* end CalcQuadraticDrift() */

```



The FrequenC Library															
<b>NAME:</b> CalcRatio	<b>FUNCTION:</b> Calculate $R(n)$ , the ratio of the modified Allan variance to normal Allan variance														
<b>SYNOPSIS:</b> float CalcRatio(int alpha, float num, float bw)															
int alpha	The log-log slope, $\alpha$ , of $S_y(f)$ for a power law noise process: <table> <tr> <th>Noise Type</th><th><math>\alpha</math></th></tr> <tr> <td>Flicker Walk FM</td><td>-3</td></tr> <tr> <td>Random Walk FM</td><td>-2</td></tr> <tr> <td>Flicker FM</td><td>-1</td></tr> <tr> <td>White FM</td><td>0</td></tr> <tr> <td>Flicker PM</td><td>1</td></tr> <tr> <td>White PM</td><td>2</td></tr> </table>	Noise Type	$\alpha$	Flicker Walk FM	-3	Random Walk FM	-2	Flicker FM	-1	White FM	0	Flicker PM	1	White PM	2
Noise Type	$\alpha$														
Flicker Walk FM	-3														
Random Walk FM	-2														
Flicker FM	-1														
White FM	0														
Flicker PM	1														
White PM	2														
float num	The # of phase data points = # frequency data points + 1														
int bw	Bandwidth factor = $2 \cdot \pi \cdot f_h \cdot \tau_0$ where $f_h$ is measuring system bandwidth														
<b>RETURN:</b> float	The $R(n)$ ratio function = $\text{Mod } \sigma_y^2(\tau) / \sigma_y^2(\tau)$ , or -1 if error														
<b>REMARKS:</b> The bandwidth factor applies only to the $\alpha = +1$ Flicker PM case															
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ x[513];  /* phase data array */ float bw;   /* bandwidth factor */ float r;   /* R(n) */ int num;   /* # phase data points */ int alpha;   /* noise exponent alpha */ . . alpha=0;   /* set alpha */ num=(int) y[0];                                   /* set # data points */ bw=10.0;   /* set bw */ r=CalcRatio(alpha, num, bw);                       /* calc R(n) */ if(r== -1)   /* check for error */ {     printf("\nError");                             /* error message */ } else {     printf("\ndr = %e", r);                         /* display r */ } </pre>															
<b>SEE ALSO:</b> None															
<b>REFERENCE:</b> NIST Technical Note 1337															

## FrequenC Library Reference Manual

```

/*****
/*
/*          CalcQuadraticDrift()
/*
/*          Function to calculate least-squares quadratic fit to phase data
/*           $x(t) = a + bt + ct^2$ 
/*
/*          Reference:      J.A. Barnes, "The Measurement of Linear Frequency
/*                          Drift in Oscillators", Proc. 15th Annual PTI
/*                          Meeting, 1983, pp. 551-582.
/*
/*          Parameters:      F_TYPE x[] = phase data array
/*                          x[0] = # phase data points
/*                          x[1] = analysis start
/*                          x[2] = analysis end
/*                          F_TYPE tau = time interval for phase data
/*                          F_TYPE *p_a = pointer to phase intercept
/*                          F_TYPE *p_b = pointer to frequency intercept
/*                          F_TYPE *p_c = pointer to frequency slope
/*                          F_TYPE *p_v = pointer to fit variance
/*
/*          Return:          int          = # analysis points
/*                                or -1 if error
/*
/*          Notes:           x(t) , t & a in sec, b in sec/sec, c in sec/sec2.
/*                          Frequency drift (slope) = 2c; intercept = b.
/*                          t is time interval of equally-spaced phase data.
/*                          t goes from 1 to n with no missing points.
/*                          Calls FrequenC functions CountGaps() and
/*                          FillGaps() as needed. To preserve gaps, save
/*                          data before calling this function.
/*
/*          Revision record:
/*          12/29/91      Created
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          01/19/92      Added error traps
/*          01/22/92      Added error trap for tau<=0
/*          11/04/92      Changed gap handling -- was NG
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```

#include "frequenc.h"                                /* FrequenC header file */

```

```

int F_declspec(dllexport) CalcQuadraticDrift(F_TYPE x[], F_TYPE tau,
      F_TYPE *p_a, F_TYPE *p_b, F_TYPE *p_c, F_TYPE *p_v)
{
    double aa,bb,cc,dd,ee,ff,gg;                    /* fit terms */
    double sx,sxx,snx,snnx;                          /* summations */
    int n=x[2]-x[1]+1;                                /* # points */
    int i;                                              /* data index */
    int j=1;                                           /* summation index */

```

```

/* check arguments */
if(tau<=0)                                /* tau negative or zero? */
{
    return(-1);                            /* error */
}

if(n<3)                                    /* need at least 3 points to calc parameters */
{
    return(-1);                            /* error */
}

/* fill gaps if necessary */
if( CountGaps(x, PHASE) )                  /* any gaps? */
{
    FillGaps(x, PHASE);                    /* fill gaps in phase data */
}

/* initialize sums */
sx = sxx = snx = snnx = 0;

/* calculate sums for quadratic fit */
for(i=x[1]; i<=x[2]; i++)
{
    sx  += x[i+2];
    sxx += SQR(x[i+2]);
    snx += x[i+2]*j;
    snnx+= x[i+2]*j*j;
    j++;
}                                           /* end for */

/* calculate terms for quadratic fit */
aa = 3*((3*n*(n+1))+2);
bb = -18*((2*n)+1);
cc = 30;
dd = (12*((2*n)+1)*((8*n)+11))/((n+1)*(n+2));
ee = -180/(n+2);
ff = 180/((n+1)*(n+2));
gg = n*(n-1)*(n-2);

/* calculate coefficients for quadratic fit */
*p_a = ((aa*sx)+(tau*bb*snx)+(tau*tau*cc*snnx))/(gg          );
*p_b = ((bb*sx)+(tau*dd*snx)+(tau*tau*ee*snnx))/(gg*tau     );
*p_c = ((cc*sx)+(tau*ee*snx)+(tau*tau*ff*snnx))/(gg*tau*tau);
*p_v=0;                                /* fit variance 0 if only 3 analysis points */

if(n>=4)                                /* need at least 4 analysis points to calc fit variance */
{
    *p_v = (sxx-(*p_a*sx)-(tau**p_b*snx)-(tau*tau**p_c*snnx))/(n-3);
}

return(n);

}                                           /* end CalcQuadraticDrift() */

```



The FrequenC Library	
<b>NAME:</b> CalcStarB1	<b>FUNCTION:</b> Description of what function does
<b>SYNOPSIS:</b> int FunctionName( F_TYPE z[], F_TYPE one, F_TYPE two)	
F_TYPE z[]	Phase or frequency data array z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE one	parameter one, and description of what it is
F_TYPE two	parameter two, and description of what it is
<b>RETURN:</b> int	# non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are modified. Embedded zeros are treated as gaps in phase data. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include &lt;frequenc.h&gt;                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ F_TYPE one;   /* parameter one */ F_TYPE two;   /* parameter two */ int num;   /* # data points processed */ . . one=1.0;   /* set 1st parameter value */ two=2.0;   /* set 2nd parameter value */ num=FunctionName(z, one, two);                     /* call function */ printf("\n# Data Points Scaled = %d", num);        /* display num */ </pre>	
<b>SEE ALSO:</b> RelatedFunctionName()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*                               CalcStarB1()
/*
/*  Function to calculate the Barnes B1 ratio of the N-sample to 2-sample
/*  (standard to Allan) variance for frequency data treated as phase data
/*  which is used to resolve alpha=3 or -4 ambiguity for Hadamard sigmas.
/*  This is called *B1 to distinguish it from the normal B1 ratio.
/*
/*
/*  Parameters:      F_TYPE   *fData           Data array
/*                   BOOL     bDataType        Data type (0=Phase, 1=Freq)
/*                   int      fTau             Averaging factor
/*                   int      nAF
/*
/*  Return:          float    fB               *B1 ratio
/*                                     or -1.0 if error
/*
/*  Notes:           What we are doing here is to use Chuck Greenhall's
/*                   idea to calculate the B1 ratio for the freq data
/*                   as phase data, and use the standard noise ID method
/*                   except for adding 2 to the resulting mu (subtracting
/*                   2 from alpha).
/*
/*  References:      1.  C.A. Greenhall, (private communication)
/*                   2.  D. Howe, et al PTTI 2000 paper
/*
/*  Revision record:
/*      11/14/00      Created
/*      11/15/00      Changed parameters
/*      04/26/03      Adapted for Version 2.0 source code documentation
/*
/*  (c) Copyright 2000-3  Hamilton Technical Services  All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

float __declspec(dllexport) FAR PASCAL CalcStarB1(F_TYPE fData[],
    BOOL bDataType, F_TYPE fTau, int nAF)
{
    // Local variables
    F_TYPE *fWork;    // Pointer to working data array
    F_TYPE fSig;      // Allan deviation
    F_TYPE fStdDev;   // Standard deviation
    int nNum;         // # data points
    int i;            // Index

    // Get # data points in data array
    nNum=(int)fData[0];

    // Allocate working array of freq data
    // Data is subject to being averaged, so must use a working array
    if((fWork=(F_TYPE*)malloc((nNum+ARRAY_OFFSET)*sizeof(F_TYPE)))==NULL)
    {
        // Error
        return -1.0;
    }
}

```

```

// For phase data, convert it to freq data in working array
if(bDataType==PHASE_DATA)
{
    // Conv phase data to freq data
    ConvPhaseToFreq(fData, fWork, fTau, TRUE);
}
else // Freq data - no conversion needed - copy it to working array
{
    // Copy freq data to working array
    for(i=0; i<nNum+ARRAY_OFFSET; i++)
    {
        fWork[i]=fData[i];
    }
}

// Average working freq data
AverageFreqData(fWork, nAF);

// Calc its sigma and std dev as if it were phase data
CalcPhaseSigma(fWork, &fSig, fTau);
CalcPhaseStdDev(fWork, &fStdDev, fTau);

// Free the working memory
free(fWork);

// Calc & return *B1 = ratio of standard to Allan variance
return (float)(SQR(fStdDev/fSig));
}

```



The FrequenC Library	
<b>NAME:</b> CalcSecondDiff	<b>FUNCTION:</b> Calculate the second difference for phase data
<b>SYNOPSIS:</b> int CalcQuadraticDrift(F_TYPE x[], F_TYPE *p_d)	
F_TYPE x[]	Phase data array: x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE *p_d	Pointer to the average of the 2nd differences (frequency drift) for the phase data
<b>RETURN:</b> int	The # of analysis points processed, or -1.0 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. There must be at least 3 non-gap analysis points. Embedded zeros are treated as gaps in phase data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[513];                                       /* phase data array */ F_TYPE d;   /* 2nd difference */ int num;   /* # analysis points */ . . num=CalcSecondDiff(x, &amp;d);                          /* calc second difference */ if(num==-1) {     printf("\nError");                               /* error message */ } else {     printf("\n2nd Diff = %e, d);                     /* display 2nd difference */ } </pre>	
<b>SEE ALSO:</b> CalcQuadraticDrift()	
<b>REFERENCE:</b> NIST Technical Note 1337	

## FrequenC Library Reference Manual

```

/*****
/*
/*          CalcSecondDiff()
/*
/*          Function to calculate average of 2nd differences of phase data
/*
/*          Parameters:      F_TYPE x[]  = array of phase data
/*                          x[0] = # phase data points
/*                          x[1] = analysis start
/*                          x[2] = analysis end
/*                          F_TYPE *p_d = pointer to average of second
/*                                  differences of phase data
/*                                  = frequency drift of phase data
/*
/*          Return:         int          = # analysis points,
/*                                  or -1 if error
/*
/*          Note:           Embedded gaps are treated as gaps in phase data.
/*                          There must be at least 1 analysis point,
/*                          which requires at least 3 adjacent non-gap
/*                          phase data points.
/*
/*          Revision record:
/*              12/29/91    Created
/*              12/31/91    Renamed
/*              01/18/92    Edited title
/*              01/19/92    Added d parameter for result, changed return to
/*                          int = # analysis points, added error trap
/*              02/03/96    Modified for use as Win 3.1 DLL
/*              01/01/98    Changes for MS VC++ compatibility & warnings
/*              04/26/03    Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcSecondDiff(F_TYPE x[], F_TYPE *p_d)
{
    float num;
    double d1;
    double d2;
    double sum;
    int i;

    num = 0;
    sum = 0;

    for(i=(int)(x[1]+2); i<=(int)x[2]; i++)
    {

```

```

if((x[i] && x[i+1] && x[i+2]) || (i==3 && x[4] && x[5]) \
    || (x[i+1] && x[i] && i==x[2]))
    /* no phase points are gaps, */
    /* or 1st point with non-zero 2nd & 3rd points, */
    /* or last point with non-zero next-to-last & */
    /* next-to-next-to-last points */
    {
        d1 = x[i+1] - x[i];
        d2 = x[i+2] - x[i+1];
        sum += d2 - d1;
        num++;
    }
    /* end if */
}
/* end for */
if(num>0)
{
    *p_d = sum / num;
    return(int)num;
}
else
{
    return(-1);
}
/* error */
}
/* end CalcSecondDiff() */

```



The FrequenC Library	
<b>NAME:</b> CalcThreePointDrift	<b>FUNCTION:</b> Calculate frequency drift using the first, middle and last phase data points.
<b>SYNOPSIS:</b> float CalcThreePointDrift(F_TYPE x[])	
F_TYPE x[]	Phase data array x[0] = # data points x[1] = analysis start point x[2] = analysis end point
<b>RETURN:</b> float	Frequency drift per tau interval
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. Embedded zeros are treated as gaps in phase data. This is the best estimator of drift for the combination of white and random walk FM noise (see reference). Tau=1 is assumed. Drift is per tau interval. This function calls FrequenC functions CountGaps() and FillGaps(). To preserve gaps, save original phase data before calling this function.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[512];                                       /* data array */ float drift;   /* freq drift */ . . drift= CalcThreePointDrift(x);                        /* call function */ printf("\nDrift = %e", drift);                      /* display result */ </pre>	
<b>SEE ALSO:</b> CalcQuadraticDrift()	
<b>REFERENCE:</b> M. Weiss, D. Allan, and D. Howe, "Confidence on the Second Difference Estimation of Frequency Drift", 1992 IEEE Frequency Control Symposium, pp.300-305, June, 1992.	

```

/*****
/*
/*          CalcThreePointDrift()
/*
/*          Function to calculate frequency drift using the first, middle
/*          and last phase data points.
/*
/*
/*          Parameters:      x[]      phase data array
/*
/*          Return:         float    frequency drift
/*
/*          Notes:  This is the best estimator of drift for the combination
/*                  of white and random walk FM noise (see reference).
/*                  Tau=1 is assumed.  Drift is per tau interval.
/*                  This function calls FrequenC functions CountGaps() and
/*                  FillGaps().  To preserve gaps, save original phase data
/*                  before calling CalcThreePointDrift().
/*
/*          Reference:
/*          M. Weiss, D. Allan, and D. Howe, "Confidence on the Second Diff-
/*          erence Estimation of Frequency Drift", 1992 IEEE Frequency Control
/*          Symposium, pp.300-305, June, 1992.
/*
/*          Revision record:
/*          11/01/92      Created
/*          02/03/96      Removed unused variable: int i
/*                      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1992-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

#include "frequenc.h"                                /* FrequenC header file */

float __declspec(dllexport) FAR PASCAL CalcThreePointDrift(F_TYPE x[])
{
    int start;                                /* first phase analysis point */
    int mid;                                  /* middle phase analysis point */
    int end;                                  /* last phase analysis point */

    float n1, n2;                            /* # analysis points in 1st and last halves */
    float n3;                                /* avg # analysis points in each half */
    float d;                                  /* frequency drift per tau interval */

    /* fill gaps if necessary */
    if( CountGaps(x, PHASE) )                /* any gaps? */
    {
        FillGaps(x, PHASE);                  /* fill gaps in phase data */
    }                                          /* end if */

    /* calculate drift */
    start = (int) x[1];                      /* first analysis point */
    mid = (int) ((x[2]-x[1])+2)/2;           /* middle analysis point */
    end = (int) x[2];                        /* last analysis point */
    n1 = (float) mid-start;                  /* # points in 1st half */
    n2 = (float) end-mid;                    /* # points in 2nd half */
    n3 = (n1+n2)/2;                          /* drift interval */

```

```
d = (float) (((x[end+2]-x[mid+2])/n2) - ((x[mid+2]-x[start+2])/n1))/n3);  
  
return(d);                                     /* frequency drift */  
}                                              /* end CalcThreePointDrift() */
```



The FrequenC Library	
<b>NAME:</b> DateConv	<b>FUNCTION:</b> Convert month & year to day of week, DOY, MJD, and # days in month
<b>SYNOPSIS:</b> <pre>void DateConv(int *lpnMonth, int *lpnDaysInMonth,               int *lpnYear, int *lpnDOW, int *lpnDOY, long *lpnMJD)</pre>	
int *p_month	Pointer to month # (January=1)
int *p_days	Pointer to # days in month
int *p_year	Pointer to 4-digit year (e.g. 2003)
int *p_dow	Pointer to day of week (Sunday=0)
int *p_doy	Pointer to day of year
long *lp_mjd	Pointer to Modified Julian Date
<b>RETURN:</b> void	
<b>REMARKS:</b> Calling program sets month and year. 1st day of month is assumed. Function calculates corresponding day of week, day of year, MJD and # days in month.	
<b>EXAMPLE:</b> <pre>#include "frequenc.h"                                /* FrequenC header file */ int month;   /* month # */ int days;   /* # days in month */ int year;   /* year */ int dow;   /* day of week */ int doy;   /* year */ long mjd;   /* MJD */ . . month=1;   /* set month */ year=2003;   /* set year */ DateConv(&amp;month, &amp;days, &amp;year, &amp;dow, &amp;doy, &amp;mjd); /* call function */ printf("\nDOW = %d", DOY = %d, MJD = %ld, Days/Month = %d", dow, doy,       mjd, days);                                /* display results */</pre>	
<b>SEE ALSO:</b> MJDtoDOY(), MJDtoDate()	
<b>REFERENCE:</b> None	

## FrequenC Library Reference Manual

```

/*****
/*
/*          DateConv()
/*
/*      Function to convert month & year to day of week, DOY and MJD,
/*      plus # days in month.
/*
/*      Calling program sets month and year. 1st day of month is assumed.
/*      Function sets corresponding day of week, day of year, MJD and
/*      # days in month.
/*
/*      Uses date functions from Hammer library.
/*
/*      Parameters:
/*          int  lpnMonth      pointer to month (January=1)
/*          int  lpnDaysInMonth pointer to # days in month
/*          int  lpnYear       pointer to year (e.g. 1995)
/*          int  lpnDOW        pointer to day of week (Sunday=0)
/*          int  lpnDOY        pointer to day of year
/*          long lplnMJD       pointer to Modified Julian Date
/*
/*      Returns nothing (void)
/*
/*      Revision record:
/*          03/30/96   Adapted from date_conv() of SCRN_CAL.C
/*          04/08/97   Fixed bug in century leap year logic
/*          07/18/97   Changed to new date function to avoid Hammer Library
/*          04/26/03   Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1996-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

#include "frequenc.h"                                /* FrequenC Library header file */

void __declspec(dllexport) FAR PASCAL DateConv(int *lpnMonth,
        int *lpnDaysInMonth, int *lpnYear, int *lpnDOW, int *lpnDOY, long *lplnMJD)
{
    static int sum[] = { 0, 31, 59, 90, 120, 151, 181, 212,
                        243, 273, 304, 334, 365 };
    static int num_days[] = {31, 28, 31, 30, 31, 30, 31, 31,
                             30, 31, 30, 31};

    // Local variables
    int month;
    int year;
    int dow;                                /* day of week: 0=Sunday ... 6=Saturday */
    int day=1;                              /* day of month always 1 */
    int doy;                                /* day of year */
    int leap=0;                             /* leap year flag */
    long int gdate;                         /* Gregorian date */
    long int jdate;                         /* Julian day # */
    long int mjd;                          /* Modified Julian Day */

    // Initializations
    month=*lpnMonth;
    year=*lpnYear;

    // Date conversions
    gdate=MakeDate(month, day, year);
    BreakDate(gdate, &month, &day, &year);

```

```

dow=DayOfWeek(gdate);

doy=sum[month-1]+day;

if( year % 4 == 0 && year % 100 != 0 || year % 400 == 0 )
{
    leap=1;
    if(month>2)
    {
        doy++;
    }
}
/* end if */
/* end if */

jdate=DateToJulian(gdate);
mjd=jdate-2400001L;

// Pass results
*lpInMJD=mjd;
*lpnDOW=dow;
*lpnDOY=doy;

if(month!=2)
{
    leap=0;
}
/* end if */

*lpnDaysInMonth=num_days[month-1]+leap;
}
/* end date_convert() */

```



The FrequenC Library	
<b>NAME:</b> DateToMJD	<b>FUNCTION:</b> Convert date to MJD
<b>SYNOPSIS:</b> long DateToMJD(int day, int month, int year)	
int day	Day of date to be converted to MJD
int month	Month of date to be converted to MJD
int year	Year of date to be converted to MJD
<b>RETURN:</b> long	Modified Julian date # for date
<b>REMARKS:</b> Example: November 11, 1992 is MJD 48937.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ int day=11;   /* day */ int month=11;   /* month */ int year=1992;                                       /* year */ long mjd;   /* MJD */ . . mjd=DateToMJD(day, month, year);                     /* call function */ printf("\nMJD = %ld", mjd);                          /* display MJD */ </pre>	
<b>SEE ALSO:</b> MJDtoDate()	
<b>REFERENCE:</b>	

## FrequenC Library Reference Manual

```

/*****
/*
/*          DateToMJD()
/*
/*          Function for date to MJD conversion
/*
/*          Parameters:
/*              int  day      day of date to be converted to MJD
/*              int  month    month of date to be converted to MJD
/*              int  year     year of date to be converted to MJD
/*
/*          Return:
/*              long mjd      modified Julian day # for date
/*
/*          Example:
/*              November 11, 1992 is MJD 48937.
/*
/*          Function revision record:
/*              11/11/92      Created
/*              11/28/92      Adapted for FrequenC Library
/*              02/03/96      Changed constant 679019 to L
/*                          Modified for use as Win 3.1 DLL
/*              01/01/98      Changes for MS VC++ compatibility & warnings
/*              04/26/03      Adapted for Version 2.0 source code documentation
/*
/*          (c) Copyright 1992-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

#include "frequenc.h"                                /* FrequenC header file */

long __declspec(dllexport) FAR PASCAL DateToMJD(int day, int month, int year)
{
    if(month>2)
    {
        month++;
    }
    else
    {
        month+=13;
        year--;
    }

    return(-679019L+(long) (365.25*year)+(long) (30.6001*month)+day);

}
/* end DateToMjd() */

```

The FrequenC Library	
<b>NAME:</b> DayOfWeek	<b>FUNCTION:</b> Find day of week for a given Gregorian date
<b>SYNOPSIS:</b> int WINAPI DayOfWeek(long gdate)	
long gdate	Gregorian date (yyyymmdd)
<b>RETURN:</b> int	Day of week (0=Sunday, 6=Saturday)
<b>REMARKS:</b> Covers years 1900-2099 Calls BreakDate()	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ long gdate;   /*Gregorian date */ int dow;  /* day of week */ . . gdate=20030101;                                       /* set date */ dow=DayOfWeek(gdate);                                /* call function */ printf("\nDOW = %d", dow);                           /* display dow */ </pre>	
<b>SEE ALSO:</b> MakeDate(), BreakDate()	
<b>REFERENCE:</b> NIST Technical Note 1337	

## FrequenC Library Reference Manual

```

/*****
/*
/*          DayOfWeek()
/*
/*      Function to find the day of the week for a given Gregorian date
/*
/*      Note: Calls Brkdate() above
/*
/*      Parameters: long      gdate      Gregorian date (yyyymmdd)
/*
/*      Return:      int          Day of week (0=Sunday, 6=Saturday)
/*
/*      Revision record:
/*          07/17/97      Cloned from dayofwk() of Hammer Library
/*                      Changed error return to -1
/*                      Modified for 4-digit year from BreakDate()
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/*      (c) Copyright 1997-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

#include "frequenc.h"                                /* FrequenC Library header file */

int __declspec(dllexport) FAR PASCAL DayOfWeek(long gdate)
{
    // Local variables
    int a, b, mo, da, yr;
    static int mos[12] = { 0,3,3,6,1,4,6,2,5,0,3,5 };

    BreakDate(gdate, &mo, &da, &yr);

    // Convert 4-digit year into 2-digit year
    // yr=yr % 100;    // Only OK 1900-1999
    yr=yr-1900;      // Better; OK 1900-2099

    if ( mo<1 || mo>12 || da<1 || da>31 || yr<0 )
    {
        return (-1);    /* error - bad date */
    }

    a = (yr/4) + yr + da + mos[mo-1];
    b = (a % 7) + 1;

    if (mo<=2 && yr!=0 && (yr % 4)==0)
    {
        b = (b==0 ? 6 : b) - 1;
    }

    b = (b==0 ? 7 : b) - 1;

    return (b); /* return day of week (0-6) */
}

```

The FrequenC Library	
<b>NAME:</b> DateToJulian	<b>FUNCTION:</b> Convert Gregorian date to Julian day number
<b>SYNOPSIS:</b> long DateToJulian(long gdate)	
long gdate	Gregorian Date (yyyymmdd)
<b>RETURN:</b> long	Julian day number
<b>REMARKS:</b>	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ long gdate;   /* Gregorian date */ long jd;  /* Julian day # */ . .  jd=DateToJulian(gdate);                               /* call function */ printf("\nJulian Day # = %ld", jd);                  /* display results */ </pre>	
<b>SEE ALSO:</b> MJDtoDOY(), MJDtoDate()	
<b>REFERENCE:</b> None	

## FrequenC Library Reference Manual

```

/*****
/*
/*          DateToJulian()
/*
/*      Function to convert Gregorian date to Julian day number
/*
/*      Parameters: long    gdate    Gregorian date (yyyymmdd)
/*
/*      Return:    long    jdate    Julian day number
/*
/*      Revision record:
/*          07/17/97    Cloned from datjul() of Hammer Library
/*                      Changed error return to -1
/*                      Modified to use 4-digit year return from BreakDate()
/*          04/26/03    Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1997-2003 Hamilton Technical Services All Rights Reserved */
*/
*****/

#include "frequenc.h"                                /* FrequenC Library header file */

long __declspec(dllexport) FAR PASCAL DateToJulian(long gdate)
{
    // Local variables
    long jdate; /* Julian Day Number for given date */
    int mo, da, yr, c, ya;

    if (gdate<=0L || gdate==19000000L)                /* if zero or negative, return -1 */
    {
        return (-1L); /* error */
    }

    BreakDate(gdate, &mo, &da, &yr);

    if (mo>2)
    {
        mo-=3;
    }
    else
    {
        mo+=9;
        yr--;
    }

    c=yr/100;
    ya=yr%100;
    jdate=(146097L*c)/4L + (1461L*ya)/4L + (153L*mo+2L)/5L + da + 1721119L;

    return (jdate);
}

```

The FrequenC Library	
<b>NAME:</b> FillGaps	<b>FUNCTION:</b> Fill gaps in phase or frequency data
<b>SYNOPSIS:</b> int FillGaps(F_TYPE z[], BOOL datatype)	
F_TYPE z[]	Phase or frequency data array: z[0] = # data points z[1] = analysis start point z[2] = analysis end point
BOOL datatype	Type of data: 0=phase, 1=frequency
<b>RETURN:</b> int	The # of gaps filled
<b>REMARKS:</b> Only data gaps between start and end analysis limits are filled. All zeros are treated as gaps in frequency data. Only embedded gaps are treated as gaps in phase data. The datatype flag determines whether the data is treated as phase or frequency data. The gaps processed are filled with interpolated values. No error codes are returned by this function.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ BOOL datatype;                                       /* data type flag */ int num;   /* # gaps */ . . datatype=FREQ;                                       /* set flag for frequency data */ /* frequenc.h contains #define PHASE 0 and #define FREQ 1 */ num=Fill(z, datatype);                               /* fill gaps in data */ printf("\n# Gaps Filled = %d", num);                /* display num */ </pre>	
<b>SEE ALSO:</b> CountGaps()	
<b>REFERENCE:</b> None	

## FrequenC Library Reference Manual

```

/*****
/*
/*          FillGaps()
/*
/*      Function to fill gaps in data with interpolated values
/*
/*      Parameters:      F_TYPE z[]  = phase or frequency data
/*                          z[0] = # data points
/*                          z[1] = analysis start
/*                          z[2] = analysis end
/*
/*                          BOOL datatype = data type: 0=phase, 1=frequency
/*
/*      Return:          int          = # gaps removed
/*
/*      Note:            All zeros treated as gaps in frequency data.
/*                        Embedded zeros treated as gaps in phase data.
/*
/*      Revision record:
/*          12/16/91      Created
/*          12/24/91      Changed to make datatype a parameter rather than a
/*                        global variable. Remove call to inc_extension().
/*          12/31/91      Renamed
/*          01/18/92      Edited title
/*          07/22/93      Fixed bug that changed i inside interior gap loop
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1991-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL FillGaps(F_TYPE z[], BOOL datatype)
{
    int g = 0;                                /* total gap count */
    int i;                                    /* general (outer) index */
    int i_start;                              /* index of last data point at start of gap */
    int i_end;                                /* index of next data point at end of gap */
    int j;                                    /* inner index */
    int k;                                    /* local gap count */
    int n = (int)*z;                          /* # data points */
    double increment;                        /* freq increment for interpolated data */

    for(i=(int) (* (z+1)+3-datatype); i<=(int) (* (z+2)+1+datatype); i++)
        /* elim leading gaps */
    {
        if(!*(z+i))                          /* is data point a gap? */
        {
            for(j=i; j<n+2; j++)              /* move all data up to remove gap */
            {
                *(z+j) = *(z+j+1);
            }
            /* end for */
            i--; /* after shifting, must test the first data point again */
            g++; /* increment the total gap count */
            n--; /* decrement the data counts */
            *z=n;
            *(z+2)=*(z+2)-1;
        }
    }
}

```

```

    }
    /* end if */

else
{
    break;          /* stop when first non-gap data point is reached */
}
/* end else */
}
/* end for */

for(i=(int) (* (z+2)+1+datatype); i>=(int) (* (z+1)+3-datatype); i--)
    /* elim trailing gaps */
{
    if(!*(z+i))
        /* is data point a gap? */
    {
        for(j=i; j<n+2; j++)
            /* move all data up to remove gap */
        {
            *(z+j) = *(z+j+1);
        }
        /* end for */
        g++;
        /* increment the total gap count */
        n--;
        /* decrement the data counts */
        *z=n;
        *(z+2)=*(z+2)-1;
    }
    /* end if */
else
{
    break;          /* stop when last non-gap data point is reached */
}
}
/* end for */

k=0;
/* replace interior gaps with interpolated values */
for(i=(int) (* (z+1)+3-datatype); i<=(int) (* (z+2)+1+datatype); i++)
{
    if(!*(z+i))
        /* is data point a gap? */
    {
        k++;
        /* increment the local gap count */
    }
    /* end if */
else
{
    if(k)
        /* are we at a gap? */
    {
        i_end = i;
        /* save the index for the end of the gap */
        i_start = i-k-1;
        /* save index for the start of the gap */
        increment = (*(z+i_end) - *(z+i_start)) / (k+1);
        for(j=1; j<=k; j++)
        {
            *(z+i_start+j) = *(z+i_start) + increment*j;
            g++;
            /* increment the gap count */
        }
        /* end for */
        k=0;
        /* reinitialize count for next gap */
    }
    /* end if */
}
/* end else */
}
/* end for */

return(g);
/* return total # gaps removed */
}
/* end FillGaps() */

```



The FrequenC Library	
<b>NAME:</b> FindMedian	<b>FUNCTION:</b> Find median value in data array
<b>SYNOPSIS:</b> int FindMedian(F_TYPE z[], BOOL datatype, F_TYPE *median)	
F_TYPE z[]	Phase or frequency data array: z[0] = # data points z[1] = analysis start point z[2] = analysis end point
BOOL datatype	Type of data: 0=phase, 1=frequency
F_TYPE median	Median value
<b>RETURN:</b> int	0 if OK, or -1 if error
<b>REMARKS:</b> Only data between start and end analysis limits are analyzed. All zeros are treated as gaps in frequency data. Embedded zeros only are treated as gaps in phase data. The datatype flag determines whether data is treated as phase or freq. Median is always center value for odd # data points. Median is average of two center values for even # data points <100, and is simply the smaller of the two for even # data points >=100.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* freq data array */ BOOL datatype=FREQ;                                /* data type flag */ /* frequenc.h contains #defines PHASE 0 and FREQ 1 */ int code;   /* return code */ . . code=FindMedian(y, datatype, &amp;median);              /* call function */ printf("\nMedian = %e", median);                    /* display result */ </pre>	
<b>SEE ALSO:</b>	
<b>REFERENCE:</b> None	

```

/*****
/*
/*                               Median Functions                               */
/*
/*   Functions to find median value in array.                                */
/*   FindMedian() calls FindMedian1() or FindMedian2() depending on          */
/*   array size. FindMedian1() calls FindMed() for size <100.                */
/*   FindMedian2() calls nrselect() for size >=100.                          */
/*   Only top-level FindMedian() function is exported.                      */
/*
/*   Revision record:
/*       03/18/03   File Created
/*       04/26/03   Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 2003  Hamilton Technical Services  All Rights Reserved
/*
*****/

// Include FrequenC header file
#include "frequenc.h"

// Local wrapper function prototypes
int FindMedian1(F_TYPE fData[], BOOL bDataType, F_TYPE *pfMedian);
int FindMedian2(F_TYPE fData[], BOOL bDataType, F_TYPE *pfMedian);

/*****
/*
/*                               FindMedian()                               */
/*
/*   Function to call one of two FindMedian wrapper functions                */
/*
/*   Parameters:      F_TYPE fData      = data array
/*                   fData[0] = # data points
/*                   fData[1] = analysis start
/*                   fData[2] = analysis end
/*
/*                   BOOL bDataType     = data type flag: 0=phase, 1=freq
/*
/*                   F_TYPE *pfMedian = pointer to median
/*
/*   Returns:        int                = 0 if OK or -1 if error
/*
/*   Note:           One of two FindMedian wrapper functions is called
/*                   depending on size of data array
/*
/*   Revision record:
/*       05/07/02   Created
/*       03/18/03   Adapted for FrequenC.dll
/*       04/26/03   Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 2002-3  Hamilton Technical Services  All Rights Reserved
/*
*****/

int __declspec(dllexport) FAR PASCAL FindMedian(F_TYPE fData[],
        BOOL bDataType, F_TYPE *pfMedian)
{
    // Local variables
    int nSize;           // Size of data array
    int nCode;           // Error code

```

```

// Find size of data array
nSize=(int) (fData[2]-fData[1]+1);

// Call one of two wrapper functions
if(nSize<100)
{
    nCode=FindMedian1(fData, bDataType, pfMedian);
}
else // Large array
{
    nCode=FindMedian2(fData, bDataType, pfMedian);
}

// Done
return nCode;
}

/*****
/*
/*                               FindMedian1()                               */
/*
/*      Wrapper function to safely call FindMed()for small array size          */
/*
/*      Parameters:      F_TYPE fData    = data array                        */
/*                               fData[0] = # data points                    */
/*                               fData[1] = analysis start                    */
/*                               fData[2] = analysis end                      */
/*
/*                               BOOL bDataType = data type flag: 0=phase, 1=freq */
/*
/*                               F_TYPE *median = pointer to median            */
/*
/*      Returns:         int              = 0 if OK or -1 if error              */
/*
/*      Note:            Embedded zeros treated as gaps in phase data.          */
/*                       All zeros gaps in frequency data.                    */
/*                       Must have at least 1 data point.                      */
/*
/*      Revision record:
/*          09/14/98      Created                                              */
/*          03/18/03      Adapted for FrequenC.dll                          */
/*          04/26/03      Adapted for Version 2.0 source code documentation */
/*
/* (c) Copyright 1998-2003 Hamilton Technical Services All Rights Reserved */
/*
*****/

// Prototype for local median function
int FindMed(F_TYPE z[], BOOL dtype, F_TYPE *median);

int FindMedian1(F_TYPE fData[], BOOL bDataType, F_TYPE *pfMedian)
{
    // Local variables
    int i;                // General index
    int nNum;              // # data points in input array
    F_TYPE *fTemp;         // Pointer to temporary array to save original data

    // Save data in temporary array
    // Get array size
    nNum=(int) fData[0];

```

```

// Allocate memory
if ((fTemp=(F_TYPE*)malloc((nNum+ARRAY_OFFSET)*sizeof(F_TYPE)))==NULL)
{
    *pfMedian=0.0;
    return -1; // Error code
}

// Save data
for(i=0; i<nNum+ARRAY_OFFSET; i++)
{
    fTemp[i]=fData[i];
}

// Call FindMed()
FindMed(fData, bDataType, pfMedian);

// Restore data
for(i=0; i<nNum+ARRAY_OFFSET; i++)
{
    fData[i]=fTemp[i];
}

// Free temporary data array
free(fTemp);

// Done
return 0; // OK
}

/*****
/*
/*                               FindMedian2()
/*
/*  Wrapper function to safely call NR nrselect()
/*  FindMed() gives strictly correct result for # odd or even
/*  Faster nrselect() used when # > 100
/*
/*  Parameters:      F_TYPE fData    = data array
/*                  fData[0] = # data points
/*                  fData[1] = analysis start
/*                  fData[2] = analysis end
/*                  BOOL bDataType = data type flag: 0=phase, 1=freq
/*                  F_TYPE *median = pointer to median
/*
/*  Returns:         int              = 0 if OK or -1 if error
/*
/*  Note:            Embedded zeros treated as gaps in phase data.
/*                  All zeros gaps in frequency data.
/*                  Must have at least 1 data point.
/*
/*                  This function best used for large N, say N>100
/*                  It handles analysis limits & gaps. It is X10
/*                  faster than full sort for large N.
/*
/*  Revision record:
/*      05/06/02      Created and working
/*      03/18/03      Adapted for FrequenC.dll
/*      04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 2002-3 Hamilton Technical Services All Rights Reserved

```

```

/*                                                                 */
/*****
// Prototype for NR select() function used in median calc
float nrselect(unsigned long k, unsigned long n, float arr[]);

int FindMedian2(F_TYPE fData[], BOOL bDataType, F_TYPE *pfMedian)
{
    // Local variables
    int i;                // General index
    int k;                // Secondary index
    int nStart;           // Analysis start point
    int nNum;             // # analysis points
    int nGaps=0;          // # gaps found
    float *fTemp;         // Pointer to temporary array for median calc

    // Copy analysis data into temporary working array using indices 1 to nNum
    // Get start # and # analysis points
    nStart=(int)fData[1];
    nNum=(int) (fData[2]-fData[1]+1);

    // Allocate memory for analysis data only - no header
    // The +1 allows the array index to start at 1 per NR style
    if((fTemp=(float*)malloc((nNum+1)*sizeof(float)))==NULL)
    {
        *pfMedian=0.0;
        return -1; // Error code
    }

    // Copy analysis data into temporary float array
    k=1;
    for(i=1; i<=nNum; i++)
    {
        if(bDataType==FREQ_DATA)
        {
            // All zeros are gaps to be omitted
            if((fTemp[k]=(float)fData[ARRAY_OFFSET+nStart+i-2])==0)
            {
                nGaps++;
            }
            else
            {
                k++;
            }
        }
        else // Phase data
        {
            // All except 1st & last zeros are gaps to be omitted
            if((fTemp[k]=(float)fData[ARRAY_OFFSET+nStart+i-2])==0)
            {
                if( (k=1) || (k=nNum) )
                {
                    nGaps++;
                }
                else
                {
                    k++;
                }
            }
        }
    }
}

```

```

        else
        {
            k++;
        }
    }
}

// Adjust # points
nNum-=nGaps;

// Call NR function to find median
// 1st arg is kth smallest value to find = (N+1)/2
// This is exactly correct median for N odd
// For N even, strictly speaking, median S/B avg of N/2 and N/2 +1 points
// We aren't going to worry about that, esp for large N
*pfMedian=(F_TYPE)nrselect((unsigned long)((nNum+1)/2), (unsigned long)nNum,
    fTemp);

// Free temporary data array
free(fTemp);

// Done
return 0; // OK
}

/*****
/*
/*                               FindMed()
/*
/*      Function to find median of array of phase or frequency data
/*
/*      Parameters:      F_TYPE z[]      = phase or frequency data
/*                      z[0] = # data points
/*                      z[1] = analysis start
/*                      z[2] = analysis end
/*                      BOOL  datatype = data type: 0=phase, 1=frequency
/*                      F_TYPE *median= pointer to median value of data
/*
/*      Notes:          All zeros treated as gaps in frequency data.
/*                      Embedded zeros treated as gaps in phase data.
/*                      This function first fills gaps in the data
/*                      with interpolated values by calling fill().
/*                      It then sorts the data into ascending order,
/*                      using qsort(), to find the median value.
/*                      The median is the center value for an odd # of
/*                      data points, and the average of the two center
/*                      values for an even # of data points.
/*
/*      Return:         int              = error flag: 0=OK, 1=NG
/*
/*      Revision record:
/*          05/03/97      Adapted from FindMedian() of STABLE_A.C
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          03/18/03      Adapted for FrequeNC.dll
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1992-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
// Declare comparison function - not exported */
static int median_compare(const void *a, const void *b);

int FindMed(F_TYPE z[], BOOL datatype, F_TYPE *median)
{
    int i; /* 1st index */
    int j=0; /* 2nd index */
    int start=(int)z[1]; /* analysis start */
    int end=(int)z[2]; /* analysis end */
    int num=(int)z[0]; /* # data points */
    F_TYPE *temp; /* pointer to temporary data storage array */
    F_TYPE med; /* median value */

    // save data
    if((temp=(F_TYPE *)malloc((num+3)*sizeof(F_TYPE)))==NULL)
        /* allocate temporary data storage space */
    {
        return(1); /* error return */
    } /* end if */

    for(i=0; i<num+3; i++)
    {
        temp[i]=z[i]; /* save data */
    } /* end for */

    /* Fill any gaps in data */
    FillGaps(z, datatype);

    /* eliminate non-analysis points */
    for(i=start+2; i<=end+2; i++)
    {
        z[j]=z[i];
        j++;
    } /* end for */
    num=end-start+1;

    /* sort data into numerical order */
    qsort((void *) z, (size_t) num, sizeof(F_TYPE), median_compare);

    /* find & return median */
    if(num%2) /* is num odd? */
    {
        med=z[num/2]; /* middle value */
    } /* end if */
    else
    {
        /* n is even */
        med=(z[(num/2)-1]+z[num/2])/2.0; /* average of 2 middle values */
    } /* end else */

    // restore data
    for(i=0; i<num+3; i++)
    {
        z[i]=temp[i]; /* restore data */
    } /* end for */
    free(temp); /* deallocate temp[] */

    *median=med; /* set median to med = median of data */
    return(0); /* normal return */
} /* end FindMedian() */
```

```

/*****
/*
/*          median_compare()
/*
/*      Qsort compare function for finding median of array
/*
/*
*****/

static int median_compare(const void *a, const void *b)
{
    F_TYPE x =  (* (F_TYPE *) a) - (* (F_TYPE *) b) ;
    return (x>0) ? 1 : (x<0) ? -1 : 0;
}

/*****
/*
/*          nrselect()
/*
/*      Fast Numerical Recipes function to find median of array
/*
/*
*****/

// Copied from on-line NR, Sec. 8.5 (later version than I have in book)
// Note: The NR working array arr[] indices go from 1 to n; arr[0] not used
// Note: The nrselect() array is just a float, but this precision S/B OK

// Local macro
#define SWAPP(a,b) temp=(a); (a)=(b); (b)=temp;

// Start of function - prototype is at top of this file - not in Stable_w.h
// This function returns the kth smallest value in the n-point array arr[]
// k is set to (n+1)/2 to find median
// About x10 faster than sorting - smaller elements moved in arbitrary order
float nrselect(unsigned long k, unsigned long n, float arr[])
{
    unsigned long i,ir,j,l,mid;
    float a,temp;

    l=1;
    ir=n;
    for(;;) {
        if (ir <= l+1) {
            if (ir == l+1 && arr[ir] < arr[l]) {
                SWAPP(arr[l],arr[ir])
            }
            return arr[k];
        } else {
            mid=(l+ir) >> 1;
            SWAPP(arr[mid],arr[l+1])
            if (arr[l] > arr[ir]) {
                SWAPP(arr[l],arr[ir])
            }
            if (arr[l+1] > arr[ir]) {
                SWAPP(arr[l+1],arr[ir])
            }
            if (arr[l] > arr[l+1]) {
                SWAPP(arr[l],arr[l+1])
            }
        }
    }
}

```

```

i=l+1;
j=ir;

a=arr[l+1];
for (;;) {
    do i++; while (arr[i] < a);
    do j--; while (arr[j] > a);
    if (j < i) break;
    SWAPP(arr[i],arr[j])
}
arr[l+1]=arr[j];
arr[j]=a;
if (j >=k) ir=j-1;
if (j <=k) l=i;
}
}
}

```



The FrequenC Library	
<b>NAME:</b> FindMinMax	<b>FUNCTION:</b> Find the minimum and maximum values of phase or frequency data
<b>SYNOPSIS:</b> int FindMinMax(F_TYPE z[], F_TYPE *p_min, F_TYPE *p_max, BOOL datatype)	
F_TYPE z[]	Phase or frequency data array: z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE *p_min	Pointer to minimum
F_TYPE *p_max	Pointer to maximum
BOOL datatype	Type of data: 0=phase, 1=frequency
<b>RETURN:</b> int	The # of analysis points (may be 0 if no non-gap data points)
<b>REMARKS:</b> Only data between start and end analysis limits are analyzed. All zeros are treated as gaps in frequency data. Only embedded gaps are treated as gaps in phase data. The datatype flag determines whether the data is treated as phase (datatype=0) or frequency (datatype=1) data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ F_TYPE min;  /* minimum value */ F_TYPE max;  /* maximum value */ BOOL datatype;                                       /* data type flag */ int num;   /* # analysis points */ . . datatype=FREQ;                                       /* set flag for frequency data */ /* frequenc.h contains #define PHASE 0 and #define FREQ 1 */ num=FindMinMax(z, &amp;min, &amp;max, datatype);           /* find min &amp; max */ printf("\nMin = %e", min);                          * display minimum */ printf("\nMax = %e", max);                          /* display maximum */ printf("\n# Points = %d, num);                      * display # analysis points */           </pre>	
<b>SEE ALSO:</b> FindPlotScale()	
<b>REFERENCE:</b> None	

## FrequenC Library Reference Manual

```

/*****
/*
/*          FindMinMax          */
/*
/*      Function to find min and max of phase or frequency data      */
/*
/*      Parameters:      F_TYPE z[]      = frequency data      */
/*                      z[0] = # data points      */
/*                      z[1] = analysis start      */
/*                      z[2] = analysis end      */
/*
/*                      F_TYPE *p_min = pointer to minimum data value      */
/*                      F_TYPE *p_max = pointer to maximum data value      */
/*                      BOOL  dtype = data type: 0=phase, 1=frequency      */
/*
/*      Notes:          All zero treated as gaps in frequency data.      */
/*                      Embedded zeros treated as gaps in phase data.      */
/*                      min & max set to 0 if no non-gap data points.      */
/*
/*      Return:         int              = # non-gap data points      */
/*
/*      Revision record:
/*          12/16/91      Created      */
/*          12/26/91      Changed to make dtype a parameter rather than      */
/*                      a global variable. Made function an int return-      */
/*                      ing # non-gap data points. y[] changed to z[].      */
/*          12/31/91      Renamed; min & max arguments reversed      */
/*          01/18/92      Edited title block      */
/*          01/19/92      Changed to min=max=0 if no non-gap data points      */
/*          02/20/92      Rewritten to eliminate use of MAXFLOAT      */
/*          02/03/96      Modified for use as Win 3.1 DLL      */
/*          01/01/98      Changes for MS VC++ compatibility & warnings      */
/*
/* (c) Copyright 1991-8  Hamilton Technical Services  All Rights Reserved  */
/*
*****/

```

```
#include "frequenc.h"
```

```

int __cdeclspec(dllexport) FAR PASCAL FindMinMax(F_TYPE z[], F_TYPE *p_min,
F_TYPE *p_max, BOOL dtype)
{
    int i;                                /* index */
    int num=0;                            /* # non-gap data points */
    BOOL flag=FALSE;                      /* flag to indicate 1st non-gap point found */

    *p_max = 0;                           /* initialize max & min to 0 */
    *p_min = 0;                           /* they will remain 0 if no non-gap data points */

    for( i = (int) (*(z+1)+2); i <= (int) (*(z+2)+2); i++)
    {
        if(*(z + i) || (!dtype && i==3) || (!dtype && i==z[0]+2))
        {
            if(flag)
            {
                if( *(z + i) > *p_max )
                {
                    *p_max = *(z + i);
                }
            }
        }
    }
}

```

```

        if( *(z + i) < *p_min )
        {
            *p_min = *(z + i);
        }
    }
else
    {
        *p_max = *(z + i);
        *p_min = *(z + i);
        flag = TRUE;
    }
    num++;
}

return(num);
}
/* end FindMinMax() */

```



The FrequenC Library	
<b>NAME:</b> FindPlotScale	<b>FUNCTION:</b> Find plot scale for phase or frequency data
<b>SYNOPSIS:</b> <pre>int FindPlotScale(F_TYPE min, F_TYPE max, F_TYPE *p_scale_min,                   F_TYPE *p_scale_max)</pre>	
F_TYPE min	Data minimum
F_TYPE max	Data maximum
F_TYPE *p_scale_min	Pointer to scale minimum
F_TYPE *p_scale_max	Pointer to scale maximum
<b>RETURN:</b> int	The # of scale tick intervals, or -1 if error
<b>REMARKS:</b> Error if min > max	
<b>EXAMPLE:</b> <pre>#include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* frequency data array */ F_TYPE min;   /* minimum value */ F_TYPE max;   /* maximum value */ F_TYPE scale_min;                                   /* scale min */ F_TYPE scale_max;                                   /* scale max */ int ticks;  /* # scale ticks */ . . FindMinMax(y, &amp;min, &amp;max, FREQ);                    /* find min &amp; max for data */ ticks=FindPlotScale(min, max, &amp;scale_min, &amp;scale_max);  * scale */ if(ticks==-1) {     printf("\nError");                               /* error message */ } else {     printf("\nScale Min = %e", scale_min);            /* display scale min */     printf("\nScale Max = %e", scale_max);            /* display scale max */     printf("\n# Tick Intervals = %d, ticks);          /* display # ticks */ } */ }</pre>	
<b>SEE ALSO:</b> FindMinMax()	
<b>REFERENCE:</b> None	

```

/*****
/*
/*          FindPlotScale()
/*
/*      Function to find scale factor for plotting phase or freq data
/*
/*      Parameters:      F_TYPE min          = minimum freq value
/*                      F_TYPE max          = maximum freq value
/*                      F_TYPE *p_scale_min = pointer to scale minimum
/*                      F_TYPE *p_scale_max = pointer to scale maximum
/*
/*      Return:          int = # tick intervals in scale,
/*                          or -1 if error
/*
/*
/*      Revision record:
/*          12/16/91      Created
/*          12/26/91      Changed to int returning # decades in scale
/*          12/31/91      Renamed
/*          01/04/91      Changed return value to # ticks
/*                          Added 4 and 8 tick choices
/*          01/05/92      Added range check & error code return if range NG
/*          01/15/92      Added 6 tick choice; changed to else if style
/*                          Changed to tighter range check logic at end
/*          01/16/92      (int) casts made floor() or ceil() to avoid O/F
/*                          Added e in fine tests; added 3 tick choice
/*                          Additional changes to range check/correction logic
/*          01/18/92      Edited title block
/*          01/22/92      Changed order of min and max parameter pairs
/*          02/17/92      Changed min & max params from pointers to values
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*
/* (c) Copyright 1991-8  Hamilton Technical Services  All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __cdeclspec(dllexport) FAR PASCAL FindPlotScale(F_TYPE min, F_TYPE max,
F_TYPE *p_scale_min, F_TYPE *p_scale_max)
{
    double range, log_range, coarse, fine, ticks;
    double full_scale, digits, e;
    int k;
    /* # ticks added */

    e=1e-6;
    /* error tolerance */
    range = max - min;

    if(range<=0)
    /* check for NG range */
    {
        *p_scale_min=0;
        *p_scale_max=0;
        return(-1);
        /* error code */
    }

    log_range = log10(range) + 100;
    coarse = floor(log_range);
    fine = log_range - coarse;

```

```

if(fine < log10(2)+e)
{
    ticks = 2;
}
/* end if */
else if(fine < log10(3)+e)
{
    ticks = 3;
}
/* end if */
else if(fine < log10(4)+e)
{
    ticks = 4;
}
/* end if */
else if(fine < log10(5)+e)
{
    ticks = 5;
}
/* end if */
else if(fine < log10(6)+e)
{
    ticks = 6;
}
/* end if */
else if(fine < log10(8)+e)
{
    ticks = 8;
}
/* end if */
else
{
    ticks = 10;
}
/* end else */

full_scale = pow(10, coarse - 100) * ticks;
if(log10(full_scale) >= 0)
{
    digits = floor(log10(full_scale));
}
/* end if */
else
{
    digits = ceil(log10(full_scale)) - 1;
}
/* end else */

if((min / pow(10, digits)) >= 0)
{
    *p_scale_min = floor(min / pow(10, digits)) * pow(10, digits);
}
/* end if */
else
{
    *p_scale_min = (floor(min / pow(10, digits))-1) * pow(10, digits);
}
/* end else */
*p_scale_max = *p_scale_min + full_scale;

k=0;

if(*p_scale_max < max)
/* check for scale max too small */
{
    while(*p_scale_max < max)
/* move scale up */
    {
        *p_scale_max += full_scale/ticks;
        *p_scale_min += full_scale/ticks;
    }
}

```

```

    if(*p_scale_min > min)
    {
        while(*p_scale_min > min)          /* add tic interval to max */
        {
            *p_scale_min -= full_scale/ticks;
            k++;
        }
    }

else if(*p_scale_min > min)                /* check for scale min too large */
{
    while(*p_scale_min > min)              /* move scale down */
    {
        *p_scale_max -= full_scale/ticks;
        *p_scale_min -= full_scale/ticks;
    }
    if(*p_scale_max < max)                  /* add tic interval to min */
    {
        while( *p_scale_max < max)
        {
            *p_scale_max += full_scale/ticks;
            k++;
        }
    }
}

ticks+=k;                                /* adjust # tic intervals */

return(int) ticks;

}                                          /* end FindPlotScale() */

```

The FrequenC Library	
<b>NAME:</b> HistoCalc	<b>FUNCTION:</b> Calculate histogram from phase or frequency data
<b>SYNOPSIS:</b> void HistoCalc(F_TYPE z[], float bins[], float hist[], F_TYPE *max, int num, BOOL datatype)	
F_TYPE z[]	Phase or frequency data array z[0] = # data points z[1] = analysis start point z[2] = analysis end point
float bins[]	Array of histogram bin values
float hist[]	Array of histogram count values
F_TYPE *max	Maximum z[] value
int num	# histogram bins
BOOL datatype	Date type (0=phase, 1=frequency)
<b>RETURN:</b> void	
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. Embedded zeros are treated as gaps in phase data. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ float *bins, hist;                                   /* pointers to float arrays */ F_TYPE z[512];                                       /* data array */ F_TYPE max;  /* data maximum */ int num=50;  /* # histo bins */  /* allocate bins[num] and hist[num] arrays */  HistoCalc(z, bins, hist, &amp;max, num, 1);              /* call function */ printf("\n# Histo Points = %d", num);              /* display num */ </pre>	
<b>SEE ALSO:</b>	
<b>REFERENCE:</b>	

```

/*****
/*
/*          HistoCalc()
/*
/*      Function to calculate histogram from frequency data
/*      Parameters:
/*          y[]          = analysis data;          y[0] = # data points
/*                  y[1] = analysis start; y[2] = analysis end
/*          bins[]       = histogram bin values
/*          hist[]       = histogram counts
/*          y_max        = maximum y[] value
/*          num_bins     = # histogram bins
/*          bDataType    = data type (0=phase, 1=frequency)
/*
/*
/*      Returns nothing (void)
/*
/*      Revision record:
/*          12/28/96      Adapted from Stable/DOS histo_calc() of STAB_F15.C
/*          12/29/96      Up and running
/*          12/30/96      Added gap handling (Histo never had that!)
/*          03/20/03      Adapted for FrequenC DLL
/*                  Added BOOL bDataType argument
/*          04/26/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1996-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

void __declspec(dllexport) FAR PASCAL HistoCalc(F_TYPE y[], float bins[],
float hist[], F_TYPE *y_max, int num_bins, BOOL bDataType)
{
    // Local variables
    int i;                                /* general index */
    int j;                                /* bin index */
    int points=(int)(y[2]-y[1]+1);        /* # analysis points */
    int offset=(int)(y[1]+2);             /* index of 1st analysis point */

    // Calc histogram of y[] values from [offset] to [points]
    // Using bins[] from [0] to [num_bins]
    // Counts of # data values/bin go into hist[] from [0] to [num_bins-1]
    // y_max keeps track of the largest bin count for the normal curve fit

    *y_max=0.0;

    for(i=offset; i<offset+points; i++)
    {
        if( y[i] || (bDataType==PHASE_DATA && i==3) ||
            (bDataType==PHASE_DATA && i==y[0]+2) )
        {
            for(j=0; j<num_bins; j++)
            {
                if(y[i]<=bins[j+1])
                {
                    hist[j]++;
                    if(hist[j]>*y_max)
                    {

```

}

}

}

}

}

}



The FrequenC Library	
<b>NAME:</b> HadamardEDF	<b>FUNCTION:</b> Description of what function does
<b>SYNOPSIS:</b> int FunctionName( F_TYPE z[], F_TYPE one, F_TYPE two)	
F_TYPE z[]	Phase or frequency data array z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE one	parameter one, and description of what it is
F_TYPE two	parameter two, and description of what it is
<b>RETURN:</b> int	# non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are modified. Embedded zeros are treated as gaps in phase data. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ F_TYPE one;  /* parameter one */ F_TYPE two;  /* parameter two */ int num;   /* # data points processed */ . . one=1.0;   /* set 1st parameter value */ two=2.0;   /* set 2nd parameter value */ num=FunctionName(z, one, two);                      /* call function */ printf("\n# Data Points Scaled = %d", num);         /* display num */ </pre>	
<b>SEE ALSO:</b> RelatedFunctionName()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*                      HadamardEDF()
/*
/*  Function to calc the estimated # of chi-squared degrees of freedom
/*  for the overlapping Hadamard variance of a power law noise process.
/*
/*  Parameters:      int N      = # phase data points
/*                  int m      = averaging factor
/*                  int b      = beta (-2 to -6)
/*
/*  Return:         float      = Hadamard edf
/*                          or -1 if error
/*
/*  Reference:      C. Greenhall, "Hadamard edf Algorithm", May 1999
/*                  (private communication via e-mail)
/*
/*  Revision Record:
/*      05/15/99    Created from hedf3.c per C. Greenhall suggestions
/*
/*  (c) Copyright 1999 Hamilton Technical Services  All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```
// Local function prototypes - not exported
```

```
double Rx(double t, int b);
```

```
double Log(double x);
```

```
float __declspec(dllexport) FAR PASCAL HadamardEDF(int N, int m, int b)
```

```

{
    // Local macros
    #define JMAX 100                // Max # terms to calc as sum
    #define SUM 0                   // Calc using sum
    #define BOUND 1                 // Calc using upper bound
    #define SMALL 2                 // Calc using smaller sum

    // Local variables
    int M=N-3*m;                   // M=N-3m
    int j;                         // Index
    int jmax;                      // Max j for summation
    int m_prime;                   // Smaller sum m
    int c;                         // Calculation type (SUM, BOUND or SMALL)
    double a0;                    // edf upper bound 1st term
    double a1;                    // edf upper bound 2nd term
    double edfinv;                // Inverse of Hadamard edf
    double r=0;                   // r(t)
    double r0;                    // r(0)
    double e;                     // edf summation term
    double t;                     // Argument of r(t)
    double p;                     // M/m

    // Check for allowed beta
    if(b<-6 || b>-2)
    {
        return -1;                // Error code
    }
}

```

```
// Check for enough points: N must be >3m
if(M<=0)
{
    return -1;                // Error code
}

// Find jmax
jmax=min(M, 3*m);

switch(b)                    // Different calc for each noise type
{
    case -2:                  // White FM
    {
        // Set r0
        r0=12;

        // Test jmax
        if(jmax<JMAX)        // Calc edf as sum
        {
            // Set calc type
            c=SUM;

            // Find sum
            for(j=1; j<=jmax; j++)
            {
                t=(double)j/(double)m;
                e=Rx(t, b);
                r+=e*e*(1-((double)j/(double)M));
            }
        }
    }
    else                      // Too many terms
    {
        // Test M
        if(M>=3*m)          // Calc edf as upper bound
        {
            // Set calc type
            c=BOUND;

            // Set coefficients
            a0=0.777778;    // 7/9
            a1=0.5;

        }
        else                  // Use smaller sum
        {
            // Set calc type
            c=SMALL;

            // Find nearest integer to JMAX/p
            p=(double)M/(double)m;
            m_prime=(int)((double)JMAX/p+0.5);

            // Calc sum using this m
            jmax=min(JMAX, 3*m_prime);
        }
    }
}
```

```

        // Find smaller sum
        for(j=1; j<=jmax; j++)
        {
            t=(double)j/(double)m_prime;
            e=Rx(t, b);
            r+=e*e*(1-((double)j/(double)JMAX));
        }
    }
}
break;

case -3:                                // Flicker FM
{
    // Set r0
    r0=13.49604;                        // 48*log(2)-18*log(3)

    // Test jmax
    if(jmax<JMAX)                        // Calc edf as sum
    {
        // Set calc type
        c=SUM;

        // Find sum
        for(j=1; j<=jmax; j++)
        {
            t=(double)j/(double)m;
            e=Rx(t, b);
            r+=e*e*(1-((double)j/(double)M));
        }
    }
    else                                // Too many terms
    {
        // Test M
        if(M>=3*m)                      // Calc edf as upper bound
        {
            // Set calc type
            c=BOUND;

            // Set coefficients
            a0=1.0;
            a1=0.62;
        }
        else                            // Use smaller sum
        {
            c=SMALL;

            // Find nearest integer to JMAX/p
            p=(double)M/(double)m;
            m_prime=(int)((double)JMAX/p+0.5);

            // Calc sum using this m
            jmax=min(JMAX, 3*m_prime);
        }
    }
}

```

```

        // Find smaller sum
        for(j=1; j<=jmax; j++)
        {
            t=(double)j/(double)m_prime;
            e=Rx(t, b);
            r+=e*e*(1-((double)j/(double)JMAX));
        }
    }
}
break;

case -4:                                // Random Walk FM
{
    // Set r0
    r0=12;

    // Test jmax
    if(jmax<JMAX)                        // Calc edf as sum
    {
        // Set calc type
        c=SUM;

        // Find sum
        for(j=1; j<=jmax; j++)
        {
            t=(double)j/(double)m;
            e=Rx(t, b);
            r+=e*e*(1-((double)j/(double)M));
        }
    }
    else                                // Too many terms
    {
        // Test M
        if(M>=3*m)                       // Calc edf as upper bound
        {
            // Set calc type
            c=BOUND;

            // Set coefficients
            a0=1.033334; // 31/30
            a1=0.607143; // 17/28
        }
        else                            // Use smaller sum
        {
            // Set calc type
            c=SMALL;

            // Find nearest integer to JMAX/p
            p=(double)M/(double)m;
            m_prime=(int)((double)JMAX/p+0.5);

            // Calc sum using this m
            jmax=min(JMAX, 3*m_prime);
        }
    }
}

```

```

        // Find smaller sum
        for(j=1; j<=jmax; j++)
        {
            t=(double)j/(double)m_prime;
            e=Rx(t, b);
            r+=e*e*(1-((double)j/(double)JMAX));
        }
    }
}
break;

case -5:                                // Flicker Walk FM
{
    // Set r0
    r0=44.89093;                        // -192*log(2)+162*log(3)

    // Test jmax
    if(jmax<JMAX)                        // Calc edf as sum
    {
        // Set calc type
        c=SUM;

        // Find sum
        for(j=1; j<=jmax; j++)
        {
            t=(double)j/(double)m;
            e=Rx(t, b);
            r+=e*e*(1-((double)j/(double)M));
        }
    }
    else                                // Too many terms
    {
        // Test M
        if(M>=3*m)                      // Calc edf as upper bound
        {
            // Set calc type
            c=BOUND;

            // Set coefficients
            a0=1.06;
            a1=0.53;
        }
        else                            // Use smaller sum
        {
            // Set calc type
            c=SMALL;

            // Find nearest integer to JMAX/p
            p=(double)M/(double)m;
            m_prime=(int)((double)JMAX/p+0.5);

            // Calc sum using this m
            jmax=min(JMAX, 3*m_prime);
        }
    }
}

```

```

        // Find smaller sum
        for(j=1; j<=jmax; j++)
        {
            t=(double)j/(double)m_prime;
            e=Rx(t, b);
            r+=e*e*(1-((double)j/(double)JMAX));
        }
    }
}
break;

case -6:                                // Random Run FM
{
    // Set r0
    r0=132;

    // Test jmax
    if(jmax<JMAX)                        // Calc edf as sum
    {
        // Set calc type
        c=SUM;

        // Find sum
        for(j=1; j<=jmax; j++)
        {
            t=(double)j/(double)m;
            e=Rx(t, b);
            r+=e*e*(1-((double)j/(double)M));
        }
    }
    else                                  // Too many terms
    {
        // Test M
        if(M>=3*m)                       // Calc edf as upper bound
        {
            // Set calc type
            c=BOUND;

            // Set coefficients
            a0=1.30;
            a1=0.54;
        }
        else                             // Use smaller sum
        {
            // Set calc type
            c=SMALL;

            // Find nearest integer to JMAX/p
            p=(double)M/(double)m;
            m_prime=(int)((double)JMAX/p+0.5);

            // Calc sum using this m
            jmax=min(JMAX, 3*m_prime);
        }
    }
}

```

```

        // Find smaller sum
        for(j=1; j<=jmax; j++)
        {
            t=(double)j/(double)m_prime;
            e=Rx(t, b);
            r+=e*e*(1-((double)j/(double)JMAX));
        }
    }
}
break;
}

switch(c) // Different way for each calc type
{
    case SUM: // Calc using sum
    {
        r*=2.0;
        r+=r0*r0;
        edfinv=r/(M*r0*r0);
    }
    break;

    case BOUND: // Calc using upper bound
    {
        p=(double)M/(double)m;
        edfinv=(1/p)*(a0-(a1/p));
    }
    break;

    case SMALL: // Calc using smaller sum
    {
        r*=2.0;
        r+=r0*r0;
        edfinv=r/(JMAX*r0*r0);
    }
    break;
}

return (float)(1/edfinv); // Return Hadamard edf
}

/*****
/*
/*                                     Rx()
/*
/* Function to calculate Rx(t,b) for Hamamard edf
/*
/* Parameters:    double t    = time (>0)
/*               int b       = beta (-2 to -6)
/*
/* Return:       double      = Rx(t,b)
/*
/* Revision Record:
/*      05/15/99    Created
/*
/* (c) Copyright 1999 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
double Rx(double t, int b)
{
    switch(b)          // Different expression for each noise type
    {
        case -2:      // White FM:  $R_x(t) = -|t|$ 
        {
            return -20*t+15*(t+1)+15*fabs(t-1)-6*(t+2)-6*fabs(t-2)+
                (t+3)+fabs(t-3);
        }

        case -3:      // Flicker FM:  $R_x(t) = t*t*\ln(|t|)$ 
        {
            return 20*t*t*log(t)-15*(t+1)*(t+1)*Log(t+1)-
                15*(t-1)*(t-1)*Log(fabs((t-1)))+
                6*(t+2)*(t+2)*Log((t+2))+
                6*(t-2)*(t-2)*Log(fabs((t-2)))-
                (t+3)*(t+3)*Log((t+3))-(t-3)*(t-3)*Log(fabs((t-3)));
        }

        case -4:      // Random Walk FM:  $R_x(t) = -|t|^3$ 
        {
            return 20*t*t*t-
                15*(t+1)*(t+1)*(t+1)-
                15*fabs((t-1)*(t-1)*(t-1))+
                6*(t+2)*(t+2)*(t+2)+
                6*fabs((t-2)*(t-2)*(t-2))-
                (t+3)*(t+3)*(t+3)-
                fabs((t-3)*(t-3)*(t-3));
        }

        case -5:      // Flicker Walk FM:  $R_x(t) = -t*t*t*t*\ln(|t|)$ 
        {
            return -20*t*t*t*t*log((t))+
                15*(t+1)*(t+1)*(t+1)*(t+1)*Log((t+1))+
                15*(t-1)*(t-1)*(t-1)*(t-1)*Log(fabs((t-1)))-
                6*(t+2)*(t+2)*(t+2)*(t+2)*Log((t+2))-
                6*(t-2)*(t-2)*(t-2)*(t-2)*Log(fabs((t-2)))+
                (t+3)*(t+3)*(t+3)*(t+3)*Log((t+3))+
                (t-3)*(t-3)*(t-3)*(t-3)*Log(fabs((t-3)));
        }

        case -6:      // Random Run FM:  $R_x(t) = -|t|^5$ 
        {
            return -20*t*t*t*t*t+
                15*(t+1)*(t+1)*(t+1)*(t+1)*(t+1)+
                15*fabs((t-1)*(t-1)*(t-1)*(t-1)*(t-1))-
                6*(t+2)*(t+2)*(t+2)*(t+2)*(t+2)-
                6*fabs((t-2)*(t-2)*(t-2)*(t-2)*(t-2))+
                (t+3)*(t+3)*(t+3)*(t+3)*(t+3)+
                fabs((t-3)*(t-3)*(t-3)*(t-3)*(t-3));
        }
    }
}
```

```

/*****
/*
/*                               Log()
/*
/*  Wrapper function for log(x) modified to return 0 for x=0
/*
/*  Parameters:    double x  = argument for log(x)
/*
/*  Return:       double    = log(x)
/*                               or 0 if x=0
/*
/*  Note: x can be 0 but must not be negative
/*
/*  Revision Record:
/*      05/10/99    Created
/*
/*  (c) Copyright 1999 Hamilton Technical Services  All Rights Reserved
/*
*****/

```

```

double Log(double x)
{
    if(x)
    {
        return log(x);
    }
    else
    {
        return 0;
    }
}

```

The FrequenC Library	
<b>NAME:</b> HadTotvarBias	<b>FUNCTION:</b> Description of what function does
<b>SYNOPSIS:</b> int FunctionName( F_TYPE z[], F_TYPE one, F_TYPE two)	
F_TYPE z[]	Phase or frequency data array z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE one	parameter one, and description of what it is
F_TYPE two	parameter two, and description of what it is
<b>RETURN:</b> int	# non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are modified. Embedded zeros are treated as gaps in phase data. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ F_TYPE one;  /* parameter one */ F_TYPE two;  /* parameter two */ int num;   /* # data points processed */ . . one=1.0;   /* set 1st parameter value */ two=2.0;   /* set 2nd parameter value */ num=FunctionName(z, one, two);                      /* call function */ printf("\n# Data Points Scaled = %d", num);         /* display num */ </pre>	
<b>SEE ALSO:</b> RelatedFunctionName()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*                                     HadTotvarBias()
/*
/*
/*      Function to calculate the Hadamard Totvar bias function
/*
/*
/*      Parameters:      int      nAlpha = noise type (-4 to 0)
/*
/*
/*
/*
/*      Return:          float fBias  = Mod Totvar bias factor
/*                          or -1 if error
/*
/*
/*      Note:  fBias is independent of T and tau, and depends only on the
/*              the noise type.  It is defined as  $a = [E\{TotHvar\}/E\{Hvar\}] - 1$ ,
/*              but is calculated and used here as simply the ratio.
/*              This fBias is exactly the same as that for MTOT, but a
/*              separate function is used just in case that should change,
/*              and because of the diffeent alphas that apply.
/*
/*
/*      Alpha      Noise      a      HTOT/HVAR = 1+a
/*      0          W FM      -0.005    0.995
/*      -1         F FM      -0.149    0.851
/*      -2         RW FM     -0.229    0.771
/*      -3         FW FM     -0.283    0.717
/*      -4         RR FM     -0.321    0.679
/*
/*
/*      The Hadamard Totvar bias factor is the ratio of the expected value
/*      HTOT to HVAR.  To correct a calculated Hadamard Totdev value for a
/*      certain noise type, divide the uncorrected Mod Totdev value by the
/*      square root of the bias factor returned by this function.
/*
/*
/*      Notes:          (1) This function applies to -4 >= alpha >= 0
/*                      (2) This function applies for all T/tau
/*
/*
/*      References:     (1) E-mail from D.A. Howe/NIST, 10/27/00
/*                      (2) Final draft of PTTI 2000 HTOT paper:
/*                          Final3-PTTI-00.pdf rcv'd 12/24/00
/*
/*
/*      Revision record:
/*      10/28/00      Created
/*      12/24/00      Revise coefficients per Ref. 2
/*
/*
/*      (c) Copyright 2000      Hamilton Technical Services      All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

float __declspec(dllexport) FAR PASCAL HadTotvarBias(int nAlpha)
{
    // Local variable
    float fBias;

    // Verify parameter
    if(nAlpha<-4 || nAlpha>0)
    {
        return (float) -1.0; // Error
    }
}

```

```
// Sort by noise type
switch(nAlpha)
{
    case 0: // W FM
    {
        fBias=(float) 0.995;
    }
    break;

    case -1: // F FM
    {
        fBias=(float) 0.851;
    }
    break;

    case -2: // RW FM
    {
        fBias=(float) 0.771;
    }
    break;

    case -3: // FW FM
    {
        fBias=(float) 0.717;
    }
    break;

    case -4: // RR FM
    {
        fBias=(float) 0.679;
    }
    break;
}

return (fBias);
}
```



The FrequenC Library	
<b>NAME:</b> HadTotvarCalc	<b>FUNCTION:</b> Calculate the Hadamard total deviation from frequency data
<b>SYNOPSIS:</b> int HadTotvarCalc(F_TYPE y[], F_TYPE *dev, int af, BOOL *abort, BOOL progress, void *ProgressFunc(int percent, char *msg))	
F_TYPE y[]	Frequency data array y[0] = # data points y[1] = analysis start point y[2] = analysis end point
F_TYPE *dev	Pointer to Hadamard total deviation
int af	Averaging factor
BOOL *abort	Pointer to abort flag
BOOL progress	Progress indicator flag
void *ProgressFunc	Pointer to progress indicator function with args int percent and char *msg
<b>RETURN:</b> int	# analysis points, or -1 if memory allocation error, or -2 if no result error
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. All zeros are treated as gaps in frequency data. This calculation is done with a new array that is deleted after the function closes. Use of the progress indicator is optional.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* freq data array */ F_TYPE dev;  /* Hadamard totdev */ int af=1;   /* averaging factor */ BOOL abort;   /* abort flag */ int num;   /* # data points processed */ . . num=HadTotCalc(y, &amp;dev, af, &amp;abort, FALSE, NULL); /* call function */ printf("\n# Data Points Analyzed = %d", num);      /* display num */ </pre>	
<b>SEE ALSO:</b> HadTotvarBias(), HadTotvarEDF()	
<b>REFERENCE:</b> D. Howe, et al, "A Total Estimator of the Hadamard Function Used for GPS Operations", Proc. 32th Meeting, November 2000.	

```

/*****
/*
/*                                     HadTotvarCalc()
/*
/*
/*      Function to calculate the Hadamard Total Variance from freq data.
/*      Uses uninverted even reflection of offset-removed freq data.
/*      This function uses fast inner loop algorithm.
/*
/*
/*      Parameters:      F_TYPE y[]      = freq data
/*                          y[0] = # data points
/*                          y[1] = analysis start
/*                          y[2] = analysis end
/*      F_TYPE *fHTDev = pointer to Hadamard Totdev
/*      int nAF        = averaging factor
/*      BOOL *bAbort   = pointer to abort flag
/*      BOOL bProgress = progress indicator flag
/*      void *ProgressFunction()
/*                          = pointer to progress indicator
/*                          function with args int nPercentDone
/*                          and char *szMessage
/*
/*
/*      Return:      int      = # Hadamard Totvar analysis points,
/*                          or -1 if memory alloc error
/*                          or -2 if no result error
/*
/*
/*      Notes:      1. Calculation is done entirely with a new array
/*                  that is deleted after this function closes.
/*                  2. Progress indicator is optional.
/*                  3. This is fast method, and it handles gaps.
/*
/*
/*      Overview:   Similar to mod totvar calc except freq instead of
/*                  phase data. Uses 3m-point subsequence from which
/*                  linear freq drift is removed before being doubly
/*                  extended by uninverted, even reflection at each end.
/*                  No tau argument needed. Different final scaling.
/*
/*
/*      Description: Given the freq data array y[], Had Totvar is
/*                  calculated using z[], which is computed from a
/*                  subsequence of y[] comprising 3m points, where m
/*                  the avg factor nAF. This subsequence is formed
/*                  from y[i] where i=n thru n+3m-1, where n is an
/*                  overall index that goes from 1 to the # of freq
/*                  data points nNum. The subsequence z[i] is found
/*                  from y[i] by removing the frequency drift by
/*                  subtracting the slope found by averaging the 1st
/*                  and last halves of the subsequence and dividing by
/*                  half the interval.
/*
/*
/*                  This subsequence is then extended at both ends by
/*                  an uninverted even reflection according to z(n-k)=
/*                  z(n+k-1) and z(n+3m+k-1)=z(n+3m-k) for k=1 thru 3m,
/*                  thus creating a new subsequence having a tripled
/*                  range from i=n-3m to i=n+6m-1.
/*
/*
/*                  Had Totvar is then calculated as the average of its
/*                  nNum-3m Totvar sub-estimates.
/*
/*
/*      Reference:   D. Howe, et al, "A Total Estimator of the Hadamard
/*                  Function Used for GPS Operations", Proc. 32th PTTI
/*                  Meeting, November 2000 (to be published).
*/

```

```

/*                                                                    */
/*      Revision record:                                              */
/*      10/28/00    Cloned from NewModTotvarCalc()                  */
/*      10/29/00    Running                                          */
/*      03/09/03    Made progress function and abprt flag arguments */
/*      03/14/03    Moved into FrequenC DLL                        */
/*                                                                    */
/*      Replaced GlobalAllocPtr() with malloc(), etc.              */
/*      04/26/03    Adapted for Version 2.0 source code documentation */
/*                                                                    */
/* (c) Copyright 2000-2003 Hamilton Technical Services All Rights Reserved */
/*                                                                    */
/*****

```

```

#include "frequenc.h"

```

```

int __declspec(dllexport) FAR PASCAL HadTotvarCalc(F_TYPE fY[], F_TYPE *fHTDev,
int nAF, BOOL *bAbort, BOOL bProgress,
void *ProgressFunction(int nPercentDone, char *szMessage))

```

```

{
    // Local variables
    int i;           // Main index
    int j;           // Auxiliary index
    int k;           // Inner index
    int m;           // Alias for averaging factor nAF
    int nNum;        // # points
    int nStart;      // Analysis start
    int nCount=0;    // # analysis points
    int nTic;        // Increment for progress indicator
    int nLast_i=0;   // Previous value of index

    double *fZ;      // Subsequence array pointer
    double fC1;      // Subsequence 1st half average
    double fC2;      // Subsequence 2nd half average
    double fC;       // Freq slope (drift)
    double fSum=0;    // Overall Had Totvar summation
    double fSubsum=0; // Subsequence Had Totvar summation
    double fTemp;     // Temporary data value

    double fZ1;      // 1st freq average
    double fZ2;      // 2nd freq average
    double fZ3;      // 3rd freq average

    // Initializations
    nStart=(int)fY[1]; // Analysis start point
    nNum=(int)(fY[2]-fY[1]+1); // # analysis freq data points = N
    m=nAF;             // Averaging factor

    nTic=(int)ceil(nNum/100); // Increment for progress report

    // Set fTemp to mean value of overall freq data
    CalcMean(fY, &fTemp, FREQ_DATA);

    // Start
    if(bProgress)
    {
        // Label progress bar
        ProgressFunction(0, "Calculating Hadamard Totdev");
    }
}

```

```

// Allocate 9m points of fZ[] working memory with index from 0 to 9m-1
// w/o array header (#, Start, End)
if((fZ=(double*)malloc((9*m)*sizeof(double)))==NULL)
{
    return(-1); // Error - memory reallocation failed
}

// Outer loop thru all nNum-3m+1 subsequences of 3m freq data points
// A subsequence will be processed during each iteration
// and the average used to find Had-Totvar
// This allows a max m of nNum/3

// To handle analysis limits, initialize index to nStart-1 not 0
// and end it before nStart-1-3*m+1 instead of nNum-3*m+1
for(i=nStart-1; i<nStart-1+nNum-3*m+1; i++)
{
    // Copy data subsequence into working array starting at index 3m
    // Note: The fY[] array needs offset for its header info
    for(j=0; j<3*m; j++)
    {
        // Test for gap (zero value)
        if(fY[i+j+ARRAY_OFFSET])
        {
            fZ[3*m+j]=fY[i+j+ARRAY_OFFSET];
            fTemp=fZ[3*m+j];
        }
        else
        {
            // Replace gap with interpolated value
            // if adjacent points are themselves not gaps
            if( (fY[i+j+ARRAY_OFFSET-1]) && (fY[i+j+ARRAY_OFFSET+1]) )
            {
                fZ[3*m+j]=
                    (fY[i+j+ARRAY_OFFSET-1]+fY[i+j+ARRAY_OFFSET+1])/2.0;
            }
            else
            {
                // For lack of a better idea,
                // replace gap with last OK value
                // or, if haven't found one, the overall mean value
                fZ[3*m+j]=fTemp;
            }
        }
    }
}

// Do removal of frequency drift
// Find slope fC by averaging the 1st and last halves of the subsequence
// subtracting them, and dividing by half the interval
fC1=0;
fC2=0;
for(j=0; j<3*m/2; j++)
{
    fC1+=fZ[3*m+j];
    fC2+=fZ[3*m+(int)ceil(3.0*(double)m/2.0)+j];
}
fC1/=(double)(3*m/2);
fC2/=(double)(3*m/2);
fC=(fC2-fC1)/ceil(3.0*(double)m/2.0);

```

```

// Then subtract slope from each point
for(j=0; j<3*m; j++)
{
    fZ[3*m+j]-=fC*(double)j;
}

// Do uninverted even reflection at bottom and top
for(j=0; j<3*m; j++)
{
    // Bottom reflection
    fZ[j]=fZ[6*m-1-j];

    // Top reflection
    fZ[6*m+j]=fZ[j];
}

// Calc Hvar for the fZ[] subsequence
// Will need to add gap testing and analysis limits
// This data array does not need an offset
// This code implements the summation of Eq(4) of the reference

// Initialize inner sum
fSubsum=0;

// We have a doubly-extended subsequence fZ[] of 9m points
// and are going to form m-point averages
// in 6m+1 groups of 3 (called fZ1, fZ2 and fZ3)
// from which all possible fully overlapping 2nd differences
// will be used to calculate Hadamard Totvar
// Note: Only 6m of the 6m+1 possible 2nd differences are used
// because the last one is a duplicate
// This implements Eq. 1 of the reference
for(j=0; j<6*m; j++)
{
    if(j==0)
    {
        // Find the 3 freq averages for the first 2nd difference
        // Initialize freq averages
        fZ1=0.0;
        fZ2=0.0;
        fZ3=0.0;

        // Sum freq averages for 1st 3 sets of m points
        // using points 0 thru m-1, m thru 2m-1 and 2m thru 3m-1
        // Note: These freq sums are divided by m = # points of each
        // sum in the 2nd difference expression below
        for(k=0; k<m; k++)
        {
            fZ1 += fZ[k];
            fZ2 += fZ[k+m];
            fZ3 += fZ[k+2*m];
        }
    }
    else
    {
        // Now do the rest of the points w/o summing all each time
        // Just subtract the old point and add the new one
        // Sum freq averages for 3 sets of m points
        // using points j thru j+m-1, j+m thru j+2m-1 and
        // j+2m thru j+3m-1
    }
}

```

```

        // Note: These freq sums are divided by m = # points of
        // each sum in the 2nd difference expression below
        fZ1 = fZ1 -fZ[j-1]      +fZ[j+m-1];
        fZ2 = fZ2 -fZ[j+m-1]    +fZ[j+2*m-1];
        fZ3 = fZ3 -fZ[j+2*m-1] +fZ[j+3*m-1];
    }

    // Calc 2nd diff of one of the rest of the 6m sets of 3 freq avgs
    fSubsum += SQR((fZ1 - 2*fZ2 + fZ3)/m);
}

// Scale the subsum and add it to overall sum
fSum+=fSubsum/(6*m);

// Increment the sum count
nCount++;

// Display progress
// Update when index has changed by at least tic amount
if(((i-nLast_i)>=nTic) && (bProgress))
{
    ProgressFunction((int) (0.5+100.0*i/(nNum-3*m)),
        "Calculating Hadamard Totdev");
    nLast_i=i;
}

// Check for abort
if(*bAbort)
{
    break;
}
}

// Free the subsequence array
free(fZ);

// Scale result - See Eq (4) of Reference
// Without gaps, nCount=nNum-3m
// Note: Divisor S/B 6
// But 3 gives result that agrees exactly with normal and overlapping
// Hadamard deviation for AF=1 for FREQ.DAT test data
// 6 OK for other AFs
// Results agree exactly with T.Peppler/NIST with 6 for all AFs
// So 6 is clearly right - low result for AF=1 is apparently a property of HTOT
fSum/=(6*nCount);

// Find Hadamard Totdev
if(nCount && fSum>0)
{
    *fHTDev=(F_TYPE) sqrt(fSum);
}
else // No result error
{
    *fHTDev=0.0;
    nCount=-2;
}

```

```
// Done
// Clear progress display
ProgressFunction(0, "");

return(nCount); // Return # freq analysis points
}
```



The FrequenC Library	
<b>NAME:</b> HadTotvarEDF	<b>FUNCTION:</b> Description of what function does
<b>SYNOPSIS:</b> int FunctionName( F_TYPE z[], F_TYPE one, F_TYPE two)	
F_TYPE z[]	Phase or frequency data array z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE one	parameter one, and description of what it is
F_TYPE two	parameter two, and description of what it is
<b>RETURN:</b> int	# non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are modified. Embedded zeros are treated as gaps in phase data. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ F_TYPE one;  /* parameter one */ F_TYPE two;  /* parameter two */ int num;   /* # data points processed */ . . one=1.0;   /* set 1st parameter value */ two=2.0;   /* set 2nd parameter value */ num=FunctionName(z, one, two);                      /* call function */ printf("\n# Data Points Scaled = %d", num);         /* display num */ </pre>	
<b>SEE ALSO:</b> RelatedFunctionName()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*                                     HadTotvarEDF()
/*
/* Function to determine the estimated # of chi-squared degrees of freedom
/* for the Hadamard total variance (HTOT) of a power law noise process.
/*
/* Params:          int    nAlpha = alpha
/*                  float fRatio = T/tau = N/m
/*                  where: N = # phase data points
/*                  m = avg factor = tau/tau0
/*
/* Return:          float edf = estimated degrees of freedom
/*                  or -1 if error
/*
/* The edf is modeled by the expression (T/tau)/[b0+b1(tau/T)], where:
/*
/* Alpha    Noise    b0    b1    Values per D. Howe, et.al
/*  0        W FM    0.559  1.004  12/24/00 draft of PTTI'00 paper
/* -1        F FM    0.868  1.140
/* -2        RW FM    0.938  1.696
/* -3        FW FM    0.974  2.554
/* -4        RR FM    1.276  3.149
/*
/* Notes:          (1) This function applies only to -4 >= alpha >= 0
/*                  (2) This function applies only for m > 16
/*                  (3) T is defined as tau0 * # phase data points
/*
/* References:      (1) E-Mail from D.A. Howe/NIST, 10/27/00
/*                  (2) Final draft of PTTI 2000 HTOT paper:
/*                      Final3-PTTI-00.pdf rcv'd 12/24/00
/*
/* Revision record:
/*      10/28/00    Created
/*      12/24/00    Revised per Ref. 2
/*
/* (c) Copyright 2000  Hamilton Technical Services    All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

float __declspec(dllexport) FAR PASCAL HadTotvarEDF(int nAlpha, float fRatio)
{
    // Local variables
    float fEDF;
    double b0;
    double b1;

    // Verify parameters
    if(nAlpha<-4 || nAlpha>0)
    {
        return -1.0; // Error
    }

    switch(nAlpha)
    {

```

```

case 0: // W FM noise
{
    b0=0.559;
    b1=1.004;
}
break;

case -1: // F FM noise
{
    b0=0.868;
    b1=1.140;
}
break;

case -2: // RW FM noise
{
    b0=0.938;
    b1=1.696;
}
break;

case -3: // FW FM noise
{
    b0=0.974;
    b1=2.554;
}
break;

case -4: // RR FM noise
{
    b0=1.276;
    b1=3.149;
}
break;
}

fEDF=(float)((fRatio)/(b0+(b1/fRatio)));
return fEDF;
}

```



The FrequenC Library	
<b>NAME:</b> JulianToDate	<b>FUNCTION:</b> Convert Julian day number to Gregorian date
<b>SYNOPSIS:</b> long JulianToDate(long jdate)	
long jdate	Julian day number
<b>RETURN:</b> long	Gregorian date (yyyymmdd)
<b>REMARKS:</b> Calls MakeDate()	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ long jdate;   /* Julian day # */ long gdate;   /* Gregorian date */ . . jdate=24050000;                                       /* set Julian day # */ gdate=JulianToDate(jdate);                           /* call function */ printf("\nGregorian Date = %ld", gdate);             /* display result */ </pre>	
<b>SEE ALSO:</b> DateToJulian(), MakeDate()	
<b>REFERENCE:</b>	

## FrequenC Library Reference Manual

```

/*****
/*
/*          JulianToDate()
/*
/*      Function to convert Julian day number to Gregorian date
/*
/*      Parameters: long    jdate    Julian day number
/*
/*      Return:      long          Gregorian date (yyyymmdd)
/*
/*      Revision record:
/*          07/17/97    Cloned from juldat() of Hammer Library
/*                      Changed error code to -1
/*
*****/

#include "frequenc.h"                                /* FrequenC Library header file */

long __declspec(dllexport) FAR PASCAL JulianToDate(long jdate)
{
    extern long int makdate();
    long int gdate; /* Gregorian Date (yyyymmdd) for given Julian Day */
    int mo, da, yr;
    long int td, tm, ty;

    if (jdate<=0L) /* if zero or negative, return -1 */
    {
        return (-1L);
    }

    jdate-=1721119L;
    ty=(4L*jdate-1L)/146097L;
    jdate=4L*jdate - 1L - 146097L*ty;
    td=jdate/4L;

    jdate=(4L*td+3)/1461L;
    td=4L*td + 3L - 1461L*jdate;
    td=(td+4L)/4L;

    tm=(5L*td - 3L)/153L;
    td=5L*td - 3L - 153L*tm;
    td=(td+5L)/5L;

    ty=100L*ty + jdate;
    if (tm<10L)
    {
        tm+=3L;
    }
    else
    {
        tm-=9L, ty++;
    }

    da=(int) td; mo=(int) tm; yr=(int) ty;
    gdate=MakeDate(mo, da, yr);

    return(gdate);
}

```

The FrequenC Library	
<b>NAME:</b> MedianDeviation	<b>FUNCTION:</b> Calculate the median absolute deviation from frequency data
<b>SYNOPSIS:</b> int MedDev(F_TYPE y[], float *mad)	
F_TYPE y[]	Frequency data array y[0] = # data points y[1] = analysis start point y[2] = analysis end point
float *mad	Pointer to median absolute deviation
<b>RETURN:</b> int	# analysis points (including filled gaps)
<b>REMARKS:</b> The median absolute deviation (MAD) is a robust statistic based on the median of the data. It is the median of the scaled absolute deviations of the data points from their median value, and is defined as $MAD = \text{Median} \{  y(i) - m  / 0.6745 \}$ , where $m = \text{Median} \{ y(i) \}$ , and the factor 0.6745 makes the MAD equal to the standard deviation for normally distributed data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* freq data array */ float mad;   /* median absolute deviation */ . . MedianDeviation(y, &amp;mad);                           /* call function */ printf("\nMAD = %e", mad);                          /* display results */ </pre>	
<b>SEE ALSO:</b> FindMedian()	
<b>REFERENCES:</b> (1) Gernot M.R. Winkler, "Introduction to Robust Statistics and Data Filtering, (2) D.B. Percival, "Use of Robust Statistical Techniques in Time Scale Formation.	

```

/*****
/*
/*          MedDev()
/*
/*      Function to calc median of absolute deviation from frequency data
/*      Based on Stable/DOS function F37 of STAB_F37.C
/*
/*      meddev = med { | x - Median | / 0.6745 }
/*
/*      Procedure for calculating meddev:
/*          1. Sort data
/*          2. Find Median of data
/*          3. Subtract Median from all data points
/*          4. Calculate absolute value of these differences
/*          5. Divide values by 0.6745 (This makes the expected value of
/*              meddev = the std dev for normally distributed data.)
/*          6. Resort data
/*          7. Find median value = meddev
/*      These operations are performed in-place on a working data array t[]
/*
/*      Parameters:
/*          y[]    = frequency data; y[0] = # data points
/*          y[1]    = analysis start; y[2] = analysis end
/*          p_mad   = pointer to median absolute deviation
/*          zero freq value treated as gap in data
/*      Returns num = # analysis points (including filled gaps)
/*
/*      References: (1) Gernot M.R. Winkler, "Introduction to Robust
/*                      Statistics and Data Filtering".
/*                  (2) D.B. Percival, "Use of Robust Statistical
/*                      Techniques in Time Scale Formation".
/*
/*      Revision record:
/*          01/14/95    Created
/*          01/15/95    Added 0.6745 factor for unbiased estimate
/*          04/30/96    Modified as MedDev() for Stable/Win
/*          01/01/98    Changes for MS VC++ compatibility & warnings
/*          04/26/03    Adapted for Version 2.0 source code documentation
/*
/*      (c) Copyright 1995-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```
// Declare comparison function - not exported
static int MedDevCompare(const void *a, const void *b);
```

```

int __declspec(dllexport) FAR PASCAL MedDev(F_TYPE y[], float *p_mad)
{
    int i;                                /* 1st index */
    int j=0;                              /* 2nd index */
    int start=(int)y[1];                  /* analysis start */
    int end=(int)y[2];                    /* analysis end */
    int num=(int)y[0];                     /* # data points */
    F_TYPE *t;                            /* pointer to temporary data storage array */
    F_TYPE med;                           /* median value */

```

```

// Allocate storage for temporary array
if((t=(F_TYPE *)malloc((num+3)*sizeof(F_TYPE)))==NULL)
    /* allocate temporary data storage space */
{
    return(1); /* error return */
} /* end if */

// Copy data
for(i=0; i<num+3; i++)
{
    t[i]=y[i]; /* copy data */
} /* end for */

// Fill any gaps in data
if(CountGaps(t, FREQ))
{
    FillGaps(t, FREQ); /* fill gaps */
} /* end if */

// Eliminate non-analysis points
for(i=start+2; i<=end+2; i++)
{
    t[j]=t[i];
    j++;
} /* end for */
num=end-start+1;

// Sort data into numerical order
qsort((void *)t, (size_t) num, sizeof(F_TYPE), MedDevCompare);

// Find median
if(num%2) /* is num odd? */
{
    med=t[num/2]; /* middle value */
} /* end if */
else
{
    /* n is even */
    med=(t[(num/2)-1]+t[num/2])/2.0; /* average of 2 middle values */
} /* end else */

// Subtract median, get absolute value and scale data points
for(i=0; i<num; i++)
{
    t[i]-=med;
    t[i]=fabs(t[i])/0.6745;
} /* end for */

// Resort data into numerical order
qsort((void *)t, (size_t) num, sizeof(F_TYPE), MedDevCompare);

// Find meddev
if(num%2) /* is num odd? */
{
    *p_med=(float)t[num/2]; /* middle value */
} /* end if */
else
{
    /* n is even */
    *p_med=(float)((t[(num/2)-1]+t[num/2])/2.0); /* avg of 2 mid values */
} /* end else */

```

```

    free(t);                                     /* deallocate temporary array */

    // Done
    return(num);                                /* # non-zero data points */
}                                                /* end MedDev() */

/*****
/*
/*      Comparison Function for qsort()
/*
/*
*****/

int MedDevCompare(const void *a, const void *b)
{
    F_TYPE x = (*(F_TYPE *) a) - (*(F_TYPE *) b) ;
    return (x>0) ? 1 : (x<0) ? -1 : 0;
}

```

The FrequenC Library	
<b>NAME:</b> MakeDate	<b>FUNCTION:</b> Make Gregorian date from month, day and year
<b>SYNOPSIS:</b> long MakeDate(int month, int day, int year)	
int month	Month (1-12)
int day	Day (1-31)
int year	Year (4-digit, e.g. 2003)
<b>RETURN:</b> long	Gregorian date (yyyymmdd)
<b>REMARKS:</b> Year must be 1900 or greater	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ long gdate;   /* Gregorian date */ int month;   /* month */ int day;   /* day */ int year;   /* year */ . . month=1;   /* set month */ day=1;   /* set day */ year=2003;   /* set year */ gdate=MakeDate(month, day, year);                 /* call function */ printf("\nDate = %ld", gdate);                     /* display results */ </pre>	
<b>SEE ALSO:</b> BreakDate()	
<b>REFERENCE:</b> None	

## FrequeNC Library Reference Manual

```

/*****
/*
/*          MakeDate()
/*
/*      Function to make Gregorian date from month, day and year
/*
/*      Parameters: int      mo      Month (1-12)
/*                  int      da      Day (1-31)
/*                  int      yr      Year (2 or 4-digit)
/*
/*      Return:      long          Gregorian date (yyyymmdd)
/*
/*      Revision record:
/*          07/17/97      Cloned from makdate() of Hammer Library
/*
*****/

#include "frequenc.h"                                /* FrequeNC Library header file */

long __declspec(dllexport) FAR PASCAL MakeDate(int mo, int da, int yr)
{
    yr = (yr<=100 ? yr+1900 : yr);
    return ((long int) yr*10000L + mo*100L + da);
}
```

The FrequenC Library	
<b>NAME:</b> MultitaperSpectrumCalc	<b>FUNCTION:</b> Description of what function does
<b>SYNOPSIS:</b> int FunctionName( F_TYPE z[], F_TYPE one, F_TYPE two)	
F_TYPE z[]	Phase or frequency data array z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE one	parameter one, and description of what it is
F_TYPE two	parameter two, and description of what it is
<b>RETURN:</b> int	# non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are modified. Embedded zeros are treated as gaps in phase data. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ F_TYPE one;  /* parameter one */ F_TYPE two;  /* parameter two */ int num;   /* # data points processed */ . . one=1.0;   /* set 1st parameter value */ two=2.0;   /* set 2nd parameter value */ num=FunctionName(z, one, two);                      /* call function */ printf("\n# Data Points Scaled = %d", num);        /* display num */ </pre>	
<b>SEE ALSO:</b> RelatedFunctionName()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*                                     MT.C                                     */
/*
/*                               ANSI C Code for Multitaper Spectral Analysis      */
/*
/*  A simple set of subroutines in ANSI-C are presented for multiple taper
/*  spectrum estimation. The multitaper approach provides an optimal spectrum
/*  estimate by minimizing spectral leakage while reducing the variance of the
/*  estimate by averaging orthogonal eigenspectrum estimates. The orthogonal
/*  tapers are Slepian np prolate functions used as tapers on the windowed time
/*  series. Since the taper functions are orthogonal, combining them to achieve
/*  an average spectrum does not introduce spurious correlations as standard
/*  smoothed single-taper estimates do. Furthermore, estimates of the degrees of
/*  freedom and F-test values at each frequency provide diagnostics for
/*  determining levels of confidence in narrow band (single frequency)
/*  periodicities. The program provided is portable and has been tested on both
/*  Unix and Macintosh systems.
/*
/*
/*  References:
/*  1. J.M. Lees and J. Park, "A C-Subroutine for Computing Multiple-Taper
/*    Spectral Analysis", Computers in Geoscience, Vol. 21, 1995, pp. 195-236.
/*  2. D.J. Thomson, "Spectrum Estimation and Harmonic Analysis", Proc. IEEE,
/*    Vol. 70, No. 9, September 1982, pp. 1055-1096.
/*  3. D.B. Percival and A.T. Walden, Spectral Analysis for Physical Applica-
/*    tions, Cambridge University Press, 1993.
/*
/*  Downloaded from: ftp://ftp.iamg.org/VOL21/v21-2-2.zip
/*
/*  Required project source files are JFOUR1.C, JREALFT.C, JTAP.C and JL.H
/*  The three C files are combined into this one.
/*  It is not necessary to invoke the JL.H header file
/*  All necessary macros and prototypes are included in this source file
/*
/*  Adapted by W. Riley, Hamilton Technical Services, as MTAP July 9, 2002
/*
/*
/*  Revision Record:
/*      07/19/02    Up-and running OK as separate program.
/*      07/20/02    Moved MTAP into Stable32 as Stable_c.c.
/*                  Made many revisions to adapt for Stable32 usage.
/*                  Basically working - getting reasonable plots.
/*      07/25/02    Trim down unwanted features
/*      03/15/03    Adapted for FrequenC DLL
/*      04/26/03    Adapted for Version 2.0 source code documentation
/*
/*  (c) 2002-3 W. Riley Hamilton Technical Services All Rights Reserved
/*
*****/

// Includes
#include "frequenc.h"
#include <stdio.h>
#include <stddef.h>
#include <stdlib.h>
#include <math.h>
#include <memory.h>

// Local Macros
#define PI 3.14159265358979
#define ABS(a) ((a) < (0) ? -(a) : (a))

```

```

#define MAX(a,b) ((a) >= (b) ? (a) : (b))
#define DIAG1 0
#define JM_ADD 0

// Memory allocation functions
float *alloc_fvec(long first , long last)
{
    float *v;
    v=(float *)malloc((size_t) ((last-first+1+JM_ADD)*sizeof(float)));
    return v-first+JM_ADD;
}

double *alloc_dvec(long first , long last)
{
    double *v;
    v=(double *)malloc((size_t) ((last-first+1+JM_ADD)*sizeof(double)));
    return v-first+JM_ADD;
}

int *alloc_ivec(long first , long last)
{
    int *v;
    v=(int *)malloc((size_t) ((last-first+1+JM_ADD)*sizeof(int)));
    return v-first+JM_ADD;
}

// Local function prototypes
int get_pow_2(int inum);
float get_cos_taper(int n, int k);
int adwait(double *sqr_spec, double *dcf, double *el, int nwin, int num_freq,
    double *ares, double *degf, double avar);
void get_F_values(double *sr, double *si, int nf, int nwin, float *Fvalue,
    double *b);
void do_mtap_spec(float *data, int npoints, int kind, int nwin, float np1,
    int inorm, float dt, float *ospec, int klen);
int hires(double *sqr_spec, double *el, int nwin, int num_freq, double *ares);
void jfour1(float data[], unsigned long nn, int isign);
void jrealft(float data[], unsigned long n, int isign);
int jtridib_(int *n, double *eps1, double *d, double *e, double *e2, double *lb,
    double *ub, int *m11, int *m, double *w, int *ind, int *ierr, double *rv4,
    double *rv5);
int jtinvit_(int *nm, int *n, double *d, double *e, double *e2, int *m,
    double *w, int *ind, double *z, int *ierr, double *rv1, double *rv2,
    double *rv3, double *rv4, double *rv6);
void mt_get_spec(float *series, int inum, int klength, float *amp);
int multitap(int n, int nwin, double *el, float np1, double *tapers,
    double *tapsum);
void zero_pad(float output[], int start, int olength);
double remove_mean(float *x, int lx);
float get_cos_taper(int n, int k);

/*****
/*
/*                               MultiTaperSpectrumCalc()
/*
/*  Function to calculate and plot multi-taper power spectrum, similar to
/*  SpectrumCalc() that uses ordinary periodogram method.
/*
/*
/*  Parameters:
/*      F_TYPE   y[]           = time-domain data; y[0] = *y = # data points
*****/

```

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```

/*      float      data[]      = real data points -> PSD results      */
/*      float      freq[]      = Fourier freq results                */
/*      float      dt          = time interval of data samples       */
/*      int         num_points  = # time series data points          */
/*      float      np1         = # pi-prolate functions              */
/*      int         nwin        = # summing windows                  */
/*      int         kind        = kind of analysis (way eigenspectra are combined)
/*                                1 = hires
/*                                2 = adwait
/*                                3 = naive periodogram
/*      int         inorm        = normalization method
/*                                1 = standard = npoints
/*                                2 = other = 1/dt
/*                                3 = sqrt(npoints)
/*      int         win_type     = windowing method code:
/*                                0 = Rectangular
/*                                1 = Hanning
/*                                2 = Hamming
/*      int         p_type       = phase_noise_type:
/*                                0 = Sx(f)
/*                                1 = So(f)
/*                                2 = L(f)
/*      float      corr_factor   = correction_factor to adjust PSD for carrier freq
/*      BOOL        bDataType    = data type:
/*                                0 = Phase
/*                                1 = Frequency
/*
/* Returns:
/*      int         num_freqs    = # FFT frequencies
/*
/* Note: Calling function must allocate the correct data & freq array size.
/* This size is 1+klen/2, where klen is twice the smallest power of 2
/* that encompasses the data (e.g. for 500 data points, klen is 1024 & array
/* size is 1+512=513).
/*
/* Revision record:
/*      07/20/02      Adapted from SpectrumCalc()
/*                    Objective is to call from SpectrumCalcDlgProc() instead of
/*                    SpectrumCalc() to offer multi-taper spectral analysis
/*      07/25/02      Eliminate O/P file and Fvalues calc
/*                    Eliminate naive spectrum calc
/*                    Eliminate dof calc and file
/*      07/30/02      Revised to handle analysis limits
/*      03/15/03      Adapted for FrequenC DLL
/*      03/16/03      Added bDataType parameter
/*                    Changed from void to int to return # freqs
/*      04/26/03      Adapted for Version 2.0 source code documentation
/*
/*****

```

```

int __declspec(dllexport) FAR PASCAL MultiTaperSpectrumCalc(F_TYPE y[],
float data[], float freq[], float dt, int num_points, float np1, int nwin,
int kind, int inorm, int win_type, int p_type, float corr_factor,
BOOL bDataType)
{
    // Local Variables
    // Ints
    int i;           // General index
    int k;
    int npoints;
    int klen;

```

```

int num_freqs;
int K;
int freqwin;
int increase;
int isign = 1;
int offset;           // Index of first data point to be analyzed

// Floats
float *spec;
float fWidth;
float df;
float nyquist;
float bw_corr;        // Bandwidth correction factor
float log_mult;       // Log PSD multiplier scale factor

// Doubles
double mean;

// WJR Notes re original input parameters 7/19/02
// name = input time series data filename
// np_i = order of pi-prolate taper functions
// Choose some small integer (j=2, 3 or 4)
// This sets resolution BW 2W
// W is set to a small multiple of the fundamental frequency 1/(N*Delta t)
// so W = j/(N*Delta t). See Percival & Walden p.335. Use 3.
// nwin = # summing windows (Percival recommends 6 for lowest bias) Use 5.
// kind = way the eigenspectra are combined
//   1 = hires=best for white noise
//   2 = adwait=optimal adaptive weights=best for colored noise
//   3 = naive periodogram
//   For our purposes, where colored noise is often encountered, use 2
// inorm=normalization method
//   1 = standard
//   2 = other
// So, our parameters are typically filename 3 5 2 1

// Input parameters
// dt = sampling interval
// num_points = # input points
// np_i = # pi-prolate functions
// nwin = # summing windows
// kind = kind of analysis
// inorm = normalization method

// Notes re parameters:
// See p. 335, Percival and Walden
// Choose np_i = 2,3,4 (some small integer)
// Then W = np_i/(num_points*dt) or num_points*W = np_i/dt
// K < 2*num_points*W*dt
// nwin = 0...K-1

// Calc BW params
fWidth=np_i/((float)num_points*dt);
K=(int) (2*num_points*fWidth*dt);

// Calc Nyquist frequency (2 samples/cycle)
nyquist=(float) (0.5/dt);

// Calc zero-padded power-of-2 data length
klen=get_pow_2(num_points);

```

```

increase=1;
klen=(int) (klen*pow((double)2, (double)increase)); // This doubles klen

// Calc # Fourier frequencies
num_freqs=1+klen/2;

// Data entry from array
// The xdata array gets loaded with the time domain data.
// This array is allocated with space for the # points & analysis limits.
// These are put into the xdata array initially to allow it to use the
// NewFillFloatGaps() function.
// Then the header info is removed from the xdata array for the FFT calcs.

// Find index of first data point to be analyzed
offset=(int)y[1]+2;

// Copy y[] analysis data into data[] with header info
data[0]=(float)num_points;
data[1]=1.0;
data[2]=(float)num_points;
for(i=0; i<num_points; i++)
{
    data[i+ARRAY_OFFSET]=(float)y[i+offset];
}

// Make sure no there are gaps in the time domain data
FillFloatGaps(data, bDataType);

// Eliminate header from analysis data
for(i=0; i<num_points; i++)
{
    data[i]=data[ARRAY_OFFSET+i];
}

npoints=i;
k=1;

// Remove average
mean=remove_mean(data, npoints);

df=2*nyquist/klen;
freqwin=(int) (fWidth/df)/2;

spec=alloc_fvec((long)0, (long)klen);

do_mtap_spec(data, npoints, kind, nwin, npi, inorm, dt, spec, klen);

// Must allocate correct size at calling function
for(i=1; i<num_freqs-1; i++) // Start index excludes dc component
{
    // Copy Fourier freqs to freq array
    freq[i-1]=df*i;
}

// Calc bandwidth correction
// Note: There are 2 other ways of doing this:
// 1. Use 2W where W=j/N*delta t
// 2. Normalize the results appropriately
bw_corr=(float)log10(freq[0]);

```

```

// Set log multiplier factor
if(p_type==2) // L(f)
{
    log_mult=10;
}
else // Sx(f) & So(f)
{
    log_mult=1;
}

// Convert spectral data to log form
// Note that data is PSD result & freq is Fourier freq
// for(i=0; i<num_freqs; i++)
for(i=1; i<num_freqs-1; i++) // Start index excludes dc component
{
    // Save power spectrum values plus correction factors
    data[i-1]=(float) (log_mult*(log10(spec[i]*corr_factor)- bw_corr));
}

// Save PSD data - eliminated 03/16/03 - now done by calling function
// PSDWrite(szPSDFile, freq, data, num_freqs-2);

// Free allocated arrays
free(spec);

// Done - return # freqs
return num_freqs;
}

/*-----*/
/*                               mt_get_spec                               */
/*-----*/

void mt_get_spec(float *series, int inum, int klength, float *amp)
{
    /* series = input time series */
    /* inum    = length of time series */
    /* klength = number of elements in power spectrum (a power of 2) */
    /* amp     = returned power spectrum */

    int i, isign = 1;
    unsigned long nn;
    nn = klength;

    /* copy amp onto series and apply zero padding to klength */
    for(i = 0; i < inum; i++)
    {
        amp[i] = series[i];
    }

    zero_pad(amp, inum, klength);

    /* Fast Fourier Transform Routine: here we are using the Numerical */
    /* Recipes routine jrealft which returns the fft in the 1-D input */
    /* array packed as pairs of real numbers. The jrealft routine */
    /* requires the input array to start at index=1 so we must decrement */
    /* the index of amp */
    jrealft(amp - 1, nn, isign);
}

```

```

/*-----*/
/*                                     do_mtap_spec                                     */
/*-----*/

void do_mtap_spec(float *data, int npoints, int kind, int nwin, float np_i,
    int inorm, float dt, float *ospec, int klen)
{
    /* data = floating point input time series */
    /* npoints = number of points in data */
    /* kind = flag for choosing hires or adaptive weighting coefficients */
    /* nwin = number of taper windows to calculate */
    /* np_i = order of the slepian functions */
    /* inorm = flag for choice of normalization */
    /* dt = sampling interval (time) ospec = output spectrum */
    /* klen = number of frequencies calculated (power of 2) */

    // Local variables
    int i, j, k;
    double *lambda, *tapers;
    FILE *fopen();
    float *b;
    int iwin, kk;
    double anrm, norm;
    double *ReSpec, *ImSpec;
    double *sqr_spec, *amu;
    float *amp;
    double avamp, temp, sqramp;
    double sum, *tapsum;
    int num_freqs;
    int len_taps, num_freq_tap;
    double *dcf, *degf, avar;
    int n1, n2, kf;

    /* lambda = vector of eigenvalues    tapsum = sum of each taper, saved */
    /* for use in adaptive weighting    tapers = matrix of slepian tapers */
    /* packed in a 1D double array */

    lambda = alloc_dvec((long)0, (long)nwin);
    tapsum = alloc_dvec((long)0, (long)nwin);
    len_taps = npoints * nwin;
    tapers = alloc_dvec((long)0, (long)len_taps);
    num_freqs = 1 + klen / 2;
    num_freq_tap = num_freqs * nwin;

    // Get a Slepian taper
    k = multitap(npoints, nwin, lambda, np_i, tapers, tapsum);

    // Choose normalization based on inorm flag
    anrm = 1.;

    switch(inorm)
    {
        case 1:
            anrm = npoints;
            break;
        case 2:
            anrm = 1 / dt;
            break;
        case 3:
            anrm = sqrt((double) npoints);
            break;
    }
}

```

```

default:
    anrm = 1.;
    break;

// Apply the taper in the loop. Do this nwin times
b = alloc_fvec((long)0, (long)npoints);
amu = alloc_dvec((long)0, (long)num_freqs);
sqr_spec = alloc_dvec((long)0, (long)num_freq_tap);
ReSpec = alloc_dvec((long)0, (long)num_freq_tap);
ImSpec = alloc_dvec((long)0, (long) num_freq_tap);

for(iwin = 0; iwin < nwin; iwin++)
{
    kk = iwin * npoints;
    kf = iwin * num_freqs;

    for(j = 0; j < npoints; j++)
    {
        // Application of iwin-th taper
        b[j] = (float)(data[j] * tapers[kk + j]);
    }

    amp = alloc_fvec((long)0, (long)klen);

    // Calculate the eigenspectrum
    mt_get_spec(b, npoints, klen, amp);

    // This causes error & program termination
    // Removed WJR 7/19/02 - Program then runs to completion
    // free(b);

    // New code to eliminate multiple free()s WJR 7/19/02
    if(iwin==nwin-1)
    {
        free(b);
    }

    sum = 0.0;

    /* get spectrum from real fourier transform */
    norm = 1.0 / (anrm * anrm);

    for(i = 1; i < num_freqs - 1; i++)
    {
        if(2 * i + 1 > klen)
        {
            fprintf(stderr, "error in index\n");
        }

        if(i + kf > num_freq_tap)
        {
            fprintf(stderr, "error in index\n");
        }

        sqramp = SQR(amp[2 * i + 1]) + SQR(amp[2 * i]);
        ReSpec[i + kf] = amp[2 * i];
        ImSpec[i + kf] = amp[2 * i + 1];
        sqr_spec[i + kf] = norm * (sqramp);
        sum += sqramp;
    }
}

```

```

sqr_spec[0 + kf] = norm * SQR(fabs(amp[0]));
sqr_spec[num_freqs - 1 + kf] = norm * SQR(fabs(amp[1]));
ReSpec[0 + kf] = amp[0];
ImSpec[0 + kf] = 0.0;
ReSpec[num_freqs - 1 + kf] = amp[1];
ImSpec[num_freqs - 1 + kf] = 0.0;
sum += sqr_spec[0 + kf] + sqr_spec[num_freqs - 1 + kf];

if(num_freqs - 1 + kf > num_freq_tap)
{
    fprintf(stderr, "error in index\n");
}

temp = sum / (double) num_freqs;

if(temp > 0.0)
{
    avamp = sqrt(temp) / anrm;
}
else
{
    avamp = 0.0;
    // fprintf(stderr, " avamp = 0.0! \n");
}

free(amp);
}

// Choice of hi-res or adaptive weighting for spectra
switch(kind)
{
    case 1:
    {
        hires(sqr_spec, lambda, nwin, num_freqs, amu);

        for(i = 0; i < num_freqs; i++)
        {
            ospec[i] = (float) (amu[i]);
        }
        break;
    }
    case 2:
    {
        /* get avar = variance */
        n1 = 0;
        n2 = npoints;
        avar = 0.0;

        for(i = n1; i < n2; i++)
        {
            avar += (data[i]) * (data[i]);
        }

        switch(inorm)
        {
            case 1:
            {
                #if(0) // Original code - NG for npoints >=65536 - get int O/F
                avar = avar / (npoints * npoints);
                #endif
            }
        }
    }
}

```

```

        #if(1) // New code - WJR - 07/28/02
        avar = avar / ((double)(npoints) * (double)(npoints));
        #endif
        break;
    }
    case 2:
    {
        avar = avar * dt * dt;
        break;
    }
    case 3:
    {
        avar = avar / npoints;
        break;
    }
    default:
    {
        break;
    }
}

dcf = alloc_dvec((long)0, (long)num_freq_tap);
degf = alloc_dvec((long)0, (long)num_freqs);
adwait(sqr_spec, dcf, lambda, nwin, num_freqs, amu, degf, avar);

// Wrap up
for(i = 0; i < num_freqs; i++)
{
    ospec[i] = (float)(amu[i]);
}

free(dcf);
free(degf);

break;
}

// Free up memory and return
free(amu);
free(sqr_spec);
free(ReSpec);
free(ImSpec);
free(lambda );
free(tapers);
}

/*-----*/
/*                                multitap                                */
/*-----*/

int multitap(int num_points, int nwin, double *lam, float np_i, double *tapers,
             double *tapsum)
{
    /* get the multitaper slepian functions: num_points = number of */
    /* points in data stream nwin = number of windows lam= vector of */
    /* eigenvalues np_i = order of slepian functions tapsum = sum of each */
    /* taper, saved for use in adaptive weighting tapers = matrix of */
    /* slepian tapers, packed in a 1D double array */

```

```

int i, k, kk;
double ww, cs, ai, an, eps, rlu, rlb, aa;
double dfac, drat, gamma, bh, tapsq, TWOPI, DPI;
double *diag, *offdiag, *offsq;
double *scratch1, *scratch2, *scratch3, *scratch4, *scratch6;

/* need to initialize iwflag = 0 */
double anpi;
double *ell;
int *ip;
double *evecs;
long len;
int ierr;
int m11;
DPI = (double) PI;
TWOPI = (double) 2 *DPI;
anpi = npi;
an = (double) (num_points);
ww = (double) (anpi) / an;          /* this corresponds to P&W's W value */
cs = cos(TWOPI * ww);
ell = alloc_dvec((long)0, (long) nwin );
diag = alloc_dvec((long)0, (long)num_points );
offdiag = alloc_dvec((long)0, (long)num_points );
offsq = alloc_dvec((long)0, (long)num_points );
scratch1 = alloc_dvec((long)0, (long)num_points );
scratch2 = alloc_dvec((long)0, (long)num_points );
scratch3 = alloc_dvec((long)0, (long)num_points );
scratch4 = alloc_dvec((long)0, (long)num_points );
scratch6 = alloc_dvec((long)0, (long)num_points );

// Make the diagonal elements of the tridiag matrix
for(i = 0; i < num_points; i++)
{
    ai = (double) (i);
    diag[i] = -cs * (((an - 1.) / 2. - ai)) * (((an - 1.) / 2. - ai));
    offdiag[i] = -ai * (an - ai) / 2.;
    offsq[i] = offdiag[i] * offdiag[i];
}

eps = 1.0e-13;
m11 = 1;
ip = alloc_ivec((long)0, (long) nwin);

// Call the eispac routines to invert the tridiagonal system
jtridib_(&num_points, &eps, diag, offdiag, offsq, &rlb, &rlu, &m11, &nwin,
        lam, ip, &ierr, scratch1, scratch2);

#ifdef DIAG1
fprintf(stderr, "ierr=%d rlb=%.8f rlu=%.8f\n", ierr, rlb, rlu);

fprintf(stderr, "eigenvalues for the eigentapers\n");

for(k = 0; k < nwin; k++)
{
    fprintf(stderr, "%.20f ", lam[k]);
}

fprintf(stderr, "\n");
#endif

```

```

len = num_points * nwin;
evecs = alloc_dvec( (long)0, (long)len);
jtinvt_(&num_points, &num_points, diag, offdiag, offsq, &nwin, lam, ip,
evecs, &ierr, scratch1, scratch2, scratch3, scratch4, scratch6);

free(scratch1);
free(scratch2);
free(scratch3);
free(scratch4);
free(scratch6);

    /* We calculate the eigenvalues of the Dirichlet-kernel problem i.e. */
    /* the bandwidth retention factors from Slepian 1978 asymptotic */
    /* formula, gotten from Thomson 1982 eq 2.5 supplemented by the */
    /* asymptotic formula for k near 2n from Slepian 1978 eq 61 more */
    /* precise values of these parameters, perhaps useful in adaptive */
    /* spectral estimation, can be calculated explicitly using the */
    /* Rayleigh-quotient formulas in Thomson (1982) and Park et al (1987) */

dfac = (double) an * DPI * ww;
drat = (double) 8. * dfac;
dfac = (double) 4. * sqrt(DPI * dfac) * exp((double) (-2.0) * dfac);

for(k = 0; k < nwin; k++)
{
    lam[k] = (double) 1.0 - (double) dfac;
    dfac = dfac * drat / (double) (k + 1);
    /* fails as k -> 2n */
}

gamma = log((double) 8. * an * sin((double) 2. * DPI * ww)) +
(double) 0.5772156649;

for (k = 0; k < nwin; k++)
{
    bh = -2. * DPI * (an * ww - (double) (k) /
(double) 2. - (double) .25) / gamma;
    ell[k] = (double) 1. / ((double) 1. + exp(DPI * (double) bh));
}

for (i = 0; i < nwin; i++)
{
    lam[i] = MAX(ell[i], lam[i]);
}

    /* Normalize the eigentapers to preserve power for a white process */
    /* i.e. they have rms value unity */
    /* tapsum is the average of the eigentaper, should be near zero for */
    /* antisymmetric tapers */

for(k = 0; k < nwin; k++)
{
    kk = (k) * num_points;
    tapsum[k] = 0.;
    tapsq = 0.;
}

```

```

    for(i = 0; i < num_points; i++)
    {
        aa = evecs[i + kk];
        tapers[i + kk] = aa;
        tapsum[k] = tapsum[k] + aa;
        tapsq = tapsq + aa * aa;
    }

    aa = sqrt(tapsq / (double) num_points);
    tapsum[k] = tapsum[k] / aa;

    for(i = 0; i < num_points; i++)
    {
        tapers[i + kk] = tapers[i + kk] / aa;
    }
}

/* Free Memory */
free(ell);
free(diag);
free(offdiag);
free(offsq);
free(ip);
free(evecs);

return 1;
}

/*-----*/
/*                                adwait                                */
/*-----*/

int adwait(double *sqr_spec, double *dcf, double *el, int nwin, int num_freq,
double *ares, double *degf, double avar)
{
    /* This version uses thomson's algorithm for calculating the */
    /* adaptive spectrum estimate */

    double as, das, tol, al, scale, ax, fn, fx;
    double *spw, *bias;
    double test_tol, dif;
    int jitter, i, k, kpoint, jloop;
    float df;

    /* Set tolerance for iterative scheme exit */

    #if(0)
    fprintf(stderr, "test input\n adwait: %d %d %f\n", nwin, num_freq, avar);
    fprintf(stderr, "\n Data=\n");
    for (i = 0; i < num_freq; i++)
    {
        fprintf(stderr, "%d %f \n", i, sqr_spec[i]);
    }
    #endif

    tol = 3.0e-4;
    jitter = 0;
    scale = avar;

```

```

/* We scale the bias by the total variance of the frequency transform */
/* from zero freq to the nyquist */
/* in this application we scale the eigenspectra by the bias to avoid */
/* possible floating point overflow */

spw = alloc_dvec((long)0, (long)nwin);
bias = alloc_dvec((long)0, (long)nwin);
for(i = 0; i < nwin; i++)
{
    bias[i] = (1.00 - el[i]);
}

#ifdef 0
for( i=1; i<=nwin; i++) fprintf(stderr, "%f %f\n", el[i], bias[i]);
fprintf(stderr, "\n");
#endif

// START do 100
for(jloop = 0; jloop < num_freq; jloop++)
{
    for(i = 0; i < nwin; i++)
    {
        kpoint = jloop + i * num_freq;
        spw[i] = (sqr_spec[kpoint]) / scale;
    }

    // First guess is the average of two lowest-order eigenspectral estimates
    as = (spw[0] + spw[1]) / 2.00;

    // START do 300
    // Find coefficients
    for(k = 0; k < 20; k++)
    {
        fn = 0.00;
        fx = 0.00;
        for(i = 0; i < nwin; i++)
        {
            a1 = sqrt(el[i]) * as / (el[i] * as + bias[i]);
            a1 = a1 * a1;
            fn = fn + a1 * spw[i];
            fx = fx + a1;
        }

        ax = fn / fx;
        dif = ax - as;
        das = ABS(dif);

        #if 0
        fprintf(stderr, "adwait: jloop = %d k=%d %g %g %g %g\n",
            jloop, k, fn, fx, ax, das);
        #endif

        test_tol = das / as;
        if(test_tol < tol)
        {
            break;
        }
        as = ax;
    }
}

```

```

    #if(0)
    fprintf(stderr, "adwait: k=%d test_tol=%f\n", k, test_tol);
    #endif

    /* end 300 */

    // Flag if iteration does not converge
    if(k >= 20)
    {
        jitter++;
    }
    ares[jloop] = as * scale;

    // Calculate degrees of freedom
    df = 0.0;
    for (i = 0; i < nwin; i++)
    {
        kpoint = jloop + i * num_freq;
        dcf[kpoint] = sqrt(el[i]) * as / (el[i] * as + bias[i]);
        df = (float)(df + dcf[kpoint] * dcf[kpoint]);
    }

    /* We normalize degrees of freedom by the weight of the first */
    /* eigenspectrum this way we never have fewer than two degrees of freedom */

    degf[jloop] = df * 2. / (dcf[jloop] * dcf[jloop]);

}

/* end 100 */

fprintf(stderr, "%d failed iterations\n", jitter);
free(spw);
free(bias);

return jitter;
}

/*-----*/
/*                               get_F_values                               */
/*-----*/

void get_F_values(double *sr, double *si, int nf, int nwin, float *Fvalue,
double *b)
{
    /* b is fft of slepian eigentapers at zero freq sr si are the */
    /* eigenspectra amu contains line frequency estimates and f-test parameter */

    double sum, sumr, sumi, sum2;
    int i, j, k;
    double *amur, *amui;
    sum = 0.;
    amur = alloc_dvec((long)0, (long)nf);
    amui = alloc_dvec((long)0, (long)nf);

    for(i = 0; i < nwin; i++)
    {
        sum = sum + b[i] * b[i];
    }

```

```

for(i = 0; i < nf; i++)
{
    amur[i] = 0.;
    amui[i] = 0.;

    for(j = 0; j < nwin; j++)
    {
        k = i + j * nf;
        amur[i] = amur[i] + sr[k] * b[j];
        amui[i] = amui[i] + si[k] * b[j];
    }

    amur[i] = amur[i] / sum;
    amui[i] = amui[i] / sum;
    sum2 = 0.;

    for(j = 0; j < nwin; j++)
    {
        k = i + j * nf;
        sumr = sr[k] - amur[i] * b[j];
        sumi = si[k] - amui[i] * b[j];
        sum2 = sum2 + sumr * sumr + sumi * sumi;
    }

    Fvalue[i] =
        (float)((nwin - 1) * (SQR(amui[i]) + SQR(amur[i])) * sum / sum2);
}

free(amur);
free(amui);
return;
}

/*-----*/
/*                                HIRES                                */
/*-----*/

int hires(double *sqr_spec, double *el, int nwin, int num_freq, double *ares)
{
    int i, j, k, kpoint;
    float a;

    for(j = 0; j < num_freq; j++)
    {
                                                                 ares[j] = 0.;
    }

    for(i = 0; i < nwin; i++)
    {
        k = i * num_freq;
        a = (float)(1. / (el[i] * nwin));

        for(j = 0; j < num_freq; j++)
        {
            kpoint = j + k;
            ares[j] = ares[j] + a * (sqr_spec[kpoint]);
        }
    }
}

```

```

for(j = 0; j < num_freq; j++)
{
    if (ares[j] > 0.0)
        ares[j] = sqrt(ares[j]);
    else
        printf("sqrt problem in hires pos=%d %f\n", j, ares[j]);
}

return 1;
}

/*-----*/
/*                               jtinvit                               */
/*-----*/

#include <math.h>
#define abs(x) ((x) >= 0 ? (x) : -(x))
#define dabs(x) (double)abs(x)
#define dmin(a,b) (double)min(a,b)
#define dmax(a,b) (double)max(a,b)

int jtinvit_(int *nm, int *n, double *d, double *e, double *e2, int *m,
double *w, int *ind, double *z, int *ierr, double *rv1, double *rv2,
double *rv3, double *rv4, double *rv6)
{
    // Initialized data
    static double machep = 1.25e-15;

    // System generated locals
    int z_dim1, z_offset, i1, i2, i3;
    double d1, d2;

    // Builtin functions
    double sqrt();

    // Local variables
    static double norm;
    static int i, j, p, q, r, s;
    static double u, v, order;
    static int group;
    static double x0, x1;
    static int ii, jj, ip;
    static double uk, xu;
    static int tag, its;
    static double eps2, eps3, eps4;
    static double rtem;

    /* This subroutine is a translation of the inverse iteration technique */
    /* in the Algol procedure tristurm by Peters and Wilkinson */
    /* Handbook for Auto. Comp., Vol.II-Linear Algebra, 418-439(1971). */
    /* This subroutine finds those eigenvectors of a tridiagonal symmetric */
    /* matrix corresponding to specified eigenvalues using inverse iteration. */
    /* On input: */
    /* nm must be set to the row dimension of two-dimensional array */
    /* parameters as declared in the calling program dimension statement */
    /* n is the order of the matrix */
    /* d contains the diagonal elements of the input matrix */
    /* e contains the subdiagonal elements of the input matrix in its last */
    /* n-1 positions */
    /* e(1) is arbitrary */

```

```

/* e2 contains the squares of the corresponding elements of e, with */
/* zeros corresponding to negligible elements of e */
/* e(i) is considered negligible if it is not larger than the product */
/* of the relative machine precision and the sum of the magnitudes of */
/* d(i) and d(i-1). */
/* e2(1) must contain 0.0d0 if the eigenvalues are in ascending order, */
/* or 2.0d0 if the eigenvalues are in descending order. If bisect, */
/* tridib, or imtqlv has been used to find the eigenvalues, their output */
/* e2 array is exactly what is expected here */
/* m is the number of specified eigenvalues */
/* w contains the m eigenvalues in ascending or descending order */
/* ind contains in its first m positions the submatrix indices */
/* associated with the corresponding eigenvalues in w -- */
/* 1 for eigenvalues belonging to the first submatrix from */
/* the top, 2 for those belonging to the second submatrix, etc. */
/* On output: */
/* all input arrays are unaltered */
/* z contains the associated set of orthonormal eigenvectors. */
/* any vector which fails to converge is set to zero */
/* ierr is set to: */
/* zero or normal return, */
/* -r if the eigenvector corresponding to the r-th */
/* eigenvalue fails to converge in 5 iterations */
/* rv1, rv2, rv3, rv4, and rv6 are temporary storage arrays. */
/* machep is a machine dependent parameter specifying */
/* the relative precision of floating point arithmetic. */
/* machep = 16.0d0**(-13) for long form arithmetic on s360 */
/* for f_floating dec fortran data machep/1.1d-16/ */
/* for g_floating dec fortran */
/*
/* Questions and comments should be directed to B. S. Garbow, */
/* Applied Mathematics Division, Argonne National Laboratory */

// Parameter adjustments
--rv6;
--rv4;
--rv3;
--rv2;
--rv1;
--e2;
--e;
--d;
z_dim1 = *nm;
z_offset = z_dim1 + 1;
z -= z_offset;
--ind;
--w;

// Function body
*ierr = 0;
if (*m == 0) {
    goto L1001;
}
tag = 0;
order = 1. - e2[1];
q = 0;
/* establish and process next submatrix */
L100:
p = q + 1;
il = *n;

```

```

for (q = p; q <= il; ++q) {
    if (q == *n) {
        goto L140;
    }
    if (e2[q + 1] == 0.) {
        goto L140;
    }
}

/* find vectors by inverse iteration */
L140:
++tag;
s = 0;
il = *m;
for (r = 1; r <= il; ++r) {
    if (ind[r] != tag) {
        goto L920;
    }
    its = 1;
    x1 = w[r];
    if (s != 0) {
        goto L510;
    }
    /* check for isolated root */
    xu = 1.;
    if (p != q) {
        goto L490;
    }
    rv6[p] = 1.;
    goto L870;
L490:
norm = (d1 = d[p], abs(d1));
ip = p + 1;
    i2 = q;
    for (i = ip; i <= i2; ++i) {
        norm = norm + (d1 = d[i], abs(d1)) + (d2 = e[i], abs(d2));
    }
    /* eps2 is the criterion for grouping, */
    /* eps3 replaces zero pivots and equal */
    /* roots are modified by eps3, */
    /* eps4 is taken very small to avoid overflow */
    eps2 = norm * .001;
    eps3 = machep * norm;
    uk = (double) (q - p + 1);
    eps4 = uk * eps3;
    uk = eps4 / sqrt(uk);
    s = p;
L505:
group = 0;
goto L520;
/* look for close or coincident roots */
L510:
if ((d1 = x1 - x0, abs(d1)) >= eps2) {
    goto L505;
}
++group;
if (order * (x1 - x0) <= 0.) {
    x1 = x0 + order * eps3;
}

```

```

/* elimination with interchanges and initialization of vector */
L520:
v = 0.;
i2 = q;
for (i = p; i <= i2; ++i) {
    rv6[i] = uk;
    if (i == p) {
        goto L560;
    }
    if ((d1 = e[i], abs(d1)) < abs(u)) {
        goto L540;
    }
    /* warning -- a divide check may occur here if */
    /* e2 array has not been specified correctly */
    xu = u / e[i];
    rv4[i] = xu;
    rv1[i - 1] = e[i];
    rv2[i - 1] = d[i] - x1;
    rv3[i - 1] = 0.;
    if (i != q) {
        rv3[i - 1] = e[i + 1];
    }
    u = v - xu * rv2[i - 1];
    v = -xu * rv3[i - 1];
    goto L580;
L540:
    xu = e[i] / u;
    rv4[i] = xu;
    rv1[i - 1] = u;
    rv2[i - 1] = v;
    rv3[i - 1] = 0.;
L560:
    u = d[i] - x1 - xu * v;
    if (i != q) {
        v = e[i + 1];
    }
L580:
    ;
}
if (u == 0.) {
    u = eps3;
}
rv1[q] = u;
rv2[q] = 0.;
rv3[q] = 0.;
/* back substitution for i=q step -1 until p do -- */
L600:
i2 = q;
for (ii = p; ii <= i2; ++ii) {
    i = p + q - ii;
    rtem = rv6[i] - u * rv2[i] - v * rv3[i];
    rv6[i] = (rtem) / rv1[i];
    v = u;
    u = rv6[i];
}

```

```

/* orthogonalize with respect to previous members of group */
if (group == 0) {
    goto L700;
}
j = r;
i2 = group;
for (jj = 1; jj <= i2; ++jj) {
    L630:
    --j;
    if (ind[j] != tag) {
        goto L630;
    }
    xu = 0.;
    i3 = q;
    for (i = p; i <= i3; ++i) {
        /* L640: */
        xu += rv6[i] * z[i + j * z_dim1];
    }
    i3 = q;
    for (i = p; i <= i3; ++i) {
        rv6[i] -= xu * z[i + j * z_dim1];
    }
}
L700:
norm = 0.;
i2 = q;
for (i = p; i <= i2; ++i) {
    norm += (d1 = rv6[i], abs(d1));
}
if (norm >= 1.) {
    goto L840;
}
/* forward substitution */
if (its == 5) {
    goto L830;
}
if (norm != 0.) {
    goto L740;
}
rv6[s] = eps4;
++s;
if (s > q) {
    s = p;
}
goto L780;
L740:
xu = eps4 / norm;
i2 = q;
for (i = p; i <= i2; ++i) {
    rv6[i] *= xu;
}
/* elimination operations on next vector */
/* iterate */
L780:
i2 = q;
for (i = ip; i <= i2; ++i) {
    u = rv6[i];

```

```

        /* if rv1(i-1) .eq. e(i), a row interchange was performed earlier */
        /* in the triangularization process */
        if (rv1[i - 1] != e[i]) {
            goto L800;
        }
        u = rv6[i - 1];
        rv6[i - 1] = rv6[i];
L800:
        rv6[i] = u - rv4[i] * rv6[i - 1];
    }
    ++its;
    goto L600;
    /* set error -- non-converged eigenvector */
L830:
    *ierr = -r;
    xu = 0.;
    goto L870;
    /* normalize so that sum of squares is 1 and expand to full order */
L840:
    u = 0.;
    i2 = q;
    for (i = p; i <= i2; ++i) {
        /* Computing 2nd power */
        d1 = rv6[i];
        u += d1 * d1;
    }
    xu = 1. / sqrt(u);
L870:
    i2 = *n;
    for (i = 1; i <= i2; ++i) {
        z[i + r * z_dim1] = 0.;
    }
    i2 = q;
    for (i = p; i <= i2; ++i) {
        z[i + r * z_dim1] = rv6[i] * xu;
    }
    x0 = x1;
L920:
    ;
}
if (q < *n) {
    goto L100;
}
L1001:
return 0;
}

```

```

/*-----*/
/*                                jtridib                                */
/*-----*/

int jtridib_(int *n, double *eps1, double *d, double *e, double *e2, double *lb,
double *ub, int *m11, int *m, double *w, int *ind, int *ierr, double *rv4,
double *rv5)
{
    // Initialized data
    static double machep = 1.25e-15;

    // System generated locals
    int i1, i2;
    double d1, d2, d3;

    // Local variables
    static int i, j, k, l, p, q, r, s;
    static double u, v;
    static int m1, m2;
    static double t1, t2, x0, x1;
    static int m22, ii;
    static double xu;
    static int isturm, tag;

    /* This subroutine is a translation of the Algol procedure bisect,
    /* Num. Math. 9, 386-393(1967) by Barth, Martin, and Wilkinson.
    /* Handbook for Auto. Comp., Vol.II-Linear Algebra, 249-256(1971).
    /* This subroutine finds those eigenvalues of a tridiagonal symmetric
    /* matrix between specified boundary indices, using bisection.
    /* On input:
    /*     n is the order of the matrix
    /*     eps1 is an absolute error tolerance for the computed eigenvalues.
    /*     if the input eps1 is non-positive, it is reset for each submatrix
    /*     to a default value, namely, minus the product of the relative machine
    /*     precision and the 1-norm of the submatrix
    /*     d contains the diagonal elements of the input matrix
    /*     e contains the subdiagonal elements of the input matrix
    /*     in its last n-1 positions.
    /*     e(1) is arbitrary
    /*     e2 contains the squares of the corresponding elements of e.
    /*     e2(1) is arbitrary
    /*     m11 specifies the lower boundary index for the desired eigenvalues
    /*     m specifies the number of eigenvalues desired. The upper boundary
    /*     index m22 is then obtained as m22=m11+m-1.
    /* On output:
    /*     eps1 is unaltered unless it was reset to its (last) default value
    /*     d and e are unaltered elements of e2, corresponding to elements of e
    /*     regarded as negligible, have been replaced by zero causing the
    /*     matrix to split into a direct sum of submatrices.
    /*     e2(1) is also set to zero
    /*     lb and ub define an interval containing exactly the desired
    /*     eigenvalues
    /*     w contains, in its first m positions, the eigenvalues between
    /*     indices m11 and m22 in ascending order
    /*     ind contains in its first m positions the submatrix indices
    /*     associated with the corresponding eigenvalues in w --
    /*     1 for eigenvalues belonging to the first submatrix from
    /*     the top, 2 for those belonging to the second submatrix, etc.
    /*     ierr is set to:
    /*         zero for normal return
    */

```

```

/*          3*n+1 if multiple eigenvalues at index m11 make unique          */
/*          selection impossible                                             */
/*          3*n+2 if multiple eigenvalues at index m22 make unique          */
/*          selection impossible                                             */
/* rv4 and rv5 are temporary storage arrays                                */
/* Note that subroutine tq11, imtq11, or tq1rat is generally faster than    */
/* tridib, if more than n/4 eigenvalues are to be found.                  */
/* machep is a machine dependent parameter specifying the relative precision */
/* of floating point arithmetic.                                            */
/* machep = 16.0d0**(-13) for long form arithmetic on s360                */
/* for f_floating dec fortran                                              */
/* data machep/1.1d-16/ for g_floating dec fortran                        */
/*                                                                            */
/* Questions and comments should be directed to B. S. Garbow,             */
/* Applied Mathematics Division, Argonne National Laboratory                */
/*                                                                            */

// Parameter adjustments
--rv5;
--rv4;
--e2;
--e;
--d;
--ind;
--w;

/* Function Body */

*iterr = 0;
tag = 0;
xu = d[1];
x0 = d[1];
u = 0.;
/* look for small sub-diagonal entries and determine an */
/* interval containing all the eigenvalues */
il = *n;
for (i = 1; i <= il; ++i) {
    x1 = u;
    u = 0.;
    if (i != *n) {
        u = (d1 = e[i + 1], abs(d1));
    }
    /* Computing MIN */
    d1 = d[i] - (x1 + u);
    xu = min(d1, xu);
    /* Computing MAX */
    d1 = d[i] + (x1 + u);
    x0 = max(d1, x0);
    if (i == 1) {
        goto L20;
    }
    if ((d1 = e[i], abs(d1)) > machep * ((d2 = d[i], abs(d2)) + (
        d3 = d[i - 1], abs(d3)))) {
        goto L40;
    }
    L20:
    e2[i] = 0.;
    L40:
    ;
}

```

```

/* Computing MAX */
d1 = abs(xu), d2 = abs(x0);
x1 = max(d1, d2) * machep * (double) (*n);
xu -= x1;
t1 = xu;
x0 += x1;
t2 = x0;
/* determine an interval containing exactly the desired eigenvalues */
p = 1;
q = *n;
m1 = *m11 - 1;
if (m1 == 0) {
    goto L75;
}
isturm = 1;
L50:
v = x1;
x1 = xu + (x0 - xu) * .5;
if (x1 == v) {
    goto L980;
}
goto L320;
L60:
if ((i1 = s - m1) < 0) {
    goto L65;
} else if (i1 == 0) {
    goto L73;
} else {
    goto L70;
}
L65:
xu = x1;
goto L50;
L70:
x0 = x1;
goto L50;
L73:
xu = x1;
t1 = x1;
L75:
m22 = m1 + *m;
if (m22 == *n) {
    goto L90;
}
x0 = t2;
isturm = 2;
goto L50;
L80:
if ((i1 = s - m22) < 0) {
    goto L65;
} else if (i1 == 0) {
    goto L85;
} else {
    goto L70;
}
L85:
t2 = x1;
L90:
q = 0;
r = 0;

```

```

/* establish and process next submatrix, refining */
/* interval by the gerschgorin bounds */
L100:
if (r == *m) {
    goto L1001;
}
++tag;
p = q + 1;
xu = d[p];
x0 = d[p];
u = 0.;
il = *n;
for (q = p; q <= il; ++q) {
    x1 = u;
    u = 0.;
    v = 0.;
    if (q == *n) {
        goto L110;
    }
    u = (d1 = e[q + 1], abs(d1));
    v = e2[q + 1];
L110:
    /* Computing MIN */
    d1 = d[q] - (x1 + u);
    xu = min(d1, xu);
    /* Computing MAX */
    d1 = d[q] + (x1 + u);
    x0 = max(d1, x0);
    if (v == 0.) {
        goto L140;
    }
}
L140:
/* Computing MAX */
d1 = abs(xu), d2 = abs(x0);
x1 = max(d1, d2) * machep;
if (*eps1 <= 0.) {
    *eps1 = -x1;
}
if (p != q) {
    goto L180;
}
/* check for isolated root within interval */
if (t1 > d[p] || d[p] >= t2) {
    goto L940;
}
m1 = p;
m2 = p;
rv5[p] = d[p];
goto L900;
L180:
x1 *= (double) (q - p + 1);
/* Computing MAX */
d1 = t1, d2 = xu - x1;
*lb = max(d1, d2);
/* Computing MIN */
d1 = t2, d2 = x0 + x1;
*ub = min(d1, d2);
x1 = *lb;
isturm = 3;

```

```

goto L320;
L200:
m1 = s + 1;
x1 = *ub;
isturm = 4;
goto L320;
L220:
m2 = s;
if (m1 > m2) {
    goto L940;
}
/* find roots by bisection */
x0 = *ub;
isturm = 5;
il = m2;
for (i = m1; i <= il; ++i) {
    rv5[i] = *ub;
    rv4[i] = *lb;
}
/* loop for k-th eigenvalue */
/* for k=m2 step -1 until m1 do */
/* do not used to legalize computed go to */
k = m2;
L250:
xu = *lb;
/* for i=k step -1 until m1 do */
il = k;
for (ii = m1; ii <= il; ++ii) {
    i = m1 + k - ii;
    if (xu >= rv4[i]) {
        goto L260;
    }
    xu = rv4[i];
    goto L280;
L260:
;
}
L280:
if (x0 > rv5[k]) {
    x0 = rv5[k];
}
/* next bisection step */
L300:
x1 = (xu + x0) * .5;
if (x0 - xu <= machep * 2. * (abs(xu) + abs(x0)) + abs(*eps1)) {
    goto L420;
}
/* in-line procedure for sturm sequence */
L320:
s = p - 1;
u = 1.;
il = q;
for (i = p; i <= il; ++i) {
    if (u != 0.) {
        goto L325;
    }
    v = (d1 = e[i], abs(d1)) / machep;
    if (e2[i] == 0.) {
        v = 0.;
    }
}

```

```

        goto L330;
L325:
    v = e2[i] / u;
L330:
    u = d[i] - x1 - v;
    if (u < 0.) {
        ++s;
    }
}
switch ((int) isturm) {
case 1:
    goto L60;
case 2:
    goto L80;
case 3:
    goto L200;
case 4:
    goto L220;
case 5:
    goto L360;
}
/* refine intervals */
L360:
if (s >= k) {
    goto L400;
}
xu = x1;
if (s >= m1) {
    goto L380;
}
rv4[m1] = x1;
goto L300;
L380:
rv4[s + 1] = x1;
if (rv5[s] > x1) {
    rv5[s] = x1;
}
goto L300;
L400:
x0 = x1;
goto L300;
/* k-th eigenvalue found */
L420:
rv5[k] = x1;
--k;
if (k >= m1) {
    goto L250;
}
/* order eigenvalues tagged with their submatrix associations */
L900:
s = r;
r = r + m2 - m1 + 1;
j = 1;
k = m1;
    il = r;
for (l = 1; l <= il; ++l) {
    if (j > s) {
        goto L910;
    }

```

```

    if (k > m2) {
        goto L940;
    }
    if (rv5[k] >= w[l]) {
        goto L915;
    }
    i2 = s;
    for (ii = j; ii <= i2; ++ii) {
        i = l + s - ii;
        w[i + 1] = w[i];
        ind[i + 1] = ind[i];
    }
    L910:
    w[l] = rv5[k];
    ind[l] = tag;
    ++k;
    goto L920;
    L915:
    ++j;
    L920:
    ;
}
L940:
if (q < *n) {
    goto L100;
}
goto L1001;
/* set error -- interval cannot be found containing */
/* exactly the desired eigenvalues */
L980:
*ierr = *n * 3 + isturm;
L1001:
*lb = t1;
*ub = t2;
return 0;
}

/*-----*/
/*-----get_pow_2-----*/
/*-----*/
int
get_pow_2(int inum)
{
    int j, klength;
    /* find smallest power of 2 that encompasses the data */

    for (j = 1; pow((double) 2, (double) j) < inum; j++);
    return klength = (int) (pow((double) 2, (double) j));
}

```

```

/*-----*/
/*-----remove_mean-----*/
/*-----*/

double remove_mean(float *x, int lx)
{
    int k;
    double mean;
    mean = 0.;

    if (lx < 2)
        return mean;

    for (k = 0; k <= lx; k++) {
        mean = x[k] + mean;
    }

    mean = mean / (float) lx;
    for (k = 0; k <= lx; k++) {
        x[k] = (float)(x[k] - mean);
    }

    return mean;
}

/*-----*/
/*-----zero_pad-----*/
/*-----*/

void zero_pad(float output[], int start, int olength)
{
    int i;
    for (i = start; i < olength; i++) {
        output[i] = 0.0;
    }
}

/*-----*/
/*-----get_cos_taper-----*/
/*-----*/

float get_cos_taper(int n, int k)
{
    int l;
    float vwin;
    vwin = 0.0;

    if (k < 0 || k > n)
        return vwin;
    vwin = 1.0;

    l = (n - 2) / 10;
    if (k <= l)
        vwin = (float)(0.5 * (1.0 - cos(k * PI / (l + 1))));
    if (k >= n - l - 2)
        vwin = (float)(0.5 * (1.0 - cos((n - k - 1) * PI / (l + 1))));

    return vwin;
}

```

```

/*****
/*
/* File JREALFT.C
/*
*****/

#include <math.h>

void jrealft(float data[], unsigned long n, int isign)
{
    void jfour1(float data[], unsigned long nn, int isign);
    unsigned long i,i1,i2,i3,i4,np3;
    float c1=0.5,c2,h1r,h1i,h2r,h2i;
    double wr,wi,wpr,wpi,wtemp,theta;

    theta=3.141592653589793/(double) (n>>1);
    if (isign == 1) {
        c2 = -0.5;
        jfour1(data,n>>1,1);
    } else {
        c2=0.5;
        theta = -theta;
    }
    wtemp=sin(0.5*theta);
    wpr = -2.0*wtemp*wtemp;
    wpi=sin(theta);
    wr=1.0+wpr;
    wi=wpi;
    np3=n+3;
    for (i=2;i<=(n>>2);i++) {
        i4=1+(i3=np3-(i2=1+(i1=i+i-1)));
        h1r=c1*(data[i1]+data[i3]);
        h1i=c1*(data[i2]-data[i4]);
        h2r = -c2*(data[i2]+data[i4]);
        h2i=c2*(data[i1]-data[i3]);
        data[i1]=(float) (h1r+wr*h2r-wi*h2i);
        data[i2]=(float) (h1i+wr*h2i+wi*h2r);
        data[i3]=(float) (h1r-wr*h2r+wi*h2i);
        data[i4]=(float) (-h1i+wr*h2i+wi*h2r);
        wr=(wtemp=wr)*wpr-wi*wpi+wr;
        wi=wi*wpr+wtemp*wpi+wi;
    }
    if (isign == 1) {
        data[1] = (h1r=data[1])+data[2];
        data[2] = h1r-data[2];
    } else {
        data[1]=c1*((h1r=data[1])+data[2]);
        data[2]=c1*(h1r-data[2]);
        jfour1(data,n>>1,-1);
    }
}

```

```

/*****
/*
/* File JFOUR1.C
/*
*****/

#include <math.h>
#define SWAP(a,b)  tempr=(a); (a)=(b); (b)=tempr

void jfour1(float data[], unsigned long nn, int isign)
{
    unsigned long n,mmax,m,j,istep,i;
    double wtemp,wr,wpr,wpi,wi,theta;
    float tempr,tempi;

    n=nn << 1;
    j=1;
    for (i=1;i<n;i+=2) {
        if (j > i) {
            SWAP(data[j],data[i]);
            SWAP(data[j+1],data[i+1]);
        }
        m=n >> 1;
        while (m >= 2 && j > m) {
            j -= m;
            m >>= 1;
        }
        j += m;
    }
    mmax=2;
    while (n > mmax) {
        istep=mmax << 1;
        theta=isign*(6.28318530717959/mmax);
        wtemp=sin(0.5*theta);
        wpr = -2.0*wtemp*wtemp;
        wpi=sin(theta);
        wr=1.0;
        wi=0.0;
        for (m=1;m<mmax;m+=2) {
            for (i=m;i<=n;i+=istep) {
                j=i+mmax;
                tempr=(float) (wr*data[j]-wi*data[j+1]);
                tempi=(float) (wr*data[j+1]+wi*data[j]);
                data[j]=data[i]-tempr;
                data[j+1]=data[i+1]-tempi;
                data[i] += tempr;
                data[i+1] += tempi;
            }
            wr=(wtemp=wr)*wpr-wi*wpi+wr;
            wi=wi*wpr+wtemp*wpi+wi;
        }
        mmax=istep;
    }
}

#undef SWAP

```



The FrequenC Library	
<b>NAME:</b> ModTotvarBias	<b>FUNCTION:</b> Description of what function does
<b>SYNOPSIS:</b> int FunctionName( F_TYPE z[], F_TYPE one, F_TYPE two)	
F_TYPE z[]	Phase or frequency data array z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE one	parameter one, and description of what it is
F_TYPE two	parameter two, and description of what it is
<b>RETURN:</b> int	# non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are modified. Embedded zeros are treated as gaps in phase data. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ F_TYPE one;  /* parameter one */ F_TYPE two;  /* parameter two */ int num;   /* # data points processed */ . . one=1.0;   /* set 1st parameter value */ two=2.0;   /* set 2nd parameter value */ num=FunctionName(z, one, two);                      /* call function */ printf("\n# Data Points Scaled = %d", num);        /* display num */ </pre>	
<b>SEE ALSO:</b> RelatedFunctionName()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*                               ModTotvarBias()
/*
/*                               Function to calculate the Mod Totvar bias function
/*
/*                               Parameters:      int    nAlpha = noise type (-2 to +2)
/*
/*
/*                               Return:          float fBias  = Mod Totvar bias factor
/*
/*                                           or -1 if error
/*
/*
/*                               Alpha      Noise      MTOT/MVAR
/*                               +2         W PM       0.94
/*                               +1         F PM       0.83
/*                               0          W FM       0.73
/*                               -1         F FM       0.70
/*                               -2         RW FM       0.69
/*
/*                               The Mod Totvar bias factor is the ratio of the expected value of
/*                               MTOT to MVAR. To correct a calculated Mod Totdev value for a
/*                               certain noise type, divide the uncorrected Mod Totdev value by the
/*                               square root of the bias factor returned by this function.
/*
/*                               Notes:           (1) This function applies to -2 >= alpha >= 2
/*
/*                                           (W PM, F PM, W FM, F FM, RW FM noise)
/*
/*                                           (2) This function applies for all T/tau
/*
/*                               Reference:       E-mail from D.A. Howe/NIST, 3/13/00
/*
/*                               Revision record:
/*                               03/25/00 Created
/*                               05/05/00 Corrected values per D. Howe e-mail
/*
/* (c) Copyright 2000 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

float __declspec(dllexport) FAR PASCAL ModTotvarBias(int nAlpha)
{
    // Local variable
    float fBias;

    // Verify parameter
    if(nAlpha<-2 || nAlpha>2)
    {
        return (float) -1.0; // Error
    }

    // Sort by noise type
    switch(nAlpha)
    {
        case -2: // RW FM
        {
            fBias=(float) 0.69;
        }
        break;
    }
}

```

```

case -1: // F FM
{
    fBias=(float) 0.70;
}
break;

case -0: // W FM
{
    fBias=(float) 0.73;
}
break;

case 1: // F PM
{
    fBias=(float) 0.83;
}
break;

case 2: // W PM
{
    fBias=(float) 0.94;
}
break;
}

return (fBias);
}

```



The FrequenC Library	
<b>NAME:</b> ModTotvarCalc	<b>FUNCTION:</b> Description of what function does
<b>SYNOPSIS:</b> int FunctionName( F_TYPE z[], F_TYPE one, F_TYPE two)	
F_TYPE z[]	Phase or frequency data array z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE one	parameter one, and description of what it is
F_TYPE two	parameter two, and description of what it is
<b>RETURN:</b> int	# non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are modified. Embedded zeros are treated as gaps in phase data. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ F_TYPE one;  /* parameter one */ F_TYPE two;  /* parameter two */ int num;   /* # data points processed */ . . one=1.0;   /* set 1st parameter value */ two=2.0;   /* set 2nd parameter value */ num=FunctionName(z, one, two);                      /* call function */ printf("\n# Data Points Scaled = %d", num);         /* display num */ </pre>	
<b>SEE ALSO:</b> RelatedFunctionName()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*                                     ModTotvarCalc()
/*
/*      Function to calculate the Modified Total Variance from phase data
/*      Uses uninverted even reflection of offset-removed phase data
/*
/*      Parameters:      F_TYPE x[]      = phase data
/*                        x[0] = # data points
/*                        x[1] = analysis start
/*                        x[2] = analysis end
/*
/*                        F_TYPE *fMTDev = pointer to Mod Totdev
/*                        F_TYPE fTau    = interval between phase data points
/*                        int nAF        = averaging factor
/*                        BOOL *bAbort   = pointer to abort flag
/*                        BOOL bProgress = progress indicator flag
/*                        void *ProgressFunction()
/*
/*                        = pointer to progress indicator
/*                        funct with args int nPercentDone
/*                        and char *szMessage
/*
/*      Return:      int      = # Mod Totvar analysis points,
/*                          or -1 if memory alloc error
/*                          or -2 if no result error
/*
/*      Notes:      1. Calculation is done entirely with a new array.
/*                  that is deleted after this function closes.
/*                  2. Progress indicator and abort not necessary.
/*                  3. The phase data need not be endmatched before
/*                     calling this function.
/*
/*      Description: Given the phase data array x[], Mod Totvar is
/*                  calculated using z[], which is computed from a
/*                  subsequence of x[] consisting of 3m points, where
/*                  m is the averaging factor nAF. This subsequence is
/*                  given by x[i] where i=n thru n+3m-1, where n is an
/*                  overall index that goes from 1 to the # of phase
/*                  data points nNum. The subsequence z[i] is found
/*                  from x[i] by removing the frequency offset by
/*                  subtracting the slope found by averaging the 1st
/*                  and last halves of the subsequence and dividing by
/*                  half the interval.
/*
/*                  This subsequence is then extended at both ends by
/*                  an uninverted even reflection according to z(n-k)=
/*                  z(n+k-1) and z(n+3m+k-1)=z(n+3m-k) for k=1 thru 3m,
/*                  thus creating a new subsequence having a tripled
/*                  range from i=n-3m to i=n+6m-1.
/*
/*                  Mod Totvar is then calculated as the average of its
/*                  nNum-3m Totvar sub-estimates.
/*
/*      Reference:   D.A. Howe and F. Vernotte, "Generalization of the
/*                  Total Variance Approach to the Modified Allan
/*                  Variance", Proc. 31th PTTI Meeting, Dec. 9, 1999,
/*                  (to be published).
/*
/*      Revision record:
/*      12/12/99    Adapted from TotvarCalc() and CalcPhaseModSigma()
/*                  of FrequenC Library.

```

```

/*      12/16/99      Basic code drafted - no gaps or analysis limits      */
/*      12/26/99      Changed progress bar argument from lpfm to flag      */
/*      12/30/99      Fixed & cleaned up a few details                    */
/*      02/06/00      Changed to fully overlapping per D. Howe review     */
/*      02/08/00      Changed inner sum index limit from 6m+1 to 6m to    */
/*                      elim duplicate term, and change divisor to 6m      */
/*      02/12/00      Added trace code to aid debugging                  */
/*      02/23/00      Added alternative freq offset removal method        */
/*      05/06/00      Added code to handle analysis limits                */
/*                      Not sure about gaps - no specific code for them    */
/*                      But seems like they S/B OK as-is                   */
/*      03/09/03      Added abort and progress args                      */
/*                      Changed from GlobalAllocPtr() to malloc()          */
/*
/* (c) Copyright 1999-2003  Hamilton Technical Services  All Rights Reserved */
/*
/*****

```

```

#include "frequenc.h"

```

```

int __cdeclspec(dllexport) FAR PASCAL ModTotvarCalc(F_TYPE fX[], F_TYPE *fMTDev,
F_TYPE fTau, int nAF, BOOL *bAbort, BOOL bProgress,
void *ProgressFunction(int nPercentDone, char *szMessage))
{
    // Local variables
    int i;           // Main index
    int j;           // Auxiliary index
    int k;           // Inner index
    int m;           // Alias for averaging factor nAF
    int nNum;        // # points
    int nStart;      // Analysis start
    int nCount=0;    // # analysis points
    int nTic;        // Increment for progress indicator
    int nLast_i=0;   // Previous value of index

    double *fZ;      // Subsequence array pointer
    double fC1;      // Subsequence 1st half average
    double fC2;      // Subsequence 2nd half average
    double fC;       // Phase slope=frequency offset
    double fSum=0;    // Overall Mod Totvar summation
    double fSubsum=0; // Subsequence Mod Totvar summation

    double fZ1;      // 1st phase average
    double fZ2;      // 2nd phase average
    double fZ3;      // 3rd phase average

    // Initializations
    nStart=(int)fX[1]; // Analysis start point
    nNum=(int)(fX[2]-fX[1]+1); // # analysis phase data points = N
    m=nAF;            // Averaging factor

    nTic=(int)ceil(nNum/100); // Increment for progress report

    // Start
    if(bProgress)
    {
        // Label progress bar
        ProgressFunction(0, "Calculating Mod Totdev");
    }
}

```

```

// Allocate 9m points of fZ[] working memory with index from 0 to 9m-1
// w/o array header (#, Start, End)
if((fZ=(double*)malloc((9*m)*sizeof(double)))==NULL)
{
    return(-1); // Error - memory reallocation failed
}

// Outer loop thru all nNum-3m+1 subsequences of 3m phase data points
// A subsequence will be processed during each iteration
// and the average used to find Mod-Totvar
// This should allow a max m of nNum/3
// Note: PTTI Paper uses only nNum-3m subsequences
// but at my suggestion the "official" version has now been expanded
// to use nNum-3m+1 as done here

// To handle analysis limits, need to initialize index to nStart-1 not 0
// and end it before nStart-1-3*m+1 instead of nNum-3*m+1
for(i=nStart-1; i<nStart-1+nNum-3*m+1; i++)
{
    // Copy data subsequence into working array starting at index 3m
    // Note: The fX[] array needs offset for its header info
    for(j=0; j<3*m; j++)
    {
        fZ[3*m+j]=fX[i+j+ARRAY_OFFSET];
    }

    // Do removal of frequency offset
    // Find slope fC by averaging the 1st and last halves of the subsequence
    // subtracting them, and dividing by half the interval
    fC1=0;
    fC2=0;
    for(j=0; j<3*m/2; j++)
    {
        fC1+=fZ[3*m+j];
        fC2+=fZ[3*m+(int)ceil(3.0*(double)m/2.0)+j];
    }
    fC1/=(double)(3*m/2);
    fC2/=(double)(3*m/2);
    fC=(fC2-fC1)/ceil(3.0*(double)m/2.0);

    // Then subtract slope from each point
    for(j=0; j<3*m; j++)
    {
        fZ[3*m+j]-=fC*(double)j;
    }

    // Do uninverted even reflection at bottom and top
    for(j=0; j<3*m; j++)
    {
        // Bottom reflection
        fZ[j]=fZ[6*m-1-j];

        // Top reflection
        fZ[6*m+j]=fZ[j];
    }

    // Calc Mvar for the fZ[] subsequence
    // Will need to add gap testing and analysis limits
    // This data array does not need an offset
    // This code implements the right summation of Eq(8) of the reference

```

```
// Initialize inner sum
fSubsum=0;

// We have a doubly-extended subsequence fZ[] of 9m points
// and are going to form m-point averages
// in 6m+1 groups of 3 (called fZ1, fZ2 and fZ3)
// from which all possible fully overlapping 2nd differences
// will be used to calculate Mod Totvar
// Note: Only 6m of the 6m+1 possible 2nd differences are used
// because the last one is a duplicate
// NOTE: For 6m+1 version, use j<6*m+1 instead of j<6*m
for(j=0; j<6*m; j++)
{
    // Find the 3 phase averages for this 2nd difference
    // Initialize phase averages
    fZ1=0.0;
    fZ2=0.0;
    fZ3=0.0;

    // Sum phase averages for 3 sets of m points
    // using points j thru j+m-1, j+m thru j+2m-1 and j+2m thru j+3m-1
    // Note: These phase sums are divided by m = # points of each sum
    // in the 2nd difference expression below
    for(k=j; k<j+m; k++)
    {
        fZ1 += fZ[k];
        fZ2 += fZ[k+m];
        fZ3 += fZ[k+2*m];
    }

    // Calc 2nd difference of one of the 6m sets of 3 phase averages
    fSubsum += SQR((fZ1 - 2*fZ2 + fZ3)/m);
}

// Scale the subsum and add it to overall sum
// NOTE: For 6m+1 version this expression uses (6*m+1) instead of (6*m)
fSum+=fSubsum/(6*m);

// Increment the sum count
nCount++;

// Display progress
// Update when index has changed by at least tic amount
if(((i-nLast_i)>=nTic) && (bProgress))
{
    ProgressFunction((int) (0.5+100.0*i/(nNum-3*m)),
        "Calculating Mod Totdev");
    nLast_i=i;
}

// Check for abort
if(*bAbort)
{
    break;
}
}

// Free the subsequence array
free(fZ);
```

```

// Scale result - See Eq (8) of Reference
// Without gaps, nCount=nNum-3m
fSum/=(fTau*fTau*nAF*nAF*2*nCount);

// Find Mod-Totdev
if(nCount && fSum>0)
{
    *fMTDev=(F_TYPE) sqrt(fSum);
}
else // No result error
{
    *fMTDev=0.0;
    nCount=-2;
}

// Done
// Clear progress display
ProgressFunction(0, "");

return(nCount); // Return # phase analysis points
}

```

The FrequenC Library	
<b>NAME:</b> MJDtoDOY	<b>FUNCTION:</b> Convert Modified Julian Date to Day of Year
<b>SYNOPSIS:</b> int MJDtoDOY(long mjd)	
long mjd	Modified Julian Date
<b>RETURN:</b> int	Day of year
<b>REMARKS:</b> Calls MJDTtoDate()	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ long mjd;   /* MJD */ int doy;   /* DOY */ . . mjd=50000;   /* set MJD */ doy=MJDtoDOY(mjd);                                /* call function */ printf("\nDOY = %d", doy);                          /* display result */ </pre>	
<b>SEE ALSO:</b> MJDTtoDate()	
<b>REFERENCE:</b> None	

```

/*****
/*
/*                               MJDtoDOY()                               */
/*
/*      Function to convert long integer MJD to DOY                        */
/*
/*      Parameters:                                                         */
/*      long      nMJD      MJD value                                     */
/*
/*      Return:    int      nDOY      Day of year                         */
/*
/*      Dependencies:                                                       */
/*      MJDToDate()                                                         */
/*
/*      Revision record:                                                     */
/*      03/20/02      Created                                              */
/*
*****/

#include "frequenc.h"                                     /* FrequenC Library header file */

int __declspec(dllexport) FAR PASCAL MJDtoDOY(long lnMJD)
{
    // Local variables
    // Ints
    int nYear;
    int nDOY;
    int nMonth;
    int nDay;
    static int nSum[] = { 0, 31, 59, 90, 120, 151, 181, 212, 243, 273, 304,
                          334, 365 };

    // Start of code
    // Convert integer MJD to date
    MJDToDate(lnMJD, &nDay, &nMonth, &nYear);

    // Convert data to DOY
    nDOY=nSum[nMonth-1]+nDay;
    if(nYear%4==0 && nYear%100!=0 || nYear%400==0)
    {
        if(nMonth>2)
        {
            nDOY++;
        }
    }

    // Return DOY
    return nDOY;
}

```

The FrequenC Library	
<b>NAME:</b> MJDtoDate	<b>FUNCTION:</b> Convert MJD to calendar date
<b>SYNOPSIS:</b> void MJDtoDate(long mjd, int *day, int *month, int *year)	
long mjd	Modified Julian Date
int *day	Pointer to day #
int *month	Pointer to month #
int *year	Pointer to year
<b>RETURN:</b> void	
<b>REMARKS:</b>	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ long mjd;   /* MJD */ int day;   /* day */ int month;   /* month */ int year;   /* year */ . . mjd=50000;   /* set MJD */ MJDtoDate(mjd, &amp;day, &amp;month, &amp;year);                /* call function */ printf("\nDay = %d, Month = %d, Year = %d", day, month, year); /* display results */ </pre>	
<b>SEE ALSO:</b>	
<b>REFERENCE:</b> None	

## FrequenC Library Reference Manual

```

/*****
/*
/*          MJDtoDate()
/*
/*      Function for MJD to calendar date conversion
/*
/*      Parameters:
/*          long mjd      modified Julian day # to be converted into date
/*          int *day      pointer to day of date to be found from MJD
/*          int *month    pointer to month of date to be found from MJD
/*          int *year     pointer to year of date to be found from MJD
/*
/*      Return:
/*          none (void)
/*
/*      Function revision record:
/*          11/11/92      Created
/*
/*      (c) 1992      W. Riley  Hamilton Technical Services  All Rights Reserved
/*
*****/

#include "frequenc.h"                                /* FrequenC Library header file */

void __declspec(dllexport) FAR PASCAL MJDtoDate(long mjd, int *day,
int *month, int *year)
{
    mjd+=679019;
    *year=(int) ((mjd-122.1)/365.25);
    *month=(int) ((mjd-(long) (365.25**year))/30.6001);
    *day=mjd-(int) (365.25**year)-(int) (30.6001**month);

    if(*month<14)
    {
        *month-=1;
    }
    else
    {
        *month-=13;
    }

    if(*month<3)
    {
        *year+=1;
    }

}

/* end MjdToDate() */

```

The FrequenC Library	
<b>NAME:</b> ModTotvarEDF	<b>FUNCTION:</b> Description of what function does
<b>SYNOPSIS:</b> int FunctionName( F_TYPE z[], F_TYPE one, F_TYPE two)	
F_TYPE z[]	Phase or frequency data array z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE one	parameter one, and description of what it is
F_TYPE two	parameter two, and description of what it is
<b>RETURN:</b> int	# non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are modified. Embedded zeros are treated as gaps in phase data. All zeros are treated as gaps in frequency data.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ F_TYPE one;  /* parameter one */ F_TYPE two;  /* parameter two */ int num;   /* # data points processed */ . . one=1.0;   /* set 1st parameter value */ two=2.0;   /* set 2nd parameter value */ num=FunctionName(z, one, two);                      /* call function */ printf("\n# Data Points Scaled = %d", num);         /* display num */ </pre>	
<b>SEE ALSO:</b> RelatedFunctionName()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*                               ModTotvarEDF()
/*
/*  Function to determine the estimated # of chi-squared degrees of freedom
/*  for the modified total variance (MTOT) of a power law noise process.
/*
/*  Params:          int    nAlpha = alpha
/*                  float fRatio = T/tau = N/m
/*
/*  Return:          float edf = estimated degrees of freedom
/*                      or -1 if error
/*
/*  The edf is modeled by the expression b(T/tau) - c, where:
/*
/*  Alpha    Noise    b    c    Original values
/*  2        W PM    1.90  2.10
/*  1        F PM    1.20  1.40
/*  0        W FM    1.10  1.20
/* -1        F FM    0.85  0.50
/* -2       RW FM    0.75  0.31
/*
/*  Alpha    Noise    b    c    New values per D. Howe
/*  2        W PM    2.16  2.28    e-mail of 05/20/00
/*  1        F PM    1.73  2.99
/*  0        W FM    1.33  1.89
/* -1        F FM    0.92  0.76
/* -2       RW FM    0.79  0.37
/*
/*  Notes:          (1) This function applies only to -2 >= alpha >= 2
/*                      (W PM, F PM, W FM, F FM and RW FM noise)
/*                  (2) This function applies only for m > 8.0
/*                  (3) T is defined as tau0 * # phase data points
/*                  (4) The t/tau ratio should never be < 3
/*
/*  References:      E-Mails from D.A. Howe/NIST, 3/13/00 & 5/20/00
/*
/*  Revision record:
/*      03/25/00    Created
/*      03/30/00    Parameter verification revised
/*      05/21/00    Parameters revised per D. Howe update
/*
/*  (c) Copyright 2000  Hamilton Technical Services  All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

float __declspec(dllexport) FAR PASCAL ModTotvarEDF(int nAlpha, float fRatio)
{
    // Local variables
    float fEDF;

    // Verify parameters
    if(fRatio<3.0)
    {
        return -1.0; // Error
    }
}

```

```

if(nAlpha<-2 || nAlpha>2)
{
    return -1.0; // Error
}

switch(nAlpha)
{
    case 2: // W PM noise
    {
        // fEDF=(float) (1.90*fRatio - 2.10);
        fEDF=(float) (2.16*fRatio - 2.28);
    }
    break;

    case 1: // F PM noise
    {
        // fEDF=(float) (1.20*fRatio - 1.40);
        fEDF=(float) (1.73*fRatio - 2.99);
    }
    break;

    case 0: // W FM noise
    {
        // fEDF=(float) (1.10*fRatio - 1.20);
        fEDF=(float) (1.33*fRatio - 1.89);
    }
    break;

    case -1: // F FM noise
    {
        // fEDF=(float) (0.85*fRatio - 0.50);
        fEDF=(float) (0.92*fRatio - 0.76);
    }
    break;

    case -2: // RW FM noise
    {
        // fEDF=(float) (0.75*fRatio - 0.31);
        fEDF=(float) (0.79*fRatio - 0.37);
    }
    break;
}

return fEDF;
}

```



The FrequenC Library	
<b>NAME:</b> MJDtoGPS	<b>FUNCTION:</b> Convert MJD to GPS Week #
<b>SYNOPSIS:</b> int MJDtoGPS(long MJD)	
long MJD	Modified Julian Date
<b>RETURN:</b> int	Global Positioning System week #
<b>REMARKS:</b> The origin (time zero) of GPS System Time was 00:00:00 UTC on 6 January 1980, Julian Day 2,444,244(.5), MJD 44244. A GPS cycle is 1024 weeks.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ long mjd;   /* MJD */ int week;   /* GPS week # */ . . mjd=50000;   /* set MJD */ week=MJDtoGPS(mjd);                                /* call function */ printf("\nGPS Week = %d", week);                    /* display result */ </pre>	
<b>SEE ALSO:</b> MJDtoDOY(), MJDtoDate()	
<b>REFERENCE:</b>	

## FrequeNC Library Reference Manual

```

/*****
/*
/*          MJDtoGPS()
/*
/*      Function to convert MJD to GPS Week #
/*
/*      Parameters: long    MJD
/*
/*      Return:    int      GPS Week #
/*
/*      Note:    The origin (time zero) of GPS System Time was 00:00:00 UTC
/*                6 January 1980, Julian Day 2,444,244.500, MJD 44244.  A
/*                GPS Cycle is 1024 weeks.
/*
/*      Revision record:
/*                01/25/98    Created
/*
*****/

#include "frequenc.h"                                /* FrequeNC Library header file */

int __declspec(dllexport) FAR PASCAL MJDtoGPS(long MJD)
{
    return ((int)((MJD-44244L)/7)%1024);
}

```

The FrequenC Library	
<b>NAME:</b> CalcMTIE	<b>FUNCTION:</b> Calc maximum time interval error for phase data
<b>SYNOPSIS:</b> <pre>int CalcMTIE(F_TYPE x[], F_TYPE *MTIE, int af, BOOL *abort,              BOOL show, void *ProgressFunc(int percent, char *msg))</pre>	
F_TYPE x[]	Phase data array x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE *MTIE	Pointer to MTIE result
int af	Averaging factor
BOOL *abort	Pointer to abort flag (FALSE = no abort)
BOOL show	Flag to show progress (FALSE = no display)
void *ProgressFunc( int percent, char *msg)	Pointer to function to display progress, with int arg set to % calc complete, and char* arg set to text message to display. Can be NULL.
<b>RETURN:</b> int	# non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are used. Embedded zeros are treated as gaps in phase data.	
<b>EXAMPLE:</b> <pre>#include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[512];                                       /* phase data array */ F_TYPE MTIE;   /* MTIE value */ int af=1;   /* avg factor */ int num;   /* # data points processed */ . . num=CalcMTIE(x, &amp;MTIE, af, FALSE, FALSE, NULL);    /* call function */ /* No aborting or progress display */ printf("\nMTIE = %e", MTIE);                        /* display MTIE */</pre>	
<b>SEE ALSO:</b> TIErms()	
<b>REFERENCE:</b> S. Bregni, "Clock Stability Characterization and Measurement in Telecommunications", IEEE Transactions on Instrumentation and Measurement, Vol. 46, No. 6, Dec 1997, pp 1284-1294, Eq. 13.	

```

/*****
/*
/*          CalcMTIE()
/*
/*  Function to calc MTIE (maximum time interval error) for phase data
/*
/*  Parameters:
/*      F_TYPE fX[]      = data array;          F_TYPE fX[0] = # data points
/*      F_TYPE fX[1]      = analysis start; F_TYPE fX[2] = analysis end
/*      F_TYPE *fMTIE     = pointer to MTIE
/*      int nAF           = averaging factor
/*      BOOL *bAbort      = pointer to abort flag
/*      BOOL bProgress    = progress indicator flag
/*      void *ProgressFunction()
/*                          = pointer to progress indicator function with
/*                          args int nPercentDone and char *szMessage
/*
/*
/*  Return:
/*      num      = # analysis points (not very useful)
/*
/*
/*  Algorithm:
/*      An n-point wide window is moved thru the phase data and the
/*      difference between the maximum and minimum phase (time) values
/*      is found at each window position.  MTIE is the overall maximum
/*      of this time interval error over the whole data set.
/*
/*
/*  Notes:
/*      (1) This function handles gaps because FindMinMax() does.
/*      (2) No test suite values to check results against.  Results are
/*          consistent with the p-p range of the test data.
/*      (3) MTIE has no tau or AF dependence for white pm noise.  It has
/*          a tau+1/2 log slope for W FM noise.  It is very sensitive to
/*          peak values (transients or outliers).
/*      (4) # time intervals is N-1, where N = # phase data points, so
/*          AF can go from 1 to N-1.
/*
/*
/*  Reference:      S. Bregni, "Clock Stability Characterization and
/*                  Measurement in Telecommunications", IEEE
/*                  Transactions on Instrumentation and Measurement,
/*                  Vol. 46, No. 6, Dec 1997, pp 1284-1294, Eq. 14.
/*
/*
/*  Revision record:
/*      12/07/96      Drafted - seems to run OK - patched into Sigma
/*                    function instead of TOTALVAR (for freq data!) since
/*                    that call has same signature.
/*      06/03/98      Put into Stable32
/*      06/04/98      Refined progress display
/*      01/27/01      Extended allowable index by 1
/*      03/09/03      Added abort and progress args
/*
/*
/*  (c) Copyright 1996-2003  Hamilton Technical Services  All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL CalcMTIE(F_TYPE fX[], F_TYPE *fMTIE,
int nAF, BOOL *bAbort, BOOL bProgress,
void *ProgressFunction(int nPercentDone, char *szMessage))

```

```
{
```

```
// Define local variables
// Ints
int i; // Index
int last_i=0; // Previous index
int tic; // Progress interval
int nStart; // Analysis start
int nEnd; // Analysis end
int nNum; // # analysis points
// F_TYPES
F_TYPE fMin; // Min phase data value within window
F_TYPE fMax; // Max phase data value within window

// Set analysis limits & progress interval
nStart=(int) fX[1];
nEnd=(int) fX[2];
nNum=nEnd-nStart+1;
tic=(int) ceil((nNum-nStart-nAF)/100); /* 1% interval for progress report */

// Initialize MTIE value
*fMTIE=0.0;

// Calc MTIE
// The analysis window is nAF points wide. It starts at the 1st data point
// and moves thru all the data until the end of the window is at the end of
// the analysis data.

// Initialize progress display
if(bProgress)
{
    ProgressFunction(0, "Calculating MTIE");
}

// Was i<nNum-nAF until 01/27/00
for(i=nStart; i<=nNum-nAF; i++)
{
    // Find the min & max values within the data window
    fX[1]=i;
    fX[2]=i+nAF;
    FindMinMax(fX, &fMin, &fMax, PHASE_DATA);

    // MTIE is the overall maximum p-p excursion
    *fMTIE=max(*fMTIE, fMax-fMin);

    // Display progress
    // Note: This code provides updates only if index has changed
    // by at least tic amount (1%)
    if( ((i-last_i)>=tic) && (bProgress) )
    {
        ProgressFunction((int) (0.5+100.0*i/(nNum-nStart-nAF)),
            "Calculating MTIE");
        last_i=i;
    }
}
```

```

    // Check for abort
    if(*bAbort)
    {
        // Restore analysis limits
        fX[1]=nStart;
        fX[2]=nEnd;

        // Bail out
        break;
    }
}

// Restore analysis limits
fX[1]=nStart;
fX[2]=nEnd;

// Done
// Clear progress display
if(bProgress)
{
    ProgressFunction(0, "");
}

// Return # analysis points
return nNum;
}

```

The FrequenC Library	
<b>NAME:</b> NormalizeData	<b>FUNCTION:</b> Normalize phase or frequency data by removing mean value
<b>SYNOPSIS:</b> int NormalizeData(F_TYPE z[], F_TYPE avg, BOOL datatype)	
F_TYPE z[]	Phase or frequency data array: z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE avg	Average (mean) value to be removed from data
BOOL datatype	Type of data: 0=phase, 1=frequency
<b>RETURN:</b> int	The # of analysis points (can be 0)
<b>REMARKS:</b> Only data between start and end analysis limits are analyzed. All zeros are treated as gaps in frequency data. Only embedded zeros are treated as gaps in phase data. The datatype flag determines whether the data is treated as phase (datatype=0) or frequency (datatype=1) data. CalcMean() may be used to calculate the value of avg to be removed. No error codes are returned from this function. Returns 0 if all gaps; an array of constant data can be normalized to all zeros, and thus will be treated as all gaps.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* freq data array */ F_TYPE avg;  /* average */ BOOL datatype;                                       /* data type flag */ int num;   /* # analysis points */ . . datatype=FREQ;                                       /* set flag for frequency data */ /* frequenc.h contains #define PHASE 0 and #define FREQ 1 */ CalcMean(y, &amp;avg, datatype)                          /* calc avg */ /* include error check for CalcMean() as required */ num=NormalizeData(y, avg, datatype);                /* normalize data */ printf("\n# Points Processed = %d", num);           /* display num */ </pre>	
<b>SEE ALSO:</b> CalcMean()	
<b>REFERENCE:</b> None	

```

/*****
/*
/*                                     NormalizeData()
/*
/*      Function to normalize phase or freq data by removing mean value
/*
/*      Parameters:      F_TYPE z[]  = phase or freq data
/*                      z[0] = # data points
/*                      z[1] = analysis start
/*                      z[2] = analysis end
/*                      F_TYPE avg  = average value to be removed
/*                      int datatype = data type: 0=phase, 1=frequency
/*
/*      Return:          int          = # non-gap data points (may be 0)
/*
/*      Notes:           All zeros treated as gaps in frequency data
/*                      Embedded zeros are gaps in phase data
/*
/*      Revision record:
/*          12/16/91      Created
/*          12/24/91      Added datatype parameter & int return value
/*          12/26/91      Changed avg parameter from pointer to value
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*
/* (c) Copyright 1991-8  Hamilton Technical Services  All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL NormalizeData(F_TYPE z[], F_TYPE avg,
    BOOL datatype)
{
    int i;
    int n=0;

    for( i = (int)(*(z+1)+2); i <= (int)(*(z+2)+2); i++)
    {
        if(*(z+i) || (!datatype && i==3 || !datatype && i==z[0]+2))
        {
            *(z+i) -= avg;
            n++;
        }
    }
    return(n);
}
/* end NormalizeData() */

```

The FrequenC Library	
<b>NAME:</b> NoiseID	<b>FUNCTION:</b> Determine power law noise type from B1 or R(n) ratio
<b>SYNOPSIS:</b> int WINAPI NoiseID(int num, int sigtype, int af, float bw, float ratio)	
int num	# non-gap data points
int sigtype	Sigma type (e.g. NORMAL_SIGMA macro)
int af	Averaging factor
float bw	Bandwidth factor
float ratio	B1 or R(n) ratio (from data analysis)
<b>RETURN:</b> int	Alpha (power law noise type) -4 <= $\alpha$ <= 2 (RR FM to W PM)
<b>REMARKS:</b> Use CalcStarB1() before call to this function with NORMAL_SIGMA as alternative to using CalcHadamardB1() with Hadamard sigmas. See sigma type macros in frequenc.h.	
<b>EXAMPLE:</b> <pre> #include &lt;frequenc.h&gt;                                /* FrequenC header file */ int alpha;   /* alpha */ int num=100;   /* # data points */ int sigtype=OVERLAPPING_SIGMA;                     /* sigma type */ int af=1;   /* averaging factor */ float bw=10.0;                                       /* BW factor */ float ratio=50.0;                                    /* B1 ratio */     /* B1 found as ratio of standard &amp; Allan variances for the data */ . . alpha=NoiseID(num, sigtype, af, bw, ratio);          /* call function */ printf("\nAlpha = %d", alpha);                       /* display alpha */ </pre>	
<b>SEE ALSO:</b> CalcBias(), CalcRatio(), CalcHadamardB1(), CalcStarB1()	
<b>REFERENCE:</b> NIST Technical Note 1337	

```

/*****
/*
/*                                     NoiseID()
/*
/* Function to determine power law noise type from B1 or R(n) ratio, where:
/*     B1 is ratio of normal variance to Allan variance
/*     R(n) is ratio of modified to normal Allan variance
/*
/* Parameters:      int      nNum          # non-gap data points
/*                  int      nSigmaType    Sigma type
/*                  int      nAvgFactor    Averaging factor
/*                  float    fBW          Bandwidth factor
/*                  float    fRatio       B1 or R(n) ratio
/*
/* Return          int      nAlpha        Alpha (noise type)
/*                                     -4 <= alpha <= 2
/*                                     RR FM to W PM
/*
/* Note 1: Use CalcStarB1() before call to this function with NORMAL_SIGMA
/*         as alternative to using CalcHadamardB1() herein with Hadamard
/*         sigmas.
/*
/* Note 2: Sigma types are as follows:
/*                                     NORMAL_SIGMA
/*                                     OVERLAPPING_SIGMA
/*                                     MODIFIED_SIGMA
/*                                     TIME_SIGMA
/*                                     TOTAL_SIGMA
/*                                     MODTOTAL_SIGMA
/*                                     TIMETOTAL_SIGMA
/*                                     HADAMARD_SIGMA
/*                                     OVERLAPHAD_SIGMA
/*                                     HADTOTAL_SIGMA
/*
/* Revision record:
/*     03/14/99    Added OVERLAPHAD_SIGMA sigma type
/*     04/24/99    Added usage of CalcHadamardB1()
/*     12/26/99    Added MODTOTAL_SIGMA sigma type
/*     05/06/00    Added TIMETOTAL_SIGMA sigma type
/*     11/05/00    Added HADTOTAL_SIGMA sigma type
/*     11/15/00    Moved TIME_SIGMA to with other mod sigma cases
/*     11/23/00    Changed Drift or FW FM case to alpha=-3
/*
/* (c) 1996-9 W. Riley Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL NoiseID(int nNum, int nSigmaType,
int nAvgFactor, float fBW, float fRatio)
{
    // Local variables
    // Ints
    int nAlpha;                                // Alpha exps
    // Floats
    float fB_rrfm, fB_fwfm, fB_rwfm, fB_ffm, fB_wfm, fB_pfm; // Bias functs
    float fR_rwfm, fR_ffm, fR_wfm, fR_fpm, fR_wpm;           // Ratio functs

```

```

#ifdef LOGGING
// Chars
char szBuffer[BUFFER_SIZE+1]; // Text buffer
#endif

switch(nSigmaType)
{
    case NORMAL_SIGMA:
    case OVERLAPPING_SIGMA:
    case TOTAL_SIGMA:
    {
        // Note: 2nd arg in CalcBias() is mu
        fB_fwfm=CalcBias(nNum, 2);
        fB_rwfm=CalcBias(nNum, 1);
        fB_ffm =CalcBias(nNum, 0);
        fB_wfm =CalcBias(nNum, -1);
        fB_pm =CalcBias(nNum, -2);

#ifdef LOGGING
sprintf(szBuffer, "NoiseID() using "
        "fB_fwfm=%f, fB_rwfm=%f, fB_ffm=%f, fB_wfm=%f, fB_pm=%f",
        fB_fwfm, fB_rwfm, fB_ffm, fB_wfm, fB_pm);
WriteLog(60, szBuffer);
#endif

        if(fRatio>((fB_fwfm+fB_rwfm)/2))
        {
            // Drift or FW FM
            // Note: Can make it -2 to avoid alpha<-2
            // which causes trouble in CI calcs
            // Or can let it be -3 to detect FW FM noise
            // and deal with potential CI calc problem separately
            // The latter approach is used
            nAlpha=-3;
        }
        else if(fRatio>sqrt(fB_rwfm*fB_ffm))
        {
            // Random Walk FM
            nAlpha=-2;
        }
        else if(fRatio>sqrt(fB_ffm*fB_wfm))
        {
            // Flicker FM
            nAlpha=-1;
        }
        else if(fRatio>sqrt(fB_wfm*fB_pm))
        {
            // White FM
            nAlpha=0;
        }
        else
        {
            // White or Flicker PM
            // Make it +1 to agree with what Run function does
            nAlpha=1; // Could also be +2
        }
    }
}
break;

```

```

case MODIFIED_SIGMA:
case TIME_SIGMA:
case MODTOTAL_SIGMA:
case TIMETOTAL_SIGMA:
{
    // Note: 1st arg in CalcRatio() is alpha = nAvg Factor
    // Was wrong (nNum) until 02/09/02
    fR_rwfm=CalcRatio(-2, nAvgFactor, fBW);
    fR_ffm =CalcRatio(-1, nAvgFactor, fBW);
    fR_wfm =CalcRatio( 0, nAvgFactor, fBW);
    fR_fpm =CalcRatio( 1, nAvgFactor, fBW);
    fR_wpm =CalcRatio( 2, nAvgFactor, fBW);

#ifdef LOGGING
    sprintf(szBuffer, "NoiseID() using "
        "fR_rwfm=%f, fR_ffm=%f, fR_wfm=%f, fR_fpm=%f, fR_wpm=%f",
        fR_rwfm, fR_ffm, fR_wfm, fR_fpm, fR_wpm);
    WriteLog(60, szBuffer);
#endif

    if(nAvgFactor==1)
    {
        // Undefined
        nAlpha=0;
    }
    else if(fRatio>sqrt(fR_rwfm*fR_ffm))
    {
        // Random Walk FM
        nAlpha=-2;
    }
    else if(fRatio>sqrt(fR_ffm*fR_wfm))
    {
        // Flicker FM
        nAlpha=-1;
    }
    else if(fRatio>sqrt(fR_wfm*fR_fpm))
    {
        // White FM
        nAlpha=0;
    }
    else if(fRatio>sqrt(fR_fpm*fR_wpm))
    {
        // Flicker PM
        nAlpha=1;
    }
    else
    {
        // White PM
        nAlpha=2;
    }
}
break;

```

```

case HADAMARD_SIGMA:
case OVERLAPHAD_SIGMA:
case HADTOTAL_SIGMA:
{
    // Note: 2nd arg in CalcHadamardB1() is mu
    fB_rrfm=CalcHadamardB1(nNum, 3);
    fB_fwfm=CalcHadamardB1(nNum, 2);
    fB_rwfm=CalcHadamardB1(nNum, 1);
    fB_ffm =CalcHadamardB1(nNum, 0);
    fB_wfm =CalcHadamardB1(nNum, -1);
    // Use ordinary B1 ratio for mu=-2 (F or F PM)
    fB_pm =CalcBias(nNum, -2);

#ifdef LOGGING
    sprintf(szBuffer, "NoiseID() using "
        "fB_rrfm=%f, fB_fwfm=%f, fB_ffm=%f, fB_wfm=%f, fB_pm=%f",
        fB_rrfm, fB_fwfm, fB_ffm, fB_wfm, fB_pm);
    WriteLog(60, szBuffer);
#endif

    if(fRatio>((fB_rrfm*fB_fwfm)))
    {
        // RR FM
        nAlpha=-4;
    }
    else if(fRatio>((fB_fwfm*fB_rwfm)))
    {
        // Drift or FW FM
        nAlpha=-3;
    }
    else if(fRatio>sqrt(fB_rwfm*fB_ffm))
    {
        // Random Walk FM
        nAlpha=-2;
    }
    else if(fRatio>sqrt(fB_ffm*fB_wfm))
    {
        // Flicker FM
        nAlpha=-1;
    }
    else if(fRatio>sqrt(fB_wfm*fB_pm))
    {
        // White FM
        nAlpha=0;
    }
    else
    {
        // White or Flicker PM

        // Make it +1 to agree with what Run function does
        nAlpha=1; // Could also be +2
    }
}
break;
}

return nAlpha;
}

```



The FrequenC Library	
<b>NAME:</b> RoundAxes	<b>FUNCTION:</b> Find plot scale
<b>SYNOPSIS:</b> void RoundAxes(F_TYPE *min, F_TYPE *max, F_TYPE *tics)	
F_TYPE min	Pointer to data minimum input; becomes scale minimum output
F_TYPE max	Pointer to data maximum input; becomes scale maximum output
F_TYPE *tics	Pointer to tic size output
<b>RETURN:</b> void	
<b>REMARKS:</b> This function is recommended for a large relative data range.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* freq data array */ double min, max;                                     /* data and scale min &amp; max */ double tics;   /* tic size */ . . FindMinMax(y, &amp;min, &amp;max, FREQ_DATA);               /* get data min &amp; max */ RoundAxes(&amp;min, &amp;max, &amp;tics);                         /* get plot scale */ printf("\nMin = %e, Max = %e, Tics = %e", min, max, tics);   /* display results */ </pre>	
<b>SEE ALSO:</b> FindPlotScale(), BasScale()	
<b>REFERENCE:</b> Ref: Quinn-Curtis S&E Tools IPC-TC-006 SEGRAPH.C	

```

/*****
/*
/*          RoundAxes()
/*
/*      Still another function to find plot scale
/*      Ref: Quinn-Curtis S&E Tools IPC-TC-006 SEGRAPH.C
/*
/*      Parameters:  realtype *a1   =   pointer to data min input
/*                  becomes scale min output
/*                  realtype *a2   =   pointer to data max input
/*                  becomes scale max output
/*                  realtype *tics =   pointer to tics size output
/*
/*      Return:      None (void)
/*
/*      Revision record:
/*          03/10/02   Copied and adapted
/*          03/12/02   Added log 0 trap
/*          03/19/03   Adapted for FrequenC DLL
/*
*****/

// FrequenC header
#include "frequenc.h"

// Local function prototypes
F_TYPE log10x(F_TYPE realnum);
int NumExp(F_TYPE realnum);
F_TYPE PowerCalc(F_TYPE realnum, F_TYPE power);

// RoundAxes function
void __declspec(dllexport) FAR PASCAL RoundAxes(F_TYPE *a1, F_TYPE *a2,
    F_TYPE *tics)
{
    F_TYPE dr1, dr2, px2, pc2;
    int di1, di2, digits, a2neg, alneg;

    alneg = (*a1 < 0);
    a2neg = (*a2 > 0);
    if (NumExp(*a2) > NumExp(*a1))
        px2 = NumExp(*a2) - 1;
    else
        px2 = NumExp(*a1) - 1;
    pc2 = PowerCalc(10.0,px2);
    dr2 = (*a2) / pc2;
    dr1 = (*a1) / pc2;

    di2 = (int)ceil(dr2 + 0.000001+(dr2-dr1)*0.05);
    if ((di2 > 0) && (dr2 <= 0.0)) di2 = 0;

    di1 = (int)floor(dr1 - 0.000001- (dr2-dr1)*0.05);
    if ((di1 < 0) && (dr1 >= 0.0)) di1 = 0;

    if ( abs(di2) < 10 )
        di2 = di2 + a2neg;
    else
        if ( abs(di2) < 60 )
            di2 = ((di2 / 5) + a2neg ) * 5;
        else
            di2 = ((di2 / 10) + a2neg) * 10;
}

```

```

if ( abs(di1) < 60 )
    di1 = ((di1 / 5) - alneg) * 5;
else
    di1 = ((di1 / 10) - alneg) * 10;

*a1 = di1 * pc2;
*a2 = di2 * pc2;
digits = abs(di2 - di1);
if ( digits < 10 )
    *tics = 1.0;
else
    if ( digits < 20 )
        *tics = 2.0;
    else
        if ( digits < 40 )
            *tics = 5.0;
        else
            if ( digits < 80 )
                *tics = 10.0;
            else
                if ( digits < 100 )
                    *tics = 20.0;
                else
                    if ( digits < 151 )
                        *tics = 20.0;
                    else
                        if ( digits < 200 )
                            *tics = 50.0;
                        else
                            *tics = 100.0;

    *tics = *tics * pc2 / 10.0;
}

// Local subroutines adapted from SELIB.C
F_TYPE log10x(F_TYPE realnum)
{
    F_TYPE fret;
    // Avoid log 0
    if(realnum==0.0)
    {
        realnum=1e-99;
    }
    fret = log10(realnum);
    return(fret);
}

int NumExp(F_TYPE realnum)
{
    int fret;
    fret = (int)floor(log10x(fabs(realnum)));
    return(fret);
}

F_TYPE PowerCalc(F_TYPE realnum, F_TYPE power)
{
    F_TYPE fret;
    fret = pow(realnum,power);
    return(fret);
}

```



The FrequenC Library	
<b>NAME:</b> RemoveDiffusionFreqDrift	<b>FUNCTION:</b> Remove the diffusion fit drift from frequency data
<b>SYNOPSIS:</b> int RemoveDiffusionFreqDrift(F_TYPE y[], F_TYPE a, F_TYPE b, F_TYPE c)	
F_TYPE y[]	Frequency data array: y[0] = # data points y[1] = analysis start point y[2] = analysis end point
F_TYPE a	Parameter a of $y(t) = a + b(t+c)^{1/2}$ diffusion fit to the frequency drift to be removed
F_TYPE b	Parameter b of $y(t) = a + b(t+c)^{1/2}$ diffusion fit to the frequency drift to be removed
F_TYPE c	Parameter c of $y(t) = a + b(t+c)^{1/2}$ diffusion fit to the frequency drift to be removed
<b>RETURN:</b> int	The # of non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are processed. All zeros are retained as gaps in the frequency data. Use CalcDiffusionFreqDrift() to calculate fit parameter of drift to be removed. No error codes are returned from this function.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* frequency data array */ F_TYPE a;   /* fit param a */ F_TYPE b;   /* fit param b */ F_TYPE c;   /* fit param c */ num;   /* # data points processed */ . . CalcDiffusionFreqDrift(y, &amp;a, &amp;b, &amp;c);             /* calc diffusion fit */ /* include error check for CalcDiffusionFreqDrift() as required */ num=RemoveDiffusionFreqDrift(y, a, b, c);          /* remove diff drift */ printf("\n# Data Points Processed = %d", num);      /* display num */ </pre>	
<b>SEE ALSO:</b> CalcDiffusionFreqDrift()	
<b>REFERENCE:</b>	

```

/*****
/*
/*          RemoveDiffusionFreqDrift()
/*
/*          Function to remove diffusion frequency drift  $y(t) = a + b\sqrt{t+c}$ 
/*
/*          Parameters:      F_TYPE y[] = frequency data
/*                          y[0] = # frequency data points
/*                          y[1] = analysis start
/*                          y[2] = analysis end
/*                          F_TYPE a   = a term of diffusion fit
/*                          F_TYPE b   = b term of diffusion fit
/*                          F_TYPE c   = c term of diffusion fit
/*
/*          Return:         int        = # data points processed
/*
/*          Notes:          All zeros treated as gaps in frequency data.
/*                          Use function CalcDiffusionFreqDrift() to
/*                          calculate diffusion fit parameters a and b.
/*
/*          Revision record:
/*          06/11/97      Created from first RemoveDiffusionFreqDrift()
/*          12/09/97      Added to FrequenC Library
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*
/* (c) Copyright 1997-8 Hamilton Technical Services    All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL RemoveDiffusionFreqDrift(F_TYPE y[],
    F_TYPE a, F_TYPE b, F_TYPE c)
{
    int i;
    int num=0;

    for(i = (int) *(y+1)+2; i <= (int) *(y+2)+2; i++)
    {
        if(*(y+i))
        {
            *(y+i) -= a + (b * sqrt((double) (i-2)+c));
            num++;
        }
    }

    return(num);
}

```

```
/* return # points processed */
/* end NewRemoveDiffusionFreqDrift() */
```

The FrequenC Library	
<b>NAME:</b> RemoveFreqOffset	<b>FUNCTION:</b> Remove the frequency offset from phase data
<b>SYNOPSIS:</b> int RemoveFreqOffset(F_TYPE x[], F_TYPE a, F_TYPE b, BOOL bA)	
F_TYPE x[]	Phase data array: x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE a	Intercept, a, of $x(t)=a+bt$ linear fit to the frequency offset to be removed
F_TYPE b	Slope, b, of $x(t)=a+bt$ linear fit to the frequency offset to be removed
BOOL c	Flag for constant term removal
<b>RETURN:</b> int	The # of non-gap data points processed
<b>REMARKS:</b> All embedded zeros treated as gaps in phase data. Use CalcFreqOffset() to calculate linear fit parameters a and b. No error codes are returned from this function.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[512];                                       /* phase data array */ F_TYPE a;   /* intercept */ F_TYPE b;   /* slope */ F_TYPE v;   /* fit variance */ BOOL c=TRUE;                                       /* constant removal flag */ int num;   /* # data points processed */ . . CalcFreqOffset(x, &amp;a, &amp;b, &amp;v);                    /* calc linear fit parameters */ num=RemoveFreqOffset(x, a, b, c);                  /* call function */ printf("\n# Data Points Processed = %d", num);      /* display num */ </pre>	
<b>SEE ALSO:</b> CalcFreqOffset()	
<b>REFERENCE:</b>	

```

/*****
/*
/*          RemoveFreqOffset()
/*
/*          Function to remove freq offset from phase data:  $x(t) = a + bt$ 
/*
/*          Parameters:      F_TYPE x[] = phase data
/*                          x[0] = # phase data points
/*                          x[1] = analysis start
/*                          x[2] = analysis end
/*                          F_TYPE a   = intercept of linear fit
/*                          F_TYPE b   = slope of linear fit = freq offset
/*                          BOOL bA    = switch for constant term removal
/*
/*          Return:          int        = # data points processed
/*
/*          Notes:           All embedded zeros treated as gaps in phase data.
/*                          Use function CalcFreqOffset() to calculate linear
/*                          fit parameters a and b.
/*
/*          Revision record:
/*          02/22/97      Adapted from RemoveLinFreqDrift() of FrequenC
/*          02/27/97      Added BOOL bA parameter
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*          04/23/03      Adapted for Version 2.0 source code documentation
/*
/* (c) Copyright 1997-2003 Hamilton Technical Services All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __cdeclspec(dllexport) FAR PASCAL RemoveFreqOffset(F_TYPE x[], F_TYPE a,
F_TYPE b, BOOL bA)
{
    int i;
    int num=0;

    // To avoid compiler warning if parameter a isn't used
    a=a;

    for(i = (int) (*(x+1)+2); i <= (int) (*(x+2)+2); i++) /* analysis limits */
    {
        if( (*(x+i)) || (i==3) || (i==*(x+2)+2) ) /* check for gap */
        {
            if(bA)
            {
                // Remove slope and intercept - make average zero
                *(x+i) -= a + (b * (i-3)); /* remove slope and intercept */
            }
            else
            {
                // Remove slope only
                *(x+i) -= b * (i-2); /* remove slope */
            }
            num++; /* increment count */
        }
    }

    return(num); /* return # points processed */
}

```

The FrequenC Library	
<b>NAME:</b> RemoveLinFreqDrift	<b>FUNCTION:</b> Remove the linear drift from frequency data
<b>SYNOPSIS:</b> int RemoveLinFreqDrift(F_TYPE y[], F_TYPE a, F_TYPE b)	
F_TYPE y[]	Frequency data array: y[0] = # data points y[1] = analysis start point y[2] = analysis end point
F_TYPE a	Intercept, a, of $y(t)=a+bt$ linear fit to the frequency drift to be removed
F_TYPE b	Slope, b, of $y(t)=a+bt$ linear fit to the frequency data to be removed
<b>RETURN:</b> int	The # of non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are processed. All zeros are retained as gaps in the frequency data. Use CalcLinFreqDrift() to calculate intercept and slope to be removed. No error codes are returned from this function.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* frequency data array */ F_TYPE a;   /* intercept */ F_TYPE b;   /* slope */ F_TYPE v;   /* variance */ int num;   /* # data points processed */ . . CalcLinFreqDrift(y, &amp;a, &amp;b, &amp;v);                    /* calc linear fit params */ /* include error check for CalcLinFreqDrift() as required */ num=RemoveLinFreqDrift(y, a, b);                   /* remove linear drift */ printf("\n# Data Points Processed = %d", num);      /* display num */ </pre>	
<b>SEE ALSO:</b> CalcLinFreqDrift()	
<b>REFERENCE:</b> NIST Technical Note 1337, TN-264 to TN-295	

```

/*****
/*
/*          RemoveLinFreqDrift()
/*
/*      Function to remove linear frequency drift  $y(t) = a + bt$ 
/*
/*      Parameters:      F_TYPE y[] = frequency data
/*                      y[0] = # frequency data points
/*                      y[1] = analysis start
/*                      y[2] = analysis end
/*                      F_TYPE a   = intercept of linear fit
/*                      F_TYPE b   = slope of linear fit
/*
/*      Return:          int         = # data points processed
/*
/*      Notes:           All zeros treated as gaps in frequency data.
/*                       Use FrequenC function CalcLinFreqDrift() to
/*                       calculate linear fit parameters a and b.
/*
/*      Revision record:
/*          12/16/91      Created
/*          12/26/91      Changed to int returning # data points processed
/*                       Changed slope & intercept from pointers to values
/*          12/30/91      Changed to include internal call to drift_calc()
/*                       with slope and intercept parameters removed
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*
/* (c) Copyright 1991-8  Hamilton Technical Services  All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL RemoveLinFreqDrift(F_TYPE y[],
    F_TYPE a, F_TYPE b)
{
    int i;                                /* index */
    int num=0;                            /* # points processed */

    for(i = (int) *(y+1)+2; i <= (int) *(y+2)+2; i++) /* analysis limits */
    {
        if(*(y+i))                        /* check for gap */
        {
            *(y+i) -= a + (b * (i-2));    /* remove drift */
            num++;                         /* increment count */
        }                                /* end if */
    }                                    /* end for */

    return(num);                          /* return # points processed */
}                                        /* end RemoveLinFreqDrift() */

```

The FrequenC Library	
<b>NAME:</b> RemoveLogFreqDrift	<b>FUNCTION:</b> Remove the log drift from frequency data
<b>SYNOPSIS:</b> int RemoveLogFreqDrift(F_TYPE y[], F_TYPE a, F_TYPE b, F_TYPE c)	
F_TYPE y[]	Frequency data array: y[0] = # data points y[1] = analysis start point y[2] = analysis end point
F_TYPE a	Multiplicative term, a, of $y(t)=a \cdot \ln(bt+1)+c$ log fit to be removed
F_TYPE b	Time term, b, of log fit to be removed
T_TYPE c	Constant term, c, of log fit to be removed
<b>RETURN:</b> int	The # of non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are analyzed. All zeros are retained as gaps in frequency data. Use CalcLogFreqDrift() to calculate quadratic fit to phase data. No error codes are returned from this function.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE y[512];                                       /* freq data array */ F_TYPE a, b, c, v;                                   /* log fit parameters */ int num;   /* # data points processed */ . . CalcLogFreqDrift(y, &amp;a, &amp;b, &amp;c, &amp;v);                /* calc log fit params */ /* include error check for CalcLogFreqDrift() as required */ num=RemoveLogFreqDrift(y, a, b, c);                 /* remove log drift */ printf("\n# Data Points Processed = %d", num);      /* display num */ </pre>	
<b>SEE ALSO:</b> CalcLogFreqDrift()	
<b>REFERENCE:</b> MIL-O-55310B, General Specification for Crystal Oscillators	

```

/*****
/*
/*          RemoveLogFreqDrift()
/*
/*      Function to remove frequency drift using log model
/*           $y(t) = a \cdot \ln(bt+1) + c$ , where:
/*           $y(t)$  = fractional frequency
/*           $t$  = time
/*           $a$  = multiplicative term
/*           $b$  = log time term
/*           $c$  = constant term
/*
/*      Parameters:      F_TYPE y[] = frequency data
/*                      y[0] = # frequency data points
/*                      y[1] = analysis start
/*                      y[2] = analysis end
/*                      F_TYPE a = log fit parameter a
/*                      F_TYPE b = log fit parameter b
/*                      F_TYPE c = log fit parameter c
/*
/*      Return:          int = # data points processed
/*
/*      Note:            All zeros treated as gaps in frequency data
/*
/*      Revision record:
/*          12/16/91      Created
/*          12/26/91      Changed to int returning # data points processed
/*                      Changed a, b & c from pointers to values
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*
/* (c) Copyright 1991-8  Hamilton Technical Services  All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL RemoveLogFreqDrift(F_TYPE y[],
    F_TYPE a, F_TYPE b, F_TYPE c)
{
    int i;                                /* index */
    int num=0;                             /* # points processed */

    for(i = (int) (*(y+1)+2); i <= (int) (*(y+2)+2); i++) /* analysis limits */
    {
        if(*(y+i))                        /* check for gap */
        {
            *(y+i) -= c + (a * (log((b * (i-2))+1))); /* remove drift */
            num++;                                /* increment count */
        }
        /* end if */
    }
    /* end for */

    return(num);                            /* return # points processed */
}
/* end RemoveLogFreqDrift() */

```

The FrequenC Library	
<b>NAME:</b> RemoveQuadraticDrift	<b>FUNCTION:</b> Remove the quadratic drift from phase data
<b>SYNOPSIS:</b> int RemoveQuadraticDrift(F_TYPE x[], F_TYPE a, F_TYPE b, F_TYPE c)	
F_TYPE x[]	Frequency data array: x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE a	Constant term, a, of $x(t)=a+bt+ct^2$ quadratic fit to be removed
F_TYPE b	Linear term, b, of quadratic fit to be removed
T_TYPE c	Quadratic term, c, of quadratic fit to be removed
<b>RETURN:</b> int	The # of non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are processed. Embedded zeros are retained as gaps in phase data. Use CalcQuadraticDrift() to calculate log fit to frequency data. No error codes are returned from this function.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[513];                                       /* phase data array */ F_TYPE a, b, c, v;                                  /* fit parameters */ int num;   /* # data points processed */ . . CalcQuadraticDrift(x, &amp;a, &amp;b, &amp;c, &amp;v);                /* calc fit params */ /* include error check for CalcQuadraticDrift() as required */ num=RemoveQuadraticDrift(x, a, b, c);               /* remove quad drift */ printf("\n# Data Points Processed = %d", num);      /* display num */ </pre>	
<b>SEE ALSO:</b> CalcLogFreqDrift()	
<b>REFERENCE:</b> NIST Technical Note 1337, TN-264 to TN-295	

```

/*****
/*
/*          RemoveQuadraticDrift()
/*
/*          Function to remove frequency drift from phase data
/*          by removing quadratic fit  $x(t) = a \ln(bt+1) + c$ 
/*
/*          Parameters:      F_TYPE x[] = phase data
/*                          x[0] = # phase data points
/*                          x[1] = analysis start
/*                          x[2] = analysis end
/*                          F_TYPE a  = multiplicative term
/*                          F_TYPE b  = log term
/*                          F_TYPE c  = constant term
/*
/*          Return:         int          = # data points processed
/*
/*          Notes:          Embedded zeros treated as gaps in phase data.
/*                          Use FrequenC function CalcQuadraticDrift() to
/*                          calculate quadratic fit parameters a, b and c.
/*
/*          Revision record:
/*          12/16/90      Created
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          02/03/96      Modified for use as Win 3.1 DLL
/*
/* (c) Copyright 1990-6  Hamilton Technical Services  All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) RemoveQuadraticDrift(F_TYPE x[], F_TYPE a,
F_TYPE b, F_TYPE c)
{
    int i;
    int num=0;

    for( i = *(x+1)+2; i <= *(x+2)+2; i++)
    {
        if(*(x+i))
        {
            *(x+i) -= a + (b * i) + (c * i * i);
            num++;
        }
    }
    return(num);
}

```

```
/* end RemoveQuadraticDrift() */
```

The FrequenC Library	
<b>NAME:</b> SpectrumCalc	<b>FUNCTION:</b> Calculate power spectrum
<b>SYNOPSIS:</b> int SpectrumCalc(F_TYPE z[], float x[], float y[], float tau, int n, int win_num, int win_type, int pn_type, float corr, int af, int data_type)	
F_TYPE z[]	Time-domain data; z[0] = *z = # data points
float x[]	Real data points -> PSD results
float y[]	Im data points (0) -> Fourier freq results
float tau	Time interval of data samples
int n	# analysis data points
int win_num	# windowings
int win_type	Windowing method: Rect=0, Han=1, Ham=2
int pn_type	Phase noise type: 0=S <sub>x</sub> (f), 1=S <sub>φ</sub> (f), 2=ℓ(f)
float corr	Corr factor: 0=1, 1=(2πv <sub>0</sub> ) <sup>2</sup> , 2=(πv <sub>0</sub> ) <sup>2</sup> & x10
int af	Averaging factor (int power of 2)
int data_type	Time-domain data type: 0=phase, 1=freq
<b>RETURN:</b> int	# FFT frequencies
<b>REMARKS:</b> # data points must be a power of 2 Data must not have any gaps	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE z[512];                                       /* time-domain data */ float x[512], y[512];                                /* FFT data */ float tau=1.0, corr=0.0; int n=512, win_num=1, win_type=0, pn_type=2, af=1, data_type=0, freqs; . . freqs=SpectrumCalc(z, x, y, tau, n, win_num, win_type, pn_type, corr, af, data_type);                                     /* call function */ printf("\n# FFT Points = %d", freqs);                /* display # results */ </pre>	
<b>SEE ALSO:</b>	
<b>REFERENCE:</b>	

```

/*****
/*
/*          SpectrumCalc()
/*
/*      Function to calculate & plot power spectrum
/*      Uses FFT functions from Science & Engineering Tools
/*      # data points must be a power of 2
/*      Data must not have any gaps
/*
/*      Function calls from Quinn-Curtis S&E Library:
/*      WindowFFTData()
/*      PowerSpectrumCalc()
/*
/*      Parameters:
/*      y[]          = time-domain data; y[0] = *y = # data points
/*      xdata[]      = real data points -> PSD results
/*      ydata[]      = imaginary data points (0) -> Fourier freq results
/*      tau          = time interval of data samples
/*      n            = # analysis data points
/*      win_num      = # windowings
/*      2*win_type   = windowing method code:
/*          0        = Rectangular          win_type = 0
/*          1        = Parzen (not used)
/*          2        = Hanning              1
/*          3        = Welch (not used)
/*          4        = Hamming              2
/*          5        = Blackman (not used)
/*      phase_noise_type: 0=Sx(f), 1=So(f) , 2=L(f)
/*      correction_factor: 0=1 , 1=(2*ã*v)ý , 2=(ã*v)ý & x10
/*      af           = averaging factor (int power of 2)
/*      data_type     = time-domain data type: 0=phase, 1=freq
/*      Return        = # FFT frequencies
/*
/*      Revision record:
/*      12/26/96      Adapted from spectrum_calc() of Stable/DOS
/*      04/12/97      Added code to preserve original data
/*      04/01/02      Added af parameter & trial code for averaging
/*      07/11/02      Added PSD data saving to disk
/*      07/27/02      Added zero padding
/*      07/30/02      Revised to handle analysis limits
/*      03/20/03      Adapted to FrequenC DLL
/*                      Added data_type argument and return
/*
*****/

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// FrequenC header file
#include "frequenc.h"

```

```

// Local defines
#define realtype float
#ifndef RECTANG
#define RECTANG 0
#define PARZEN 1
#define HANNING 2
#define WELCH 3
#define HAMMING 4
#define EXACTB 5
#endif

```

```
// FFT Windowing Types
#define RECTANGULAR_WIN 0
#define HANNING_WIN 1
#define HAMMING_WIN 2
#define MULTITAPER_WIN 3

// Local function prototypes - not exported
double RemoveMean(float *x, int lx);
void WindowData(realtype *x, int numdat, int window);
void WindowFFTData(realtype *xreal, realtype *yimag, int numdat, int window);
void fft(realtype *xreal, realtype *yimag, int numdat, int flag);
void PowerSpectrumCalc(realtype *xreal, realtype *yimag, int numdat, realtype delta);
void fft2 (realtype *aa, realtype *bb, int n, int m, int ks);
void reorder (realtype *aa, realtype *bb, int n, int m, int ks, int reel);

// SpectrumCalc() top-level function
int __declspec(dllexport) FAR PASCAL SpectrumCalc(F_TYPE y[], float xdata[],
    float ydata[], float tau, int n, int win_num, int win_type,
    int phase_noise_type, float correction_factor, int af, int data_type)
{
    int i; // General index
    int j; // Index for # windowings
    int k; // Index for averaging
    static int offset; // Index of first analysis data point
    static int nn; // Padded array size
    static int nNum; // # data points in input array
    static int nFFT; // # data points in one FFT section
    static float pad_factor; // Correction factor for zero padding
    static float correction[3][4] =
    {
        { (float)0.00, (float)0.000, (float)0.000, (float)0.000 },
        // Rectangular
        { (float)0.00, (float)0.426, (float)0.563, (float)0.647 },
        // Hanning
        { (float)0.00, (float)0.401, (float)0.542, (float)0.627 }
        // Hamming
    };

    // These are log power amplitude corrections factors for wideband noise
    // 1st index is win_type; 2nd index is win_num
    static float bw_correction;
    static float log_mult;
    static F_TYPE avg;

    // The xdata array gets loaded with the time domain data.
    // This array is allocated with space for the # points & analysis limits.
    // These are put into the xdata array initially to allow it to use the
    // FillFloatGaps() function.
    // Then the header info is removed from the xdata array for the FFT calcs.

    // Input parameter n the # of analysis points - not necessarily a power-of-2

    // Find data offset
    offset=(int)y[1]+2; // Index of first data point to be analyzed

    // Copy analysis limits info into xdata[]
    xdata[0]=(float)n;
    xdata[1]=(float)1;
    xdata[2]=(float)n;

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// Load analysis data into the xdata array with header info
for(i=0; i<n; i++)
{
    xdata[i+ARRAY_OFFSET]=(float)y[i+offset];
}

// Make sure no there are gaps in the analysis data
FillFloatGaps(xdata, data_type);

// Eliminate header from the analysis data
for(i=0; i<n; i++)
{
    xdata[i]=xdata[ARRAY_OFFSET+i];           /* real data points */
    ydata[i]=0.0;                             /* imaginary data points */
}

// Remove DC component
RemoveMean(xdata, n);

// The original FFT code just analyzes the entire data set as one block
// w/o averaging. Thus a longer record at the same tau increases the
// frequency resolution but does not reduce the variance of the FFT
// results. To do that, one must break the data into sections, analyze
// each section separately, and then average them to produce better FFT
// values. Doing so obviously shortens each individual data record, so
// the FFT results won't extend to as low a Fourier frequency. The variance
// of the FFT values is thereby reduced from 100% to 100% divided by the
// sqrt of the # averages, which should be an integer power of 2.
// The averaged FFT can be done in the same pair of xdata and ydata arrays.
// The xdata array starts with the real data points, and is filled with the
// PSD results. The ydata array starts with 0's and gets the Fourier freqs.
// For averaging, just FFT each section separately in-place. Then sum the
// PSDs and Fourier freqs in the 1st section, and divide them by # averages.
// Then continue to apply BW correftion and log mult to 1st section.
// Both nNum and nAF are integer powers of 2, so k is also
// e.g. if n is 512 and nAF is 8 then k goes from 0 to 7
// and each section of FFT has nFFT=64 points.

// Find size of next higher power-of-two = allocated size
nn=(int)pow(2.0, (double)(ceil(log(n)/log(2))));

// Zero the padded portion of the data
for(i=n; i<nn; i++)
{
    xdata[i]=0.0;                             /* real data points */
    ydata[i]=0.0;                             /* imaginary data points */
}

// Zero padding correction factor
// Square of ratio of total to actual (non-zero) FFT points
pad_factor=((float)(nn)*(float)(nn))/((float)(n)*(float)(n));

// Calc the # of averaged FFT points
nFFT=nn/af;

// Perform FFT on each section
for(k=0; k<af; k++)
{
    // Apply the desired windowing function
    j=win_num;

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while(j--)
{
    WindowFFTData(&xdata[k*nFFT], &ydata[k*nFFT], nFFT, win_type);
    /* window win_num times */
}

// Calculate the power spectrum using S&E function
PowerSpectrumCalc(&xdata[k*nFFT], &ydata[k*nFFT], nFFT, tau);
/* calc power spectrum */
}

// Sum the results into the 1st section
// Note that summation starts a k=1 (not k=0) - don't add 1st section to itself
for(k=1; k<af; k++)
{
    for(i=0; i<nFFT; i++)
    {
        xdata[i]+=xdata[k*nFFT+i];
        ydata[i]+=ydata[k*nFFT+i];
    }
}

// Find the average values in 1st section
for(i=0; i<nFFT; i++)
{
    xdata[i]/=af;
    ydata[i]/=af;
}

// Calc bandwidth correction
bw_correction=(float)log10(ydata[1]);

// Apply zero padding correction
correction_factor*=pad_factor;

// Set log multiplier factor
if(phase_noise_type==2) /* L(f) */
{
    log_mult=10;
}
else /* Sx(f) & So(f) */
{
    log_mult=1;
}

// Drop dc term from PSD and convert spectral data to log form
// Note that xdata is PSD & ydata is Fourier freq
for(i=0; i<(nFFT/2)-1; i++)
{
    ydata[i]=ydata[i+1]; /* Fourier frequency values */
    if(xdata[i+1]>0)
    {
        xdata[i]=(float)(log_mult*(log10(xdata[i+1]*correction_factor)
            - bw_correction + correction[win_type/2][win_num]));
        /* power spectrum values plus correction factors */
    }
}

```

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        else
        {
            // Error in power spectrum calc
            break;
        }
    }

    // Save PSD data - Must move to Stable32 calling function
    // PSDWrite(szPSDFile, ydata, xdata, (nFFT/2)-1);

    return (nFFT/2)-1;
}

/*****
/*
/*      Quinn-Curtis Science & Engineering Library FFT Functions      */
/*
/*      TC-006 S/N 18146 Rev 8.01 Date: 6/1/92 File: FFT.C (Excerpt)  */
/*
/*      Functions:                                                    */
/*      Parzen()      Hanning()      Hamming()      ExactBlackman()    */
/*      Welch()      WindowData()    WindowFFTData()  fft()           */
/*      fft2()        reorder()       SumAnd Square()  PowerSpectrumCalc() */
/*
/*      Note: The Stable/Win usage of these functions is with realtype */
/*      defined as a float. The local header fft_.h is a special version */
/*      of fft.h that calls in reetype.h which defines realtype as float */
/*      and has prototypes for these functions.                        */
/*
/*      Copyright (c) Quinn-Curtis, 1992                               */
/*
*****/

// File macros
#ifndef M_PI // Defined in math.h under Borland C++ but not Visual C++
#define M_PI      3.14159265358979323846
#endif

/* Apply a parzen window */
realtype Parzen (realtype n, realtype j)
{
    realtype fret;

    fret = (realtype) (1.0 - fabs((j - 0.5 * (n - 1.0)) / (0.5 * (n - 1.0))));
    return(fret);
}

/* Apply a hanning window */
realtype Hanning (realtype n, realtype j)
{
    realtype fret;

    fret = (realtype) (0.5 * (1.0 - cos(2.0 * M_PI * j / (n-1.0))));
    return(fret);
}

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/* Apply a hamming window */
realtype Hamming (realtype n, realtype j)
{
    realtype fret;

    fret = (realtype) (0.54 - 0.46 * cos(2.0 * M_PI * j / (n-1.0)));
    return(fret);
}

/* Apply a blackman window */
realtype ExactBlackman (realtype n, realtype j)
{
    realtype fret;

    fret = (realtype) (0.42 - 0.50 * cos(2.0 * M_PI * j / (n-1.0)) +
        0.08 * cos(4.0 * M_PI * j / (n-1.0)));
    return(fret);
}

/* Apply a welch window */
realtype Welch (realtype n, realtype j)
{
    realtype fret;
    fret = (realtype) ((j - 0.5 * (n - 1.0)) / (0.5 * (n + 1.0)));
    fret = (realtype) (1.0 - fret*fret);
    return(fret);
}

/* Apply a window for an array */
void WindowData (realtype *x, int numdat, int window)
{
    int i;
    realtype multiplier;

    for ( i = 0; i < numdat; i++ )
    {
        switch ( window )
        {
            case RECTANG:
                multiplier = (realtype) 1.0;
                break;
            case PARZEN:
                multiplier = Parzen ((realtype)numdat, (realtype)i);
                break;
            case HANNING:
                multiplier = Hanning ((realtype)numdat, (realtype)i);
                break;
            case WELCH:
                multiplier = Welch ((realtype)numdat, (realtype)i);
                break;
            case HAMMING:
                multiplier = Hamming ((realtype)numdat, (realtype)i);
                break;
            case EXACTB:
                multiplier = ExactBlackman ((realtype)numdat, (realtype)i);
                break;
            default:
                multiplier = (realtype) 1.0;
                break;
        }
    }
}

```

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        x[i] = multiplier * x[i];
    }
}

/* Apply a window for both x and y data sets */
void WindowFFTDData (realtype *xdata, realtype *ydata, int numdat, int window)
{
    WindowData (xdata, numdat, window);
    WindowData (ydata, numdat, window );
}

/* Complex Fourier Transform */
/* number of points n must be a power of 2 */
void fft (realtype *xr, realtype *yi, int n, int inverse)
{
    int nn, j;
    int      m;
    realtype pp, qq;

    m = -1;
    nn = n;

    /* determine power of 2 */
    while (nn > 0)
    {
        nn = nn >> 1;
        m++;
    }

    fft2 (xr, yi, n, m, n);
    reorder (xr, yi, n, m, n, 0);
    if (inverse)
    {
        pp = (realtype) 1.0 / n;
        qq = -pp;
        for (j = 0; j < n; j++)
        {
            xr [j] *= pp;
            yi [j] *= qq;
        }
    }
    else
    {
        for (j = 0; j < n; j++)
            yi[j] = -yi[j];
    }
}

/* FFT for one variable of dimension n = 2^m */
void fft2 (realtype *x, realtype *y, int n, int m, int ks)
{
    int      indx, k0, k1, k2, k3, span, j, k, kb, kn, mm, mk;
    realtype  rad, c1, c2, c3, s1, s2, s3, ck, sk, sq;
    realtype  x0, x1, x2, x3, y0, y1, y2, y3;
    int *cc;

    cc = (int *) calloc (m + 1, sizeof (int));

    sq = (realtype) 0.707106781187;
    sk = (realtype) 0.382683432366;

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ck = (realtype) 0.92387953251;

cc[m] = ks;
mm = (m / 2) * 2;
kn = 0;
for (k = m - 1; k >= 0; k--)
    cc[k] = cc[k+1] / 2;
rad = (realtype) 6.28318530718 / (cc[0] * ks);
mk = m - 5;

do
{
    kb = kn;
    kn = kn + ks;

    if (mm != m)
    {
        k2 = kn;
        k0 = cc[mm] + kb;
        do
        {
            k2--;
            k0--;
            x0 = x[k2];
            y0 = y[k2];
            x[k2] = x[k0] - x0;
            x[k0] = x[k0] + x0;
            y[k2] = y[k0] - y0;
            y[k0] = y[k0] + y0;
        } while (k0 > kb);
    }

    c1 = (realtype) 1.0, s1 = (realtype) 0.0;
    indx = 0;
    k = mm - 2;
    j = 3;

    if (k >= 0)
        goto l2;
    else
        if (kn < n)
            continue;
        else
            break;

l1:    while (1)
    {
        if (cc[j] <= indx)
        {
            indx = indx - cc[j];
            j--;
            if (cc[j] <= indx)
            {
                indx = indx - cc[j];
                j--;
                k += 2;
            }
        }
    }

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```

        else
            break;
    }

    indx = cc[j] + indx;
    j = 3;

12:    span = cc[k];
    if (indx != 0)
    {
        c2 = indx * span * rad;
        c1 = (realtype) cos (c2);
        s1 = (realtype) sin (c2);

15:        c2 = c1 * c1 - s1 * s1;
        s2 = (realtype) 2.0 * s1 * c1;
        c3 = c2 * c1 - s2 * s1;
        s3 = c2 * s1 + s2 * c1;
    }
    for (k0 = kb + span - 1; k0 >= kb; k0--)
    {
        k1 = k0 + span;
        k2 = k1 + span;
        k3 = k2 + span;
        x0 = x[k0];
        y0 = y [k0];
        if (s1 == 0)
        {
            x1 = x[k1]; y1 = y [k1];
            x2 = x[k2]; y2 = y [k2];
            x3 = x[k3]; y3 = y [k3];
        }
        else
        {
            x1 = x[k1] * c1 - y [k1] * s1;
            y1 = x[k1] * s1 + y [k1] * c1;
            x2 = x[k2] * c2 - y [k2] * s2;
            y2 = x[k2] * s2 + y [k2] * c2;
            x3 = x[k3] * c3 - y [k3] * s3;
            y3 = x[k3] * s3 + y [k3] * c3;
        }
        x [k0] = x0 + x2 + x1 + x3; y[k0] = y0 + y2 + y1 + y3;
        x [k1] = x0 + x2 - x1 - x3; y[k1] = y0 + y2 - y1 - y3;
        x [k2] = x0 - x2 - y1 + y3; y[k2] = y0 - y2 + x1 - x3;
        x [k3] = x0 - x2 + y1 - y3; y[k3] = y0 - y2 - x1 + x3;
    }
    if (k > 0)
    {
        k = k - 2;
        goto 12;
    }
    kb = k3 + span;
    if (kb < kn)
    {
        if (j == 0)
        {
            k = 2;
            j = mk;
            goto 11;
        }
    }

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        j--;
        c2 = c1;
        if (j == 1)
        {
            c1 = c1 * ck + s1 * sk;
            s1 = s1 * ck - c2 * sk;
        }
        else
        {
            c1 = (c1 - s1) * sq;
            s1 = (s1 + c2) * sq;
        }
        goto 15;
    }
}
while (kn < n);

free (cc);
}

void reorder ( realtype *x, realtype *y, int n, int m, int ks, int reel)
{
    int i, j, indx, k, kk, kb, k2, ku, lim, p;
    realtype temp;

    int *cc, *lst;

    cc = (int *) calloc (m + 1, sizeof (int));
    lst = (int *) calloc (m + 1, sizeof (int));

    cc [m] = ks;
    for (k = m; k > 0; k--)
        cc [k-1] = cc [k] / 2;
    p = j = m - 1;
    i = kb = 0;
    if (reel)
    {
        ku = n - 2;
        for (k = 0; k <= ku; k += 2)
        {
            temp = x [k + 1];
            x [k + 1] = y [k];
            y [k] = temp;
        }
    }
    else
        m--;
    lim = (m + 2) / 2;
    if (p > 0)
    do
    {
        ku = k2 = cc [j] + kb;
        indx = cc [m - j];
        kk = kb + indx;

        do
        {
            k = kk + indx;

```

```

        do
        {
            temp = x [kk];
            x [kk] = x [k2];
            x [k2] = temp;
            temp = y [kk];
            y [kk] = y [k2];
            y [k2] = temp;
            kk++;
            k2++;
        }
        while (kk < k);

        kk = kk + indx;
        k2 = k2 + indx;
    }
    while (kk < ku);

    if (j > lim)
    {
        j--, i++;
        lst [i] = j;
        continue;
    }
    kb = k2;
    if (i > 0)
    {
        j = lst [i];
        i--;
        continue;
    }
    if (kb < n)
        j = p;
    else
        break;
}
while (1);

free (cc);
free (lst);
}

realtype SquareAndSum (realtype a, realtype b)
{
    realtype fret;

    fret = a * a + b * b;
    return(fret);
}

/* Calculate the power spectrum periodogram of a sampled dataset */
void PowerSpectrumCalc(realtype *xreal, realtype *yimag,
    int numdat, realtype delta)
{
    realtype timespan, normal, n;
    int i;

    n = (float)numdat;
    normal = (realtype) 1.0 / (n * n);
    fft (xreal, yimag, numdat, 0);

```

```

xreal[0] = SquareAndSum (xreal[0], yimag[0]) * normal;

for (i = 1; i <= (numdat / 2) - 1; i++)
{
    xreal[i] = normal * (SquareAndSum(xreal[i], yimag[i]) +
        SquareAndSum (xreal[numdat - i], yimag[numdat - i]));
}
i = numdat / 2;
xreal[i] = SquareAndSum(xreal[i], yimag[i]) * normal;
timespan = (realtype) ((1.0*numdat) * delta);
for (i = 0; i <= (numdat/2); i++)
{
    yimag[i] = (realtype) (1.0*i) / timespan;
}
}

/* Remove mean from data array */
/* Cloned from same code used in multitaper PSD calc */
double RemoveMean(float *x, int lx)
{
    int k;
    double mean;

    mean = 0.;
    if(lx<2)
    {
        return mean;
    }

    for(k=0; k<=lx; k++)
    {
        mean= x[k]+mean;
    }

    mean=mean/(float)lx;

    for(k=0; k<=lx; k++)
    {
        x[k]=(float) (x[k]-mean);
    }

    return mean;
}

```



The FrequenC Library	
<b>NAME:</b> ScaleData	<b>FUNCTION:</b> Scale phase or frequency data by a+bx
<b>SYNOPSIS:</b> int ScaleData(F_TYPE z[], F_TYPE add, F_TYPE mult)	
F_TYPE z[]	Phase or frequency data array: z[0] = # data points z[1] = analysis start point z[2] = analysis end point
F_TYPE add	Addend, the number to be added to all non-gap data points
F_TYPE mult	Multiplier, the number to multiply all data points by
<b>RETURN:</b> int	The # of non-gap data points processed
<b>REMARKS:</b> Only data points between start and end analysis limits are modified. Multiplication is done first, then addition. Embedded zeros are treated as gaps in phase data. All zeros are treated as gaps in frequency data. No error codes are returned from this function.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE z[512];                                       /* data array */ F_TYPE add;  /* addend */ F_TYPE mult;   /* multiplier */ int num;   /* # data points processed */ . . add=1.0;   /* set addend value */ mult=5.0;   /* set multiplier value */ num=ScaleData(z, add, mult);                         /* scale data */ printf("\n# Data Points Scaled = %d", num);         /* display num */ </pre>	
<b>SEE ALSO:</b> None	
<b>REFERENCE:</b> None	

```

/*****
/*
/*          ScaleData()
/*
/*      Function to scale phase or frequency data by multiplying by a
/*      multiplier constant and adding an addend constant:
/*      z[i] = addend + z[i] * multiplier
/*
/*      Parameters:      F_TYPE z[] = data array
/*                      z[0] = # data points
/*                      z[1] = analysis start
/*                      z[2] = analysis end
/*                      F_TYPE add = addend
/*                      F_TYPE mult = multiplier
/*                      int datatype = data type: 0=phase, 1=frequency
/*
/*      Notes:          All zeros treated as gaps in frequency data
/*                      Embedded zeros are gaps in phase data
/*
/*      Return:         int          = # non-gap values processed
/*
/*      Revision record:
/*          12/16/91      Created
/*          12/26/91      Changed to int returning # data points processed
/*                      Added datatype parameter; changed array to z[]
/*                      Changed add and mult to values not pointers
/*          12/31/91      Renamed
/*          01/18/92      Edited title block
/*          02/03/96      Modified for use as Win 3.1 DLL
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*
/* (c) Copyright 1991-8  Hamilton Technical Services  All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __cdeclspec(dllexport) FAR PASCAL ScaleData(F_TYPE z[], F_TYPE add,
F_TYPE mult, BOOL datatype)
{
    int i;
    int num=0;

    for(i = (int) (*(z+1)+2); i <= (int) (*(z+2)+2); i++)
    {
        if(*(z+i) || (!datatype && i==3 || !datatype && i==z[0]+2))
        {
            *(z+i) *= mult;          /* multiply data by multiplier */
            *(z+i) += add;           /* add addend to data */
            num++;
        }
    }
    return(num);
}
/* end ScaleData() */

```

The FrequenC Library	
<b>NAME:</b> TotvarBias	<b>FUNCTION:</b> Calculate TOTVAR bias
<b>SYNOPSIS:</b> float TotvarBias(int nAlpha, float fRatio)	
int alpha	Alpha of power law noise type (-2 to +2)
float ratio	Record length/tau = $T/\tau = \tau_0 \cdot N / \tau$
<b>RETURN:</b> float	TOTVAR bias factor, or -1 if error
<b>REMARKS:</b> The TOTALVAR bias factor is the ratio of the expected value of TOTVAR to AVAR. To correct a calculated TOTDEV value for a certain noise type, record length & analysis tau, divide it by the square root of the bias factor returned by this function. It applies to $-2 \geq \alpha \geq 2$ (W PM, F PM, W FM, F FM, RW FM noise), and for $T/\tau \geq 2.0$ , where $T = \tau_0 \cdot \#$ phase data points. No bias correction is necessary for W PM, F PM & W FM noise ( $\alpha = 2, 1$ or $0$ ).	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ int alpha=0;  /* alpha */ float ratio=10.0;                                    /* record length/tau */ float bias;  /* TOTVAR bias factor */ . . bias=TotvarBias(alpha, ratio);                      /* call function */ if(bias== -1.0)                                     /* check for error */ {     printf("\nError");                             /* error message */ } else {     printf("\nTOTVAR Bias = %e", bias);              /* display result */ } </pre>	
<b>SEE ALSO:</b> TotvarEDF(), TotvarCalc()	
<b>REFERENCES:</b> D.A. Howe, "Method of Improving the Estimation of Long-Term Frequency Variance", Proc. 11th EFTF, March, 1997, and private e-mail communication from C.A. Greenhall/JPL via D.A. Howe/NIST 03/28/97.	

```

/*****
/*
/*          TotvarBias()
/*
/*      Function to calculate the TOTVAR bias function
/*
/*      Parameters:      int    nAlpha = noise type (-2 to +2)
/*                      float fRatio = T/ç
/*
/*
/*      Return:          float fBias  = TOTVAR bias factor
/*                          or -1 if error
/*
/*
/*      The TOTVAR bias factor is the ratio of the expected value of
/*      TOTVAR to AVAR. To correct a calculated TOTDEV value for a
/*      certain noise type, record length & analysis tau, calc the T/ç
/*      ratio, call this function, and divide the uncorrected TOTDEV value
/*      by the square root of the bias factor returned by this function.
/*
/*
/*      Notes:           (1) This function applies to -2 >= alpha >= 2
/*                          (W PM, F PM, W FM, F FM, RW FM noise)
/*                          (2) This function applies only for T/ç >= 2.0
/*                          (3) T is defined as ç0 * # phase data points
/*                          (4) No bias correction is necessary for W PM,
/*                              F PM & W FM noise (alpha=2, 1 or 0)
/*
/*
/*      Reference:       D.A. Howe and C.A. Greenhall, "Total Variance: A
/*                          Progress Report on a New Frequency Stability
/*                          Characterization", Proc. 29th PTTI Meeting,
/*                          Dec. 2, 1997, (to be published).
/*
/*
/*                          TOTVAR Bias Factor = 1 - a * (tau / T)
/*                          where  a = 0 for W FM noise (no bias) (alpha=0)
/*                                  = 1/(3 ln 2) for F FM noise (alpha=-1)
/*                                  = 3/4      for RW FM noise (alpha=-2)
/*
/*
/*                          Note that the fRatio entered is T/tau not tau/T!
/*
/*
/*      Revision record:
/*          12/06/97      Created & debugged
/*          12/09/97      Added to FrequenC Library
/*          12/21/97      Fixed error reported by D. Howe/NIST:
/*                          F FM and RW FM constants were reversed
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*
/* (c) Copyright 1997      Hamilton Technical Services    All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

float __declspec(dllexport) FAR PASCAL TotvarBias(int nAlpha, float fRatio)
{
    // Local variables
    float fBias;

```

```

// Verify parameters
if(fRatio<2.0)
{
    return -1.0; // Error
}

if(nAlpha<-2 || nAlpha>2)
{
    return -1.0; // Error
}

// Sort by noise type
switch(nAlpha)
{
    case -2: // RW FM
    {
        fBias=(float)(1.0 - 0.7500/fRatio);
    }
    break;

    case -1: // F FM
    {
        fBias=(float)(1.0 - 0.4809/fRatio);
    }
    break;

    case -0: // W FM
    {
        fBias=1.0;
    }
    break;

    case 1: // F PM
    {
        fBias=1.0;
    }
    break;

    case 2: // W PM
    {
        fBias=1.0;
    }
    break;
}

return (fBias);
}

```



The FrequenC Library	
<b>NAME:</b> TotvarCalc	<b>FUNCTION:</b> Calculate TOTVAR using doubly reflected phase data
<b>SYNOPSIS:</b> int TotvarCalc(F_TYPE x[], F_TYPE *totdev, F_TYPE tau, int af, void *progress)	
F_TYPE x[]	Phase data array: x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE *totdev	Pointer to total deviation
F_TYPE tau	Averaging time of data $\tau_0$
int af	Averaging factor $\tau/\tau_0$
void *progress( int percent, char *msg)	Pointer to function to display progress, with int arg set to % calc complete, and char* arg set to text message to display. Can be NULL.
<b>RETURN:</b> int	# TOTVAR analysis points, or -1 if memory alloc error, or -2 if no result error
<b>REMARKS:</b> Calculation is done in new array that is deleted after function closes. The progress indicator is not necessary. The phase data need not be end matched before calling this function.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ F_TYPE x[512];                                       /* data array */ F_TYPE totdev;                                       /* TOTDEV */ F_TYPE tau=1.0;                                     /* meas interval */ int af=2;   /* avg factor */ int num;   /* return code */ . . num=TotvarCalc(x, totdev, tau, af, NULL);           /* call function */ if(num&lt;0)   /* check for error */ {     printf("\nError");                             /* error message */ } else {     printf("\nTOTDEV = %e", totdev);               /* display result */ }           </pre>	
<b>SEE ALSO:</b> TotvarEDF(), TotvarBias()	
<b>REFERENCE:</b> D.A. Howe and C.A. Greenhall, "Total Variance: A Progress Report on a New Frequency Stability Characterization", Proc. 29th PTTI Meeting, Dec. 1997.	

```

/*****
/*
/*                               TotvarCalc()
/*
/*      Function to calculate TOTVAR using doubly reflected phase data
/*
/*      Parameters:      F_TYPE x[]      =   phase data
/*                      x[0] = # data points
/*                      x[1] = analysis start
/*                      x[2] = analysis end
/*
/*                      F_TYPE *TotDev= pointer to TOTDEV
/*                      F_TYPE fTau    = interval between phase data points
/*                      int nAF        = averaging factor
/*                      void *lpfnProgress = ptr to progress display funct
/*
/*      Return:          int              = # TOTALVAR analysis points,
/*                                      or -1 if memory alloc error
/*                                      or -2 if no result error
/*
/*      Notes:           1. Calculation is done entirely with a new array.
/*                       that is deleted after this function closes.
/*                       2. Progress indicator and abort not necessary.
/*                       3. The phase data need NOT be endmatched before
/*                           calling this function.
/*
/*      Reference:       D.A. Howe and C.A. Greenhall, "Total Variance: A
/*                       Progress Report on a New Frequency Stability
/*                       Characterization", Proc. 29th PTTI Meeting,
/*                       Dec. 2, 1997, (to be published).
/*
/*      Revision record:
/*          12/06/97      Adapted from ReflectedTotalvarCalc()
/*          12/09/97      Added to FrequenC Library
/*          01/01/98      Changes for MS VC++ compatibility & warnings
/*
/* (c) Copyright 1997-8 Hamilton Technical Services    All Rights Reserved
/*
*****/

```

// Headers

#include "frequenc.h"

#include <windowsx.h> // For GlobalAllocPtr() & GlobalAllocFree()

// For Win 3.1 and Win32 Compatibility

#ifndef WIN32

#define HUGE huge

#else

#define HUGE

#endif

// Defines

#define ARRAY\_OFFSET 3 // Offset to 1st data point

```

int __declspec(dllexport) FAR PASCAL TotvarCalc(F_TYPE fX[], F_TYPE *fTotDev,
F_TYPE fTau, int nAF, void *lpfnProgress)

```

```

{

```

```

    // Local variables

```

```

    int i;                // Index

```

```

    int j;                // Auxiliary index

```

```

    int nNum;             // # points

```

```

int nStart;           // Analysis start
int nDummy;           // Dummy variable to avoid compiler warning
int nCount=0;         // # analysis points

#if(0) // Not needed if no progress indicator
int nTic;             // Increment for progress indicator
int nLast_i=0;        // Previous value of index
#endif

double HUGE *fP;      // TOTVAR phase array pointer
F_TYPE fSum=0;         // TOTVAR summation
F_TYPE fEdge;          // Phase data value at edge of reflection

// Avoid compiler warning if no progress indicator
lpfnProgress=lpfnProgress;

// Initializations
nStart=(int)fX[1];      // Analysis start point
nNum=(int)(fX[2]-fX[1]+1); // # analysis phase data points = N

#if(0) // Not needed if no progress indicator
nTic=(int)ceil(nNum/100); // Increment for progress report

if(lpfnProgress!=NULL)
{
    lpfnProgress(0, "Calculating Total Sigma"); // Label progress bar
}
#endif

#if(0) // For testing - check input params
TRACE_EXP(fTau);
TRACE_INT(nStart);
TRACE_INT(nNum);
#endif

// Allocate a new "virtual" phase data array to size 3N-4, where N is
// the # of phase data points to be analyzed. This virtual array is the
// result of extension by reflection about both endpoints. N-2 reflected
// points are added at both ends of the original phase data to be analyzed.
// Do NOT need the array header (#, Start, End)
// Note that fP is cast to a huge double ptr and that array size is long
if((fP=(double HUGE *)GlobalAllocPtr(GHND,
    (long)(3*nNum-4)*sizeof(double)))==NULL)
{
    #if(0) // Eliminated for FrequenC DLL usage
    AllocErrorMessage();
    #endif
    return(-1); // Error - memory reallocation failed
}

// Note that in the referenced paper the index of the virtual phase data
// array goes from 3-N (a negative number) to 2N-2 (a positive number),
// with the original data having indices from 1 to N. Our indices start at
// 0 and go to 3N-5. The lower reflected data has indices from 0 to N-3.
// The original data in the middle of the virtual array has indices from
// N-2 to 2N-3. The upper reflected data has indices from 2N-2 to 3N-5.

// Copy original phase data array fX[] to (headerless) working array fP[]
// Analysis limits are handled by copying only the points between the
// start and end. i is the index into the virtual array fP[]. j is the

```

```

// variable part of the index into the original phase data array fX[].
j=0;
for(i=nNum-2; i<2*nNum-2; i++)
{
    fP[i]=fX[j+nStart+ARRAY_OFFSET-1];
    j++;
}

// Fill the lower reflected phase data
// These values are twice the first phase data point minus the particular
// data point value to be reflected
j=0;
fEdge=2*fP[nNum-2];

for(i=0; i<nNum-2; i++)
{
    fP[i]=fEdge-fP[2*nNum-4-j];
    j++;
}

// Fill the upper reflected phase data
// These values are twice the last phase data point minus the particular
// data point value to be reflected
j=0;
fEdge=2*fP[2*nNum-3];

for(i=2*nNum-2; i<3*nNum-4; i++)
{
    fP[i]=fEdge-fP[2*nNum-4-j];
    j++;
}

#if(0) // For testing - examine virtual array
for(i=0; i<3*nNum-4; i++)
{
    TRACE_EXP(fP[i]);
}
#endif

// Calc TOTVAR - See Eq (3) of Reference
for(i=nNum-1; i<2*nNum-3; i++)
{
    #if(1) // To eliminate gap checking
    // Check for gap
    if( (fP[i-nAF] && fP[i] && fP[i+nAF]) ||
        (i==nNum+nAF-2) ||
        (i==2*nNum-nAF-3) ) )
    #endif
    {
        // Sum 2nd differences
        fSum+=SQR(fP[i-nAF]-2*fP[i]+fP[i+nAF]);
        nCount++;
    }
    #if(0) // For testing - display gap index
    else
    {
        TRACE_INT(i);
    }
}
#endif

```

```

    #if(0) // Not needed if no progress indicator or abort
    // Display progress
    // Note: This code provides updates only if index has changed
    // by at least tic amount
    // Uses pointer to progress display function PFVi argument
    // Pass NULL for no progress display
    if(((i-nLast_i)>=nTic) && (lpfnProgress!=NULL))
    {
        lpfnProgress(0.5+100.0*i/nNum, "Calculating Total Sigma");
        nLast_i=i;
    }

    // Check for abort
    if(bAbort)
    {
        nCount=0; /* force error */
        break;
    }
    #endif
}

#if(0) // For testing - display # points analyzed
TRACE_INT(nCount);
#endif

// Scale result - See Eq (3) of Reference
fSum/=(fTau*fTau*nAF*nAF*2*nCount);

// Find TOTDEV
if(nCount && fSum>0)
{
    *fTotDev=sqrt(fSum);
}
else // No result error
{
    *fTotDev=0.0;
    nCount=-2;
}

// Free memory
nDummy=GlobalFreePtr(fP);
nDummy=nDummy;

return(nCount); // Return # phase analysis points
}

```



The FrequenC Library	
<b>NAME:</b> TotvarEDF	<b>FUNCTION:</b> Determine the equivalent # of chi-squared degrees of freedom for the total variance.
<b>SYNOPSIS:</b> float TotvarEDF(int alpha, float ratio)	
int alpha	Alpha of power law noise process
float ratio	$T/\tau = \tau_0 \cdot N/\tau$ = Record length/averaging time
<b>RETURN:</b> float	float edf = equivalent # of degrees of freedom or -1 if error
<b>REMARKS:</b> This function applies only to $-2 \leq \alpha \leq 0$ (W FM, F FM and RW FM noise), and for $T/\tau \geq 2.0$ , where $T = \tau_0 \cdot \#$ phase data points.	
<b>EXAMPLE:</b> <pre> #include "frequenc.h"                                /* FrequenC header file */ int alpha=0;  /* alpha */ float ratio=10.0;                                    /* ratio */ float edf;   /* edf */ . . edf=TotvarEDF(alpha, ratio);                          /* call function */ if(num==-1)   /* check for error */ {     printf("\nError");                               /* error message */ } else {     printf("\nEDF = %f", edf);                       /* display result */ }           </pre>	
<b>SEE ALSO:</b> TotvarCalc(), TotvarBias()	
<b>REFERENCE:</b> D.A. Howe and C.A. Greenhall, "Total Variance: A Progress Report on a New Frequency Stability Characterization", Proc. 29th PTTI Meeting, Dec. 1997.	

```

/*****
/*
/*                               TotvarEDF()
/*
/*  Function to determine the estimated # of chi-squared degrees of freedom
/*  for the total variance (TOTVAR) of a power law noise process.
/*
/*
/*  Params:           int    nAlpha = alpha
/*                   float fRatio = T/ç
/*
/*  Return:           float edf = estimated degrees of freedom
/*                   or -1 if error
/*
/*
/*  Notes:            (1) This function applies only to -2 >= alpha >= 0
/*                   (W FM, F FM and RW FM noise)
/*                   (2) This function applies only for T/ç >= 2.0
/*                   (3) T is defined as ç0 * # phase data points
/*
/*  Reference:        D.A. Howe and C.A. Greenhall, "Total Variance: A
/*                   Progress Report on a New Frequency Stability
/*                   Characterization", Proc. 29th PTTI Meeting,
/*                   Dec. 2, 1997, (to be published).
/*
/*
/*  Revision record:
/*      12/06/97      Created
/*      12/09/97      Added to FrequenC Library
/*      01/01/98      Changes for MS VC++ compatibility & warnings
/*
/*  (c) Copyright 1997-8  Hamilton Technical Services  All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

float __declspec(dllexport) FAR PASCAL TotvarEDF(int nAlpha, float fRatio)
{
    // Local variables
    float fEDF;

    #if(0) // For testing
    TRACE_INT(nAlpha);
    TRACE_EXP(fRatio);
    #endif

    // Verify parameters
    if(fRatio<2.0)
    {
        return -1.0; // Error
    }

    if(nAlpha<-2 || nAlpha>0)
    {
        return -1.0; // Error
    }
}

```

```

switch(nAlpha)
{
    case 0:      // W FM noise
    {
        fEDF=(float) (1.500*fRatio);
    }
    break;

    case -1:     // F FM noise
    {
        fEDF=(float) (1.16832*fRatio - 0.222);
    }
    break;

    case -2:     // RW FM noise
    {
        fEDF=(float) (0.92715*fRatio -0.358);
    }
    break;
}

#ifdef 0 // For testing
TRACE_EXP(fEDF);
#endif

return fEDF;
}

```



The FrequenC Library	
<b>NAME:</b> TIErms	<b>FUNCTION:</b> Calc rms time interval error for phase data
<b>SYNOPSIS:</b> <pre>int TIErms(F_TYPE x[], F_TYPE *TIE, int af)</pre>	
F_TYPE x[]	Phase data array x[0] = # data points x[1] = analysis start point x[2] = analysis end point
F_TYPE *TIE	Pointer to TIE rms result
int af	Averaging factor
<b>RETURN:</b> int	# non-gap data points processed, or -1 if error
<b>REMARKS:</b> Only data points between start and end analysis limits are used. Embedded zeros are treated as gaps in phase data. Must have at least 1 analysis point; this requires at least 2 adjacent non-gap phase data points.	
<b>EXAMPLE:</b> <pre>#include &lt;frequenc.h&gt; F_TYPE x[512]; F_TYPE TIE; int af=1; int num; . . num=TIErms(x, &amp;TIE, af); printf("\nTIE rms = %e", TIE);</pre> <pre>/* FrequenC header file */ /* phase data array */ /* TIE value */ /* avg factor */ /* # analysis points */ /* call function */ /* display TIE rms */</pre>	
<b>SEE ALSO:</b> CalcMTIE()	
<b>REFERENCE:</b> S. Bregni, "Clock Stability Characterization and Measurement in Telecommunications", IEEE Transactions on Instrumentation and Measurement, Vol. 46, No. 6, Dec 1997, pp 1284-1294, Eq. 13.	

```

/*****
/*
/*          TIErms()
/*
/*      Function to calc rms time interval error from phase data
/*
/*      Parameters:      F_TYPE fX[]      = phase data array
/*                      fX[0] = # data points
/*                      fX[1] = analysis start
/*                      fX[2] = analysis end
/*                      F_TYPE *fTIE     = pointer to TIE rms
/*                      int nAF          = averaging factor
/*
/*      Returns:         int              = # analysis points,
/*                                     or -1 if error
/*
/*      Note:            Embedded zero value treated as gap in phase data.
/*                      Must have at least 1 analysis point; this
/*                      requires at least 2 adjacent non-gap phase
/*                      data points.
/*
/*      Reference:       S. Bregni, "Clock Stability Characterization and
/*                      Measurement in Telecommunications", IEEE
/*                      Transactions on Instrumentation and Measurement,
/*                      Vol. 46, No. 6, Dec 1997, pp 1284-1294, Eq. 13.
/*
/*      Revision record:
/*                      06/03/98      Created
/*
/*      (c) Copyright 1998  Hamilton Technical Services  All Rights Reserved
/*
*****/

```

```
#include "frequenc.h"
```

```

int __declspec(dllexport) FAR PASCAL TIErms(F_TYPE fX[], F_TYPE *fTIE,
int nAF)
{
    F_TYPE fSum=0;                /* summing variable to calc TIE */
    int i;                        /* index for summing */
    int nNum=0;                   /* # analysis points */

    for( i = (int)(fX[1]+2); i <= (int)(fX[2]+2-nAF); i++)
        /* For full analysis limits, index goes from 3 to nNum+2-nAF */
        /* In summation, smallest index is 1st data point=3, and */
        /* largest index is nNum+2 */
        {
            if( (i==fX[1]+2 && fX[i+nAF])
                || (fX[i] && fX[i+nAF])
                || (i==fX[2]+2-nAF && fX[i]))
                /* skip if any embedded phase data value is zero */
            {
                fSum += SQR(fX[i+nAF] - fX[i]);
                nNum++;
            }
        }

    if(nNum>0)
    {
        *fTIE=sqrt(fSum/nNum);

        return(nNum);                /* # analysis points */
    }
    else
    {
        *fTIE=0;
        return(-1);                  /* error */
    }
}

```

}

## Notes